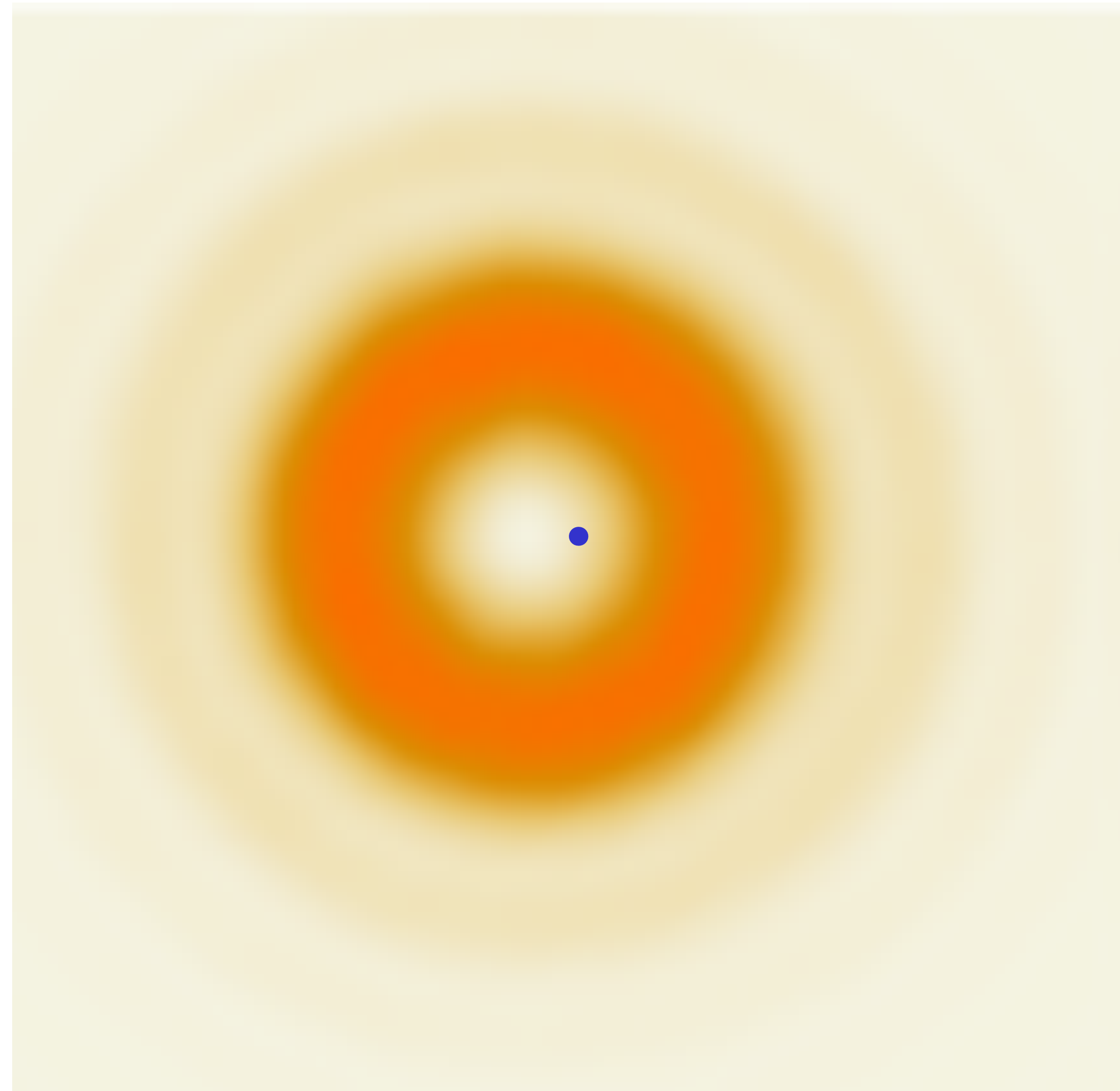


How to twist, turn, and kick ions using structured light



Slides ↓ ↓



Christian Schmiegelow
Universidad de Buenos Aires & CONICET
Ciudad de Buenos Aires - Argentina

Paraty 2025 - RJ - Brasil

Structure of this course

- 1) Structured light basics
- 2) Structured light and atoms
- 3) Structured light and optical forces

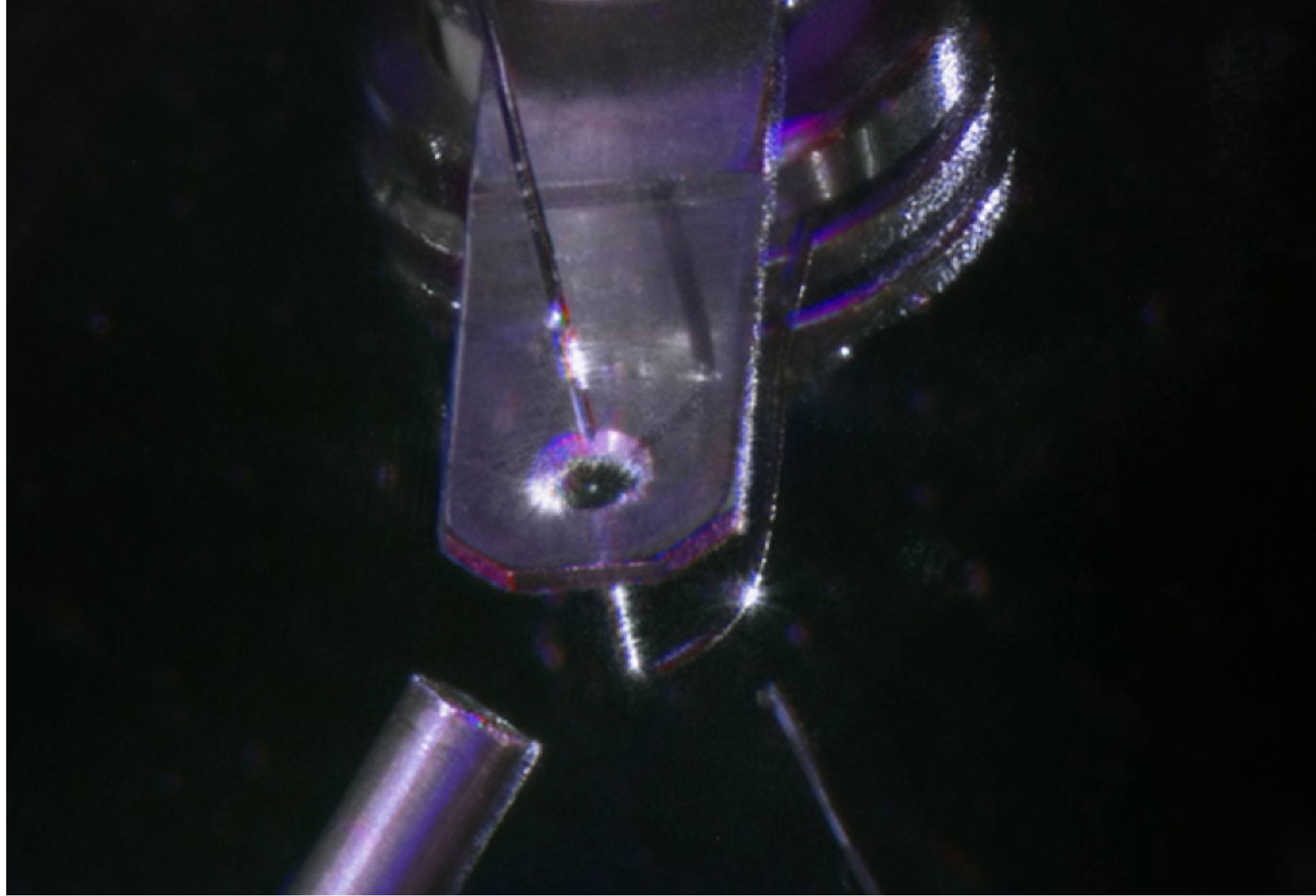
Day Three

Part 0

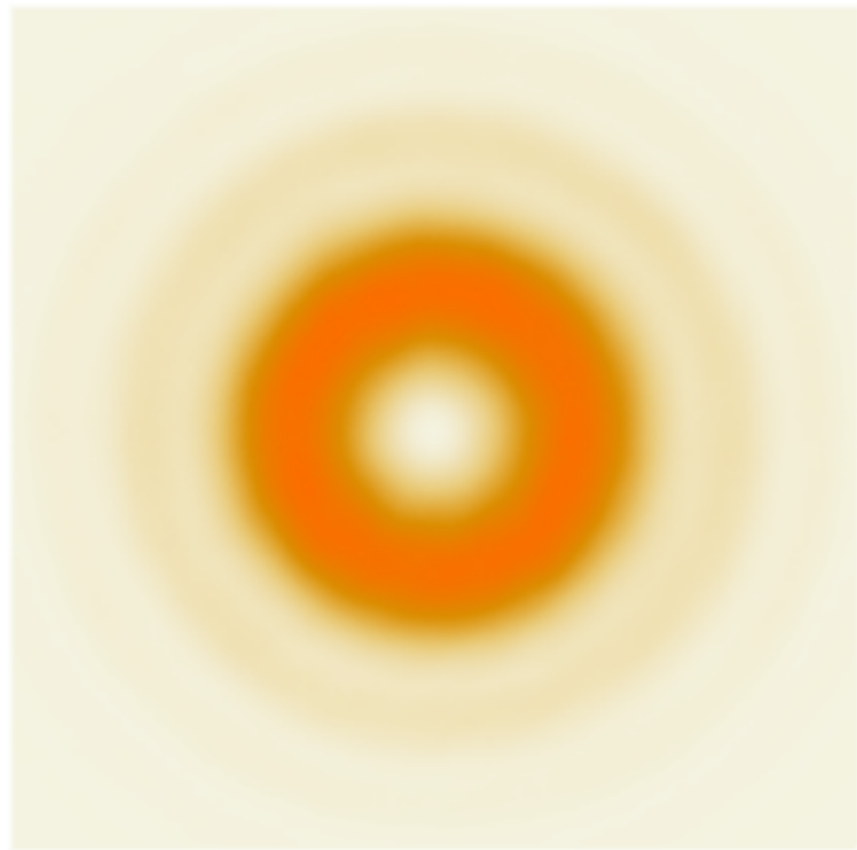
Review Day 1 & 2

Dancing in the dark - the Sao Paulo anecdote, ca. 2008

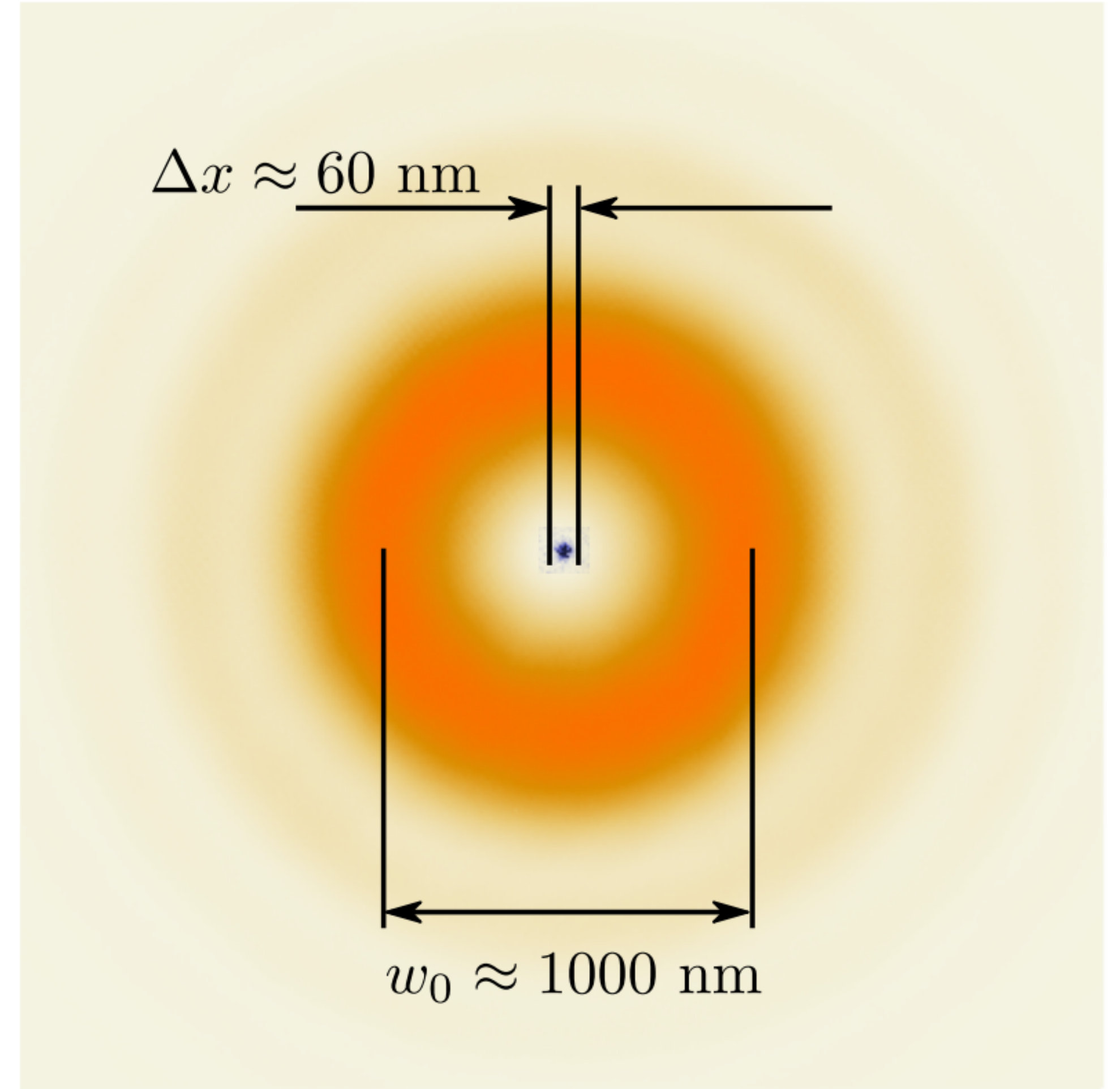
an ion trap



a hollow beam



ion in a beam

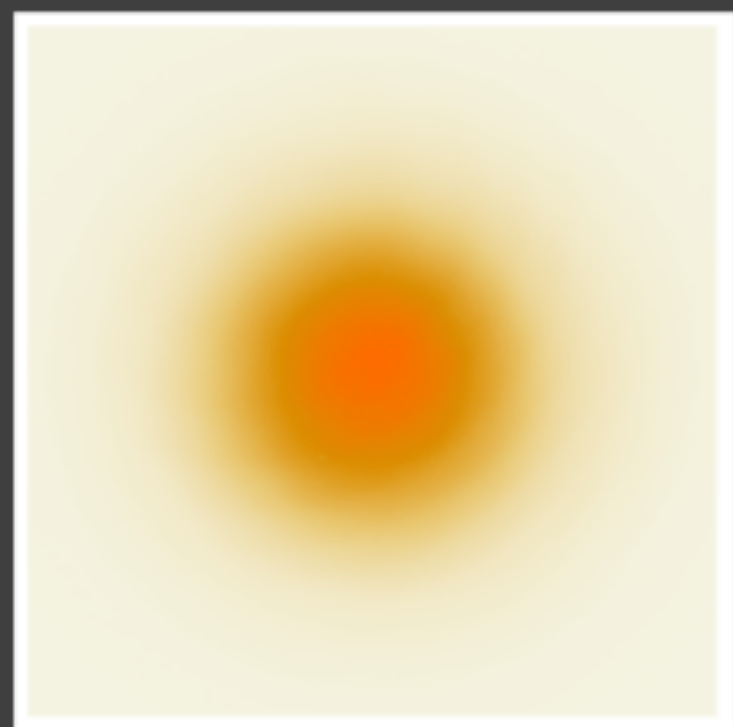


Twisted Light

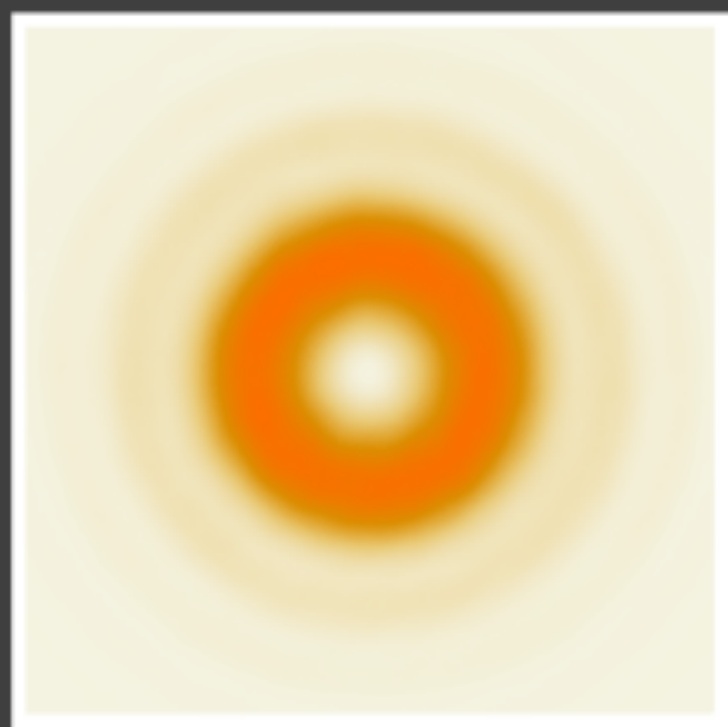
$$A = A_{lp}(\rho, \phi, z) \vec{e} e^{ikz} e^{-i\omega t}$$

$$\mathbf{A}_{lp} = \mathbf{A}_0 \frac{w_0}{w(z)} \exp \left(\frac{-\rho^2}{w(z)} + \frac{ik\rho^2}{2R(z)} + i\Phi_g(z) \right)$$

$$\sqrt{\frac{2p!}{\pi(|l|+p)!}} \left(\frac{\sqrt{2}\rho}{w(z)} \right)^{|l|} \mathcal{L}_p^{|l|} \left(\frac{2\rho^2}{w^2(z)} \right) \exp(il\phi)$$



$l = 0$



$l = 1$



$l = 2$

Dancing in the dark Structured light beams - Laguerre- Gauss type.

Equation of the LG beams

$$A = A_{lp}(\rho, \phi, z) \vec{e} e^{ikz} e^{-i\omega t}$$

$$\mathbf{A}_{lp} = \mathbf{A}_0 \frac{w_0}{w(z)} \exp \left(\frac{-\rho^2}{w(z)} + \frac{ik\rho^2}{2R(z)} + i\Phi_g(z) \right)$$

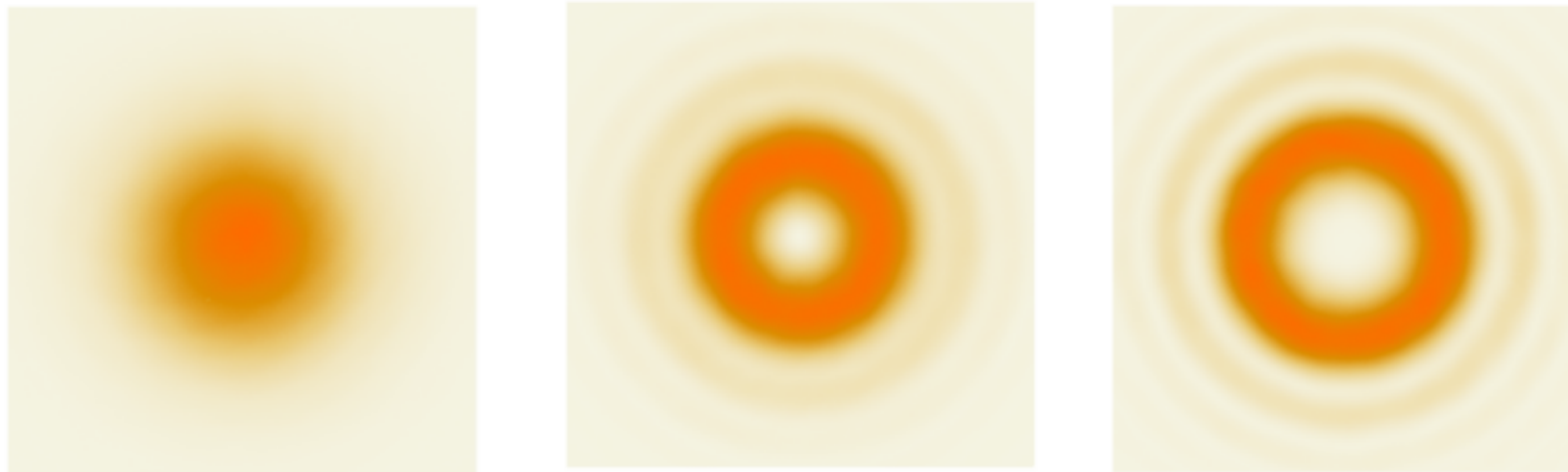
$$\sqrt{\frac{2p!}{\pi(|l|+p)!}} \left(\frac{\sqrt{2}\rho}{w(z)} \right)^{|l|} \mathcal{L}_p^{|l|} \left(\frac{2\rho^2}{w^2(z)} \right) \exp(il\phi)$$

Light Angular Momentum

$$\mathbf{M}_z = \frac{l}{\omega} |u|^2 + \frac{\sigma_z r}{2\omega} \frac{\partial |u|^2}{\partial r} .$$

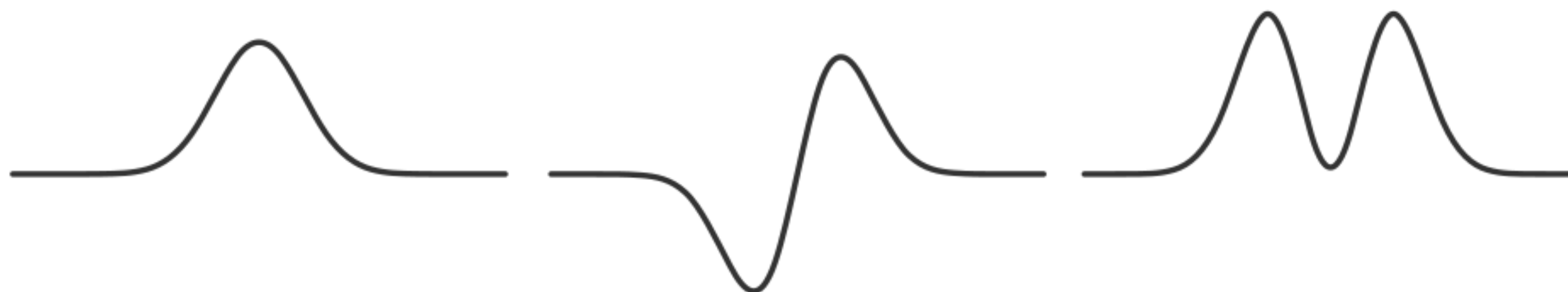
$|A_{pl}(x, y)|^2$

Intensity



$A_{pl}(x)$

Field



Orbital Angular Momentu - first experiment

VOLUME 75, NUMBER 5

PHYSICAL REVIEW LETTERS

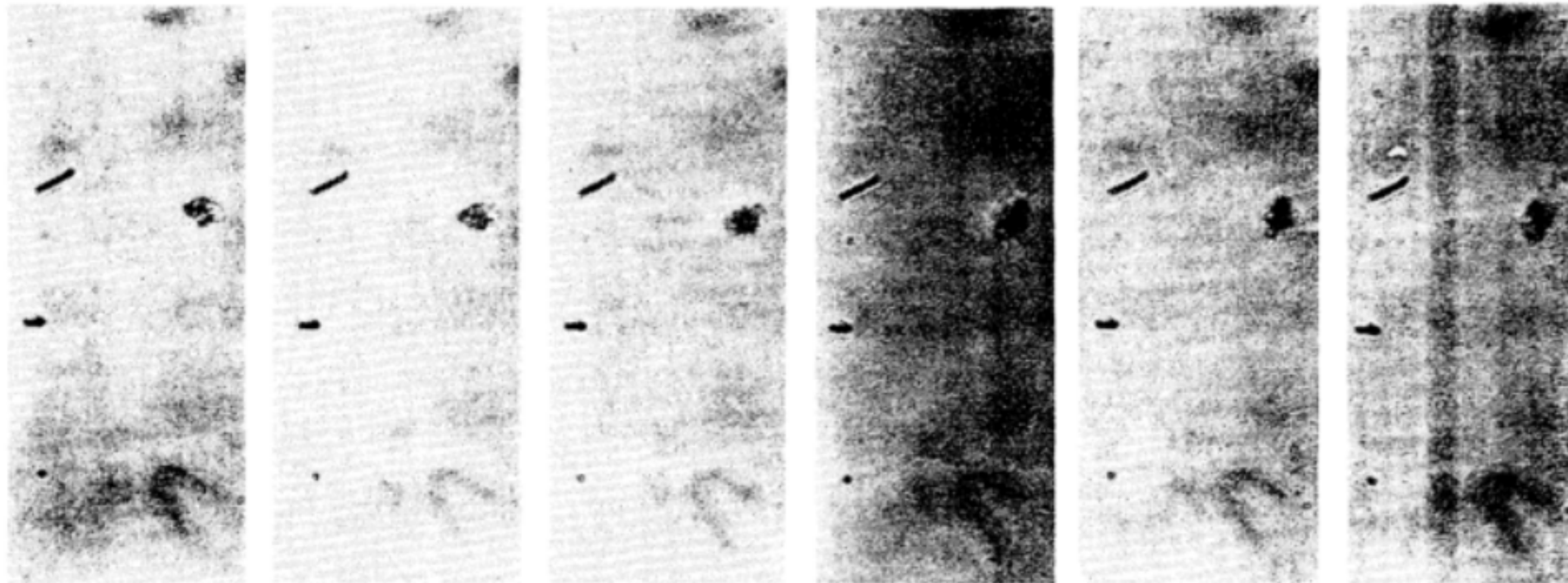
31 JULY 1995

pg. 826

Direct Observation of Transfer of Angular Momentum to Absorptive Particles from a Laser Beam with a Phase Singularity

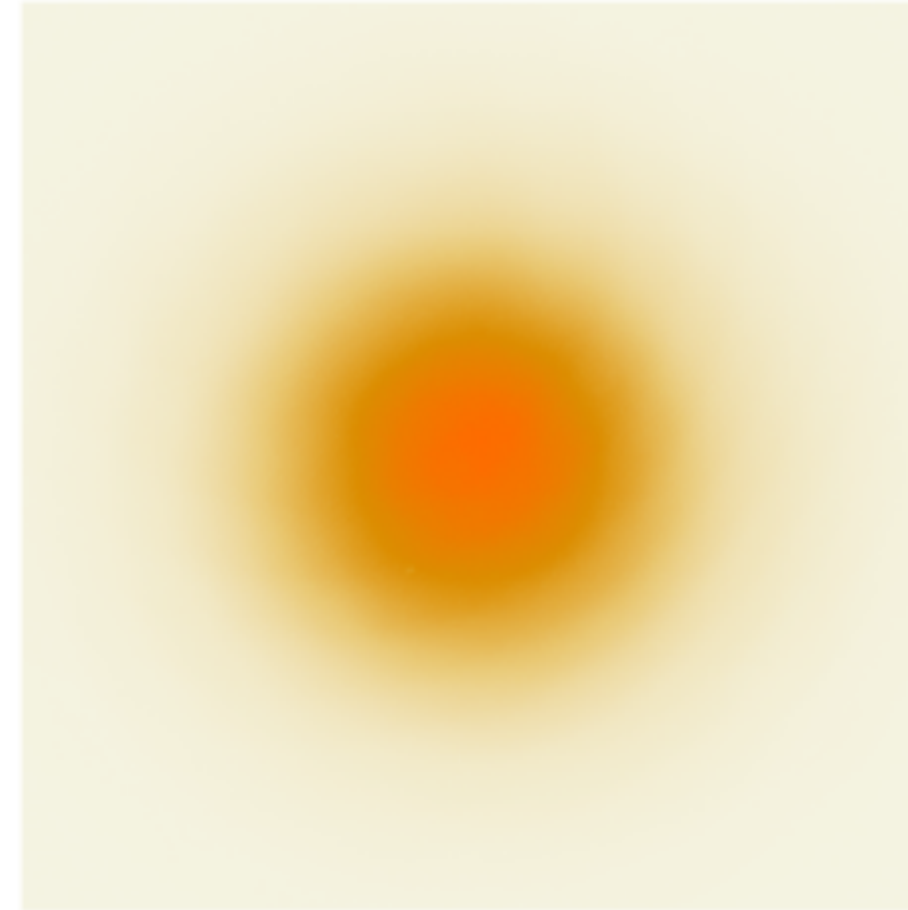
H. He, M. E. J. Friese, N. R. Heckenberg, and H. Rubinsztein-Dunlop

Department of Physics, The University of Queensland, Brisbane, Queensland, Australia Q4072

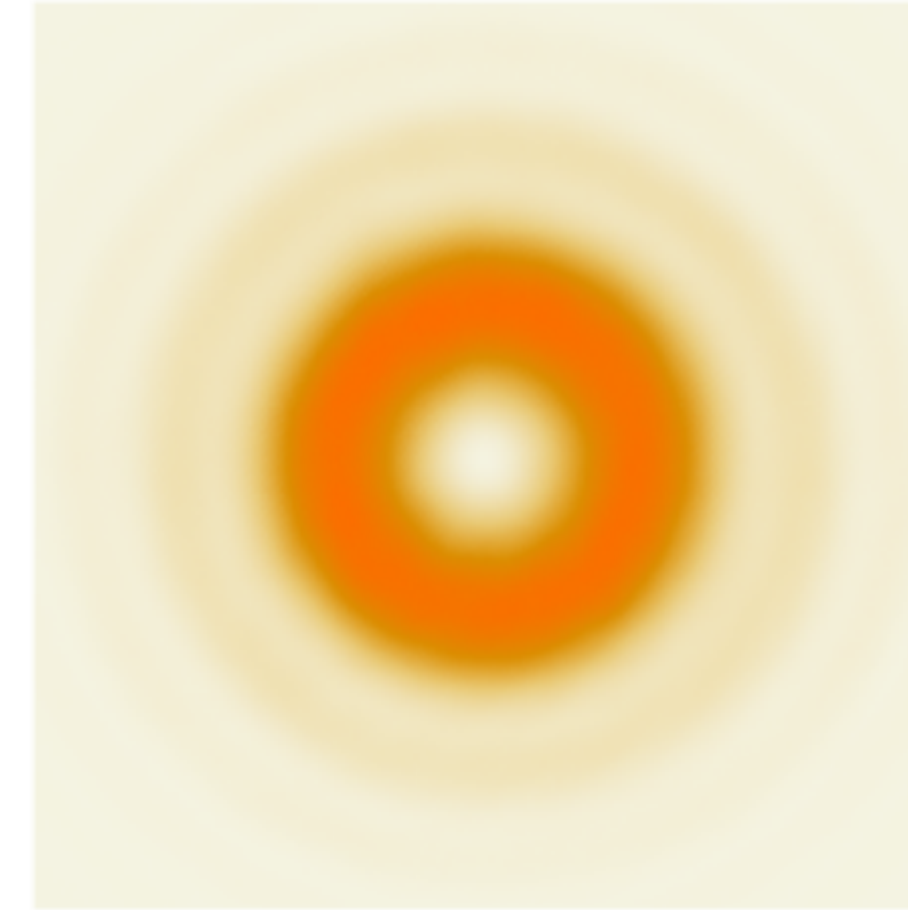


Beam Intensity Profiles
(measured with CCD
before focusing on the ion)

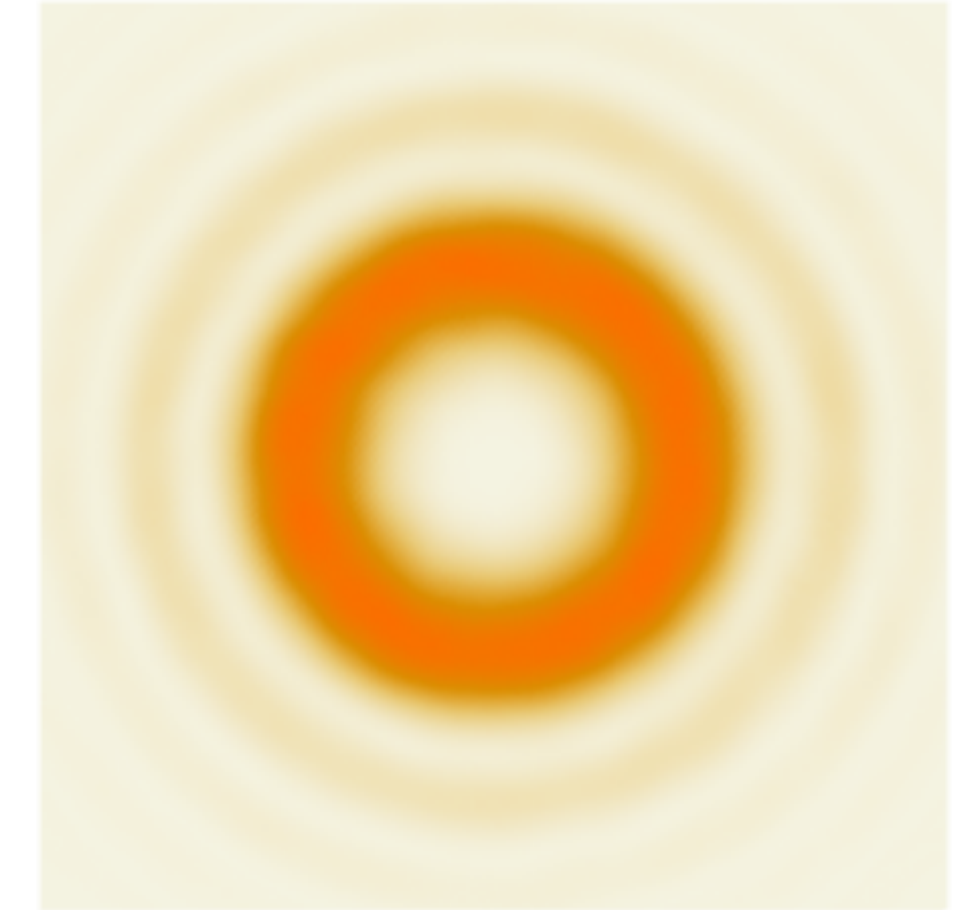
Gaussian Beam $l=0$



Doughnut Beam $l=1$



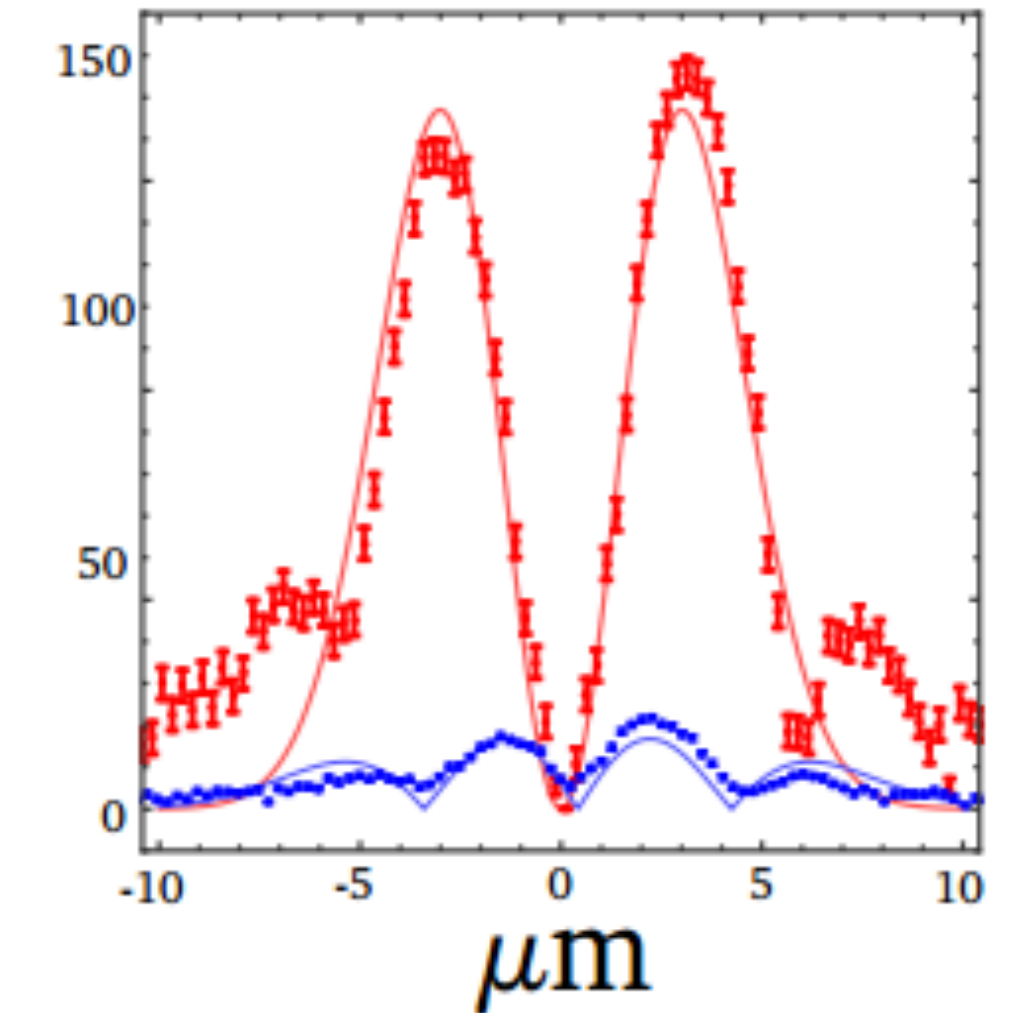
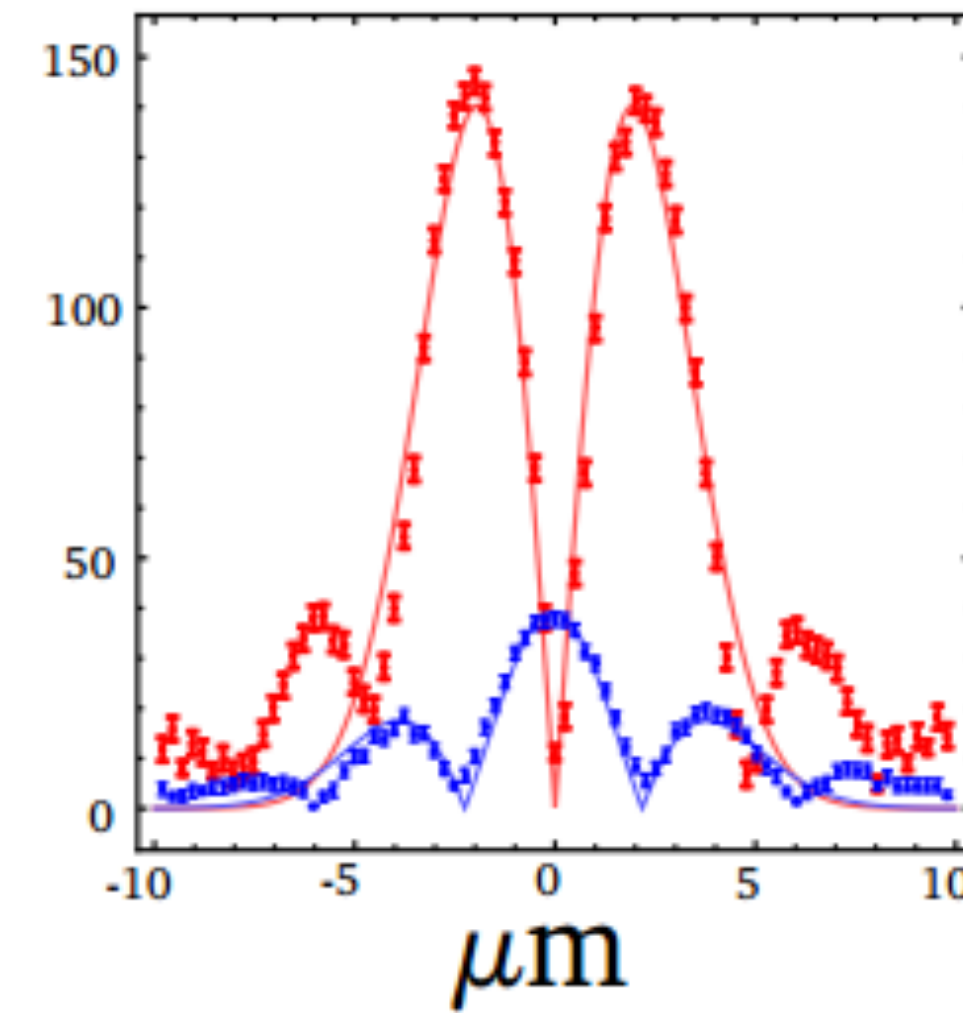
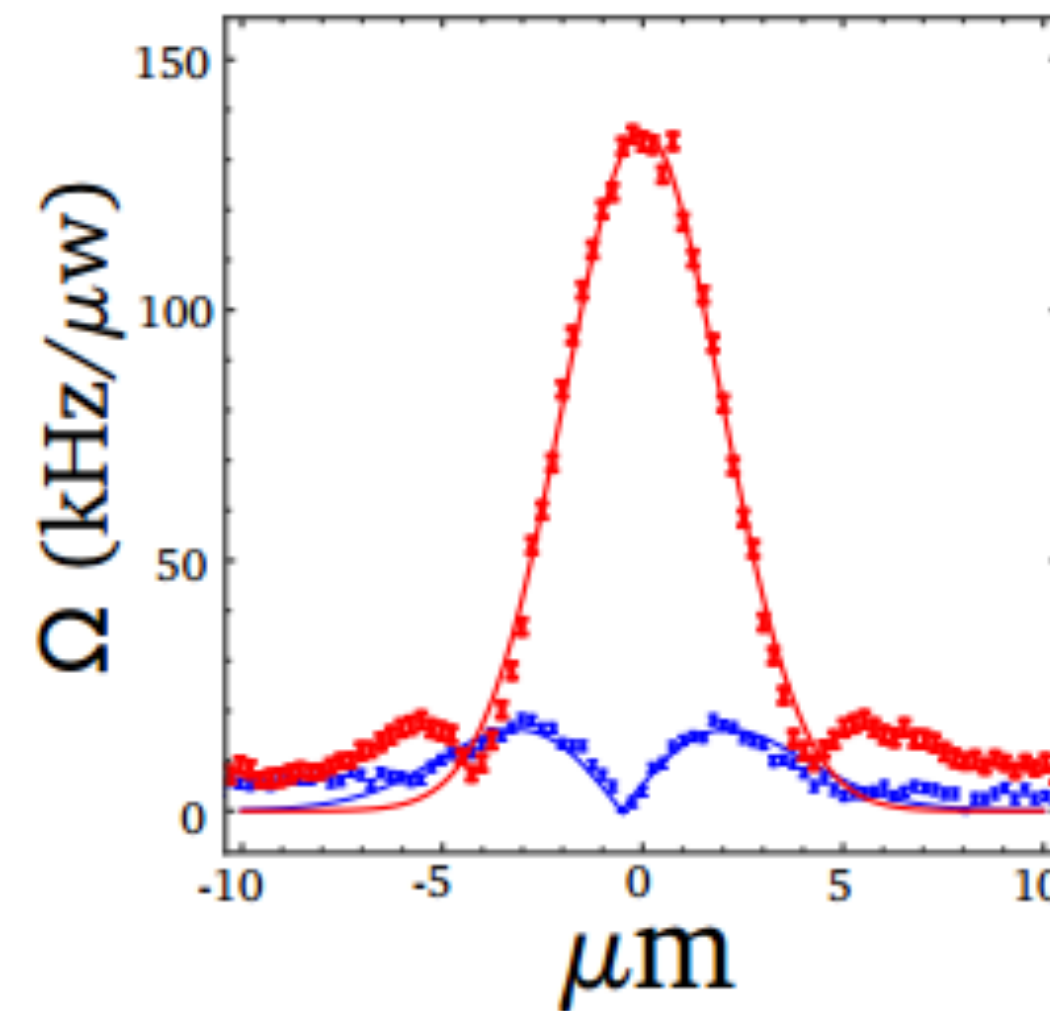
Ring Beam $l=2$



Quadrupole Excitation
as a function of the
position of the ion
in the beam

Longitudinal Gradient
proportional to $\sqrt{\text{intensity}}$

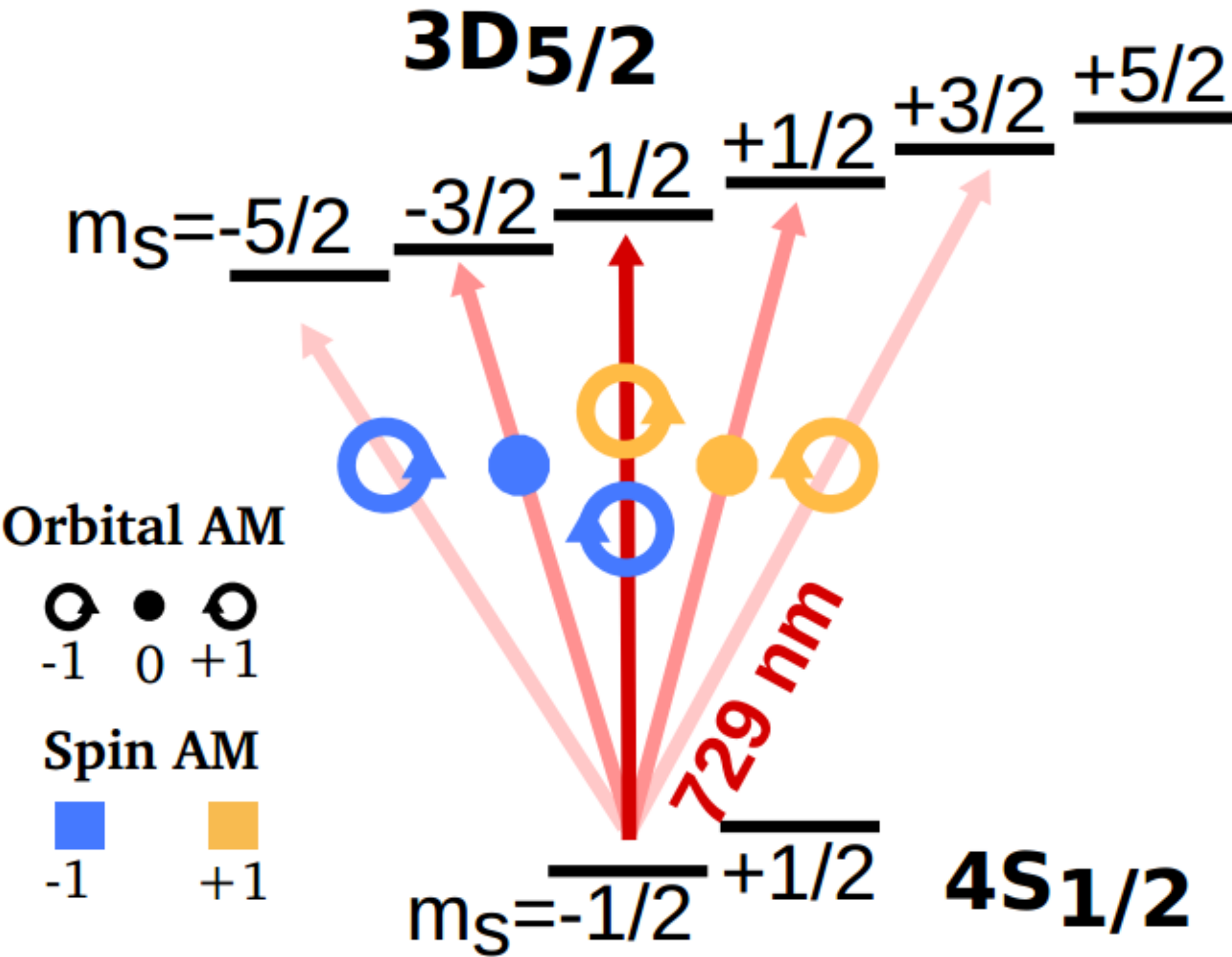
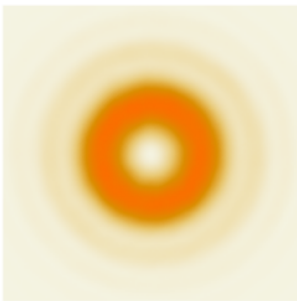
Transverse Gradient



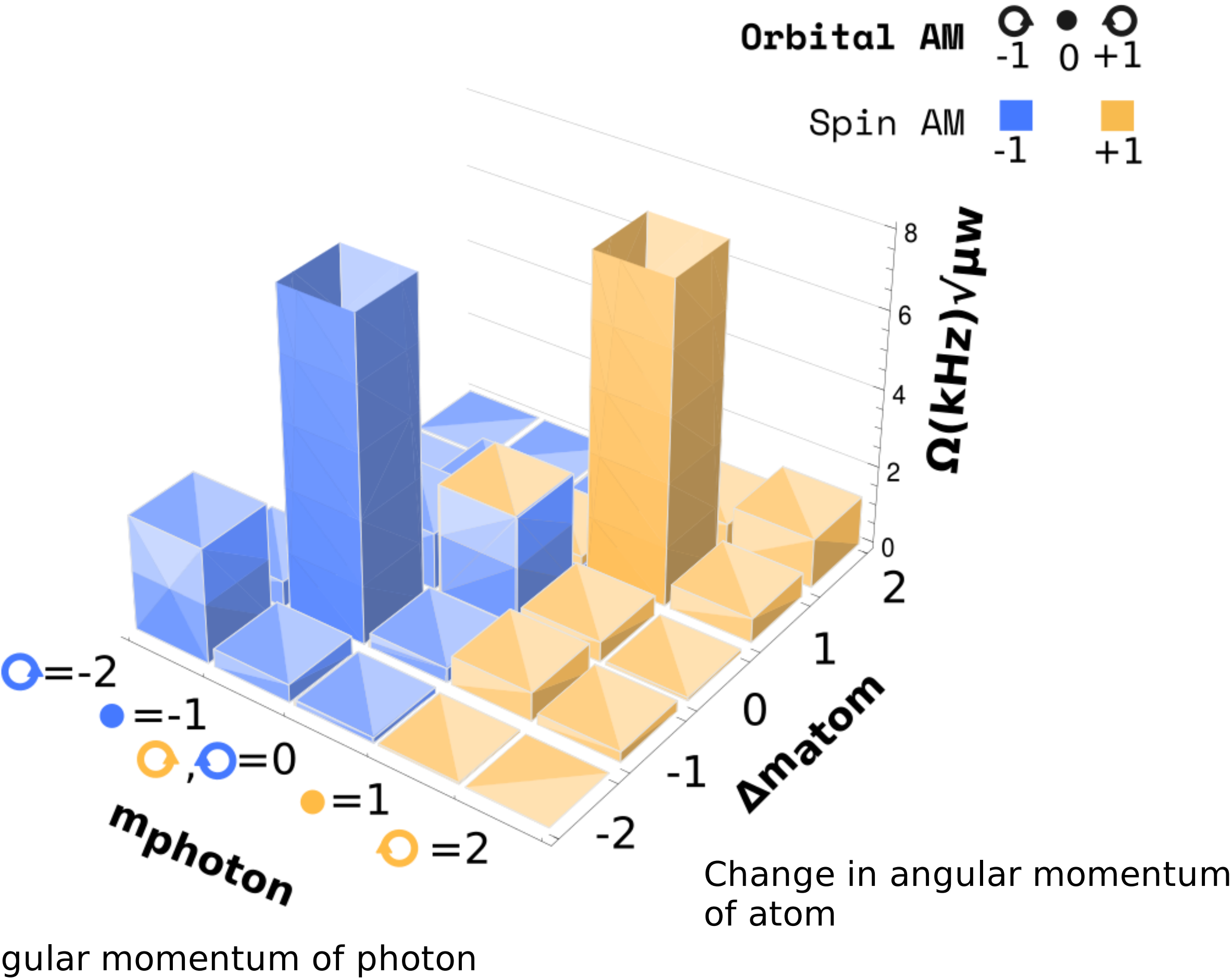
Twisting in the dark selection rules, for a rotationally symmetric system B||k

Nature communications 7, 12998 (2016)

Selection rules for polarization + structure



Rabi frequencies for each transition



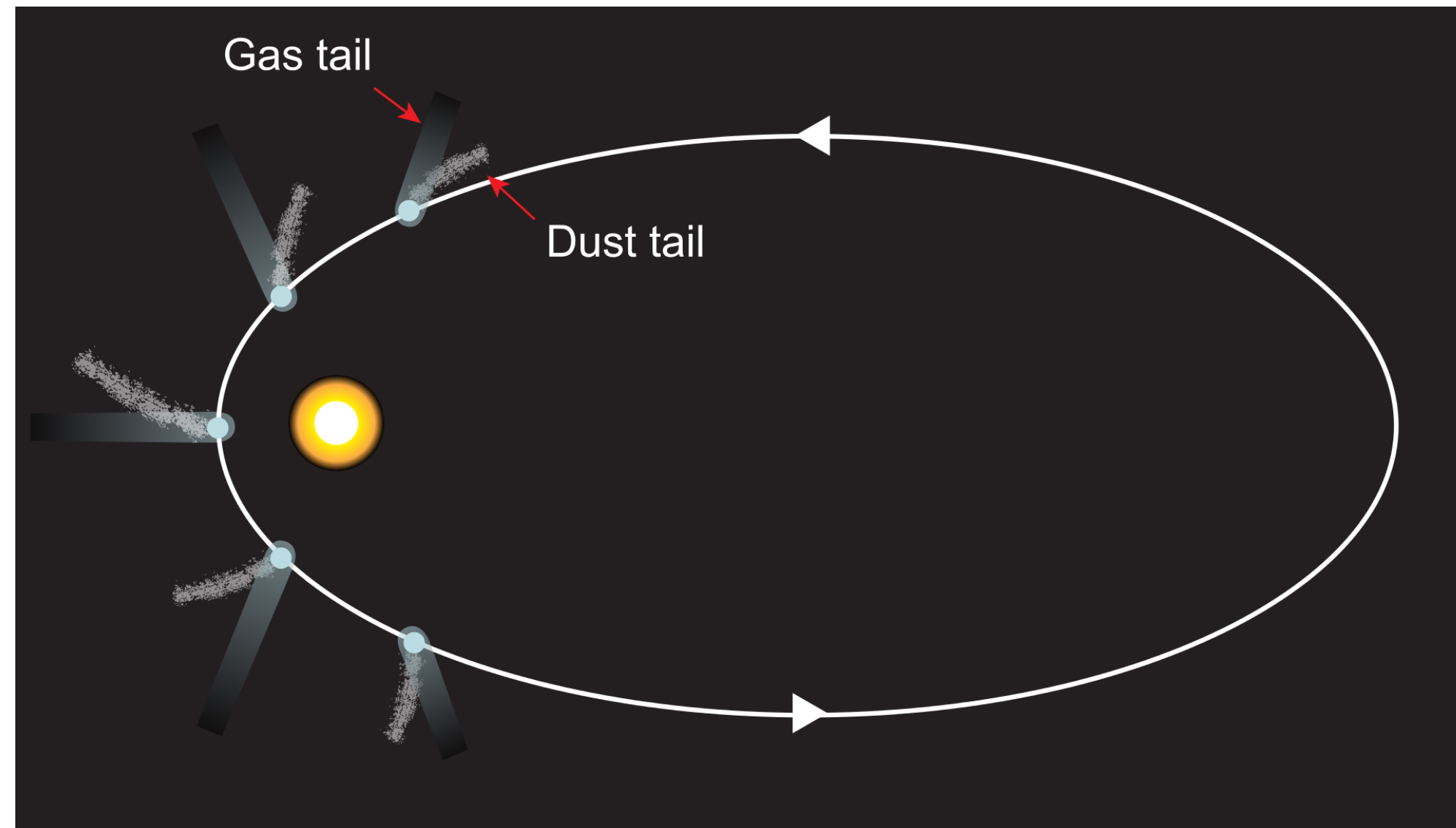
Day Three

Part 1

Center of mass motion with resonant interaction.

Moving in the dark the center of mass, trasnversal radiation pressure

Radiation pressure - comets and Kepler



Pressure is always in the propagation direction
- longitudinal -

wait!!

momentum transfer is the direction of the field gradient

... for plane waves

$$E = E_0 e^{ikz} \longrightarrow \Delta p = \hbar k \hat{z}$$

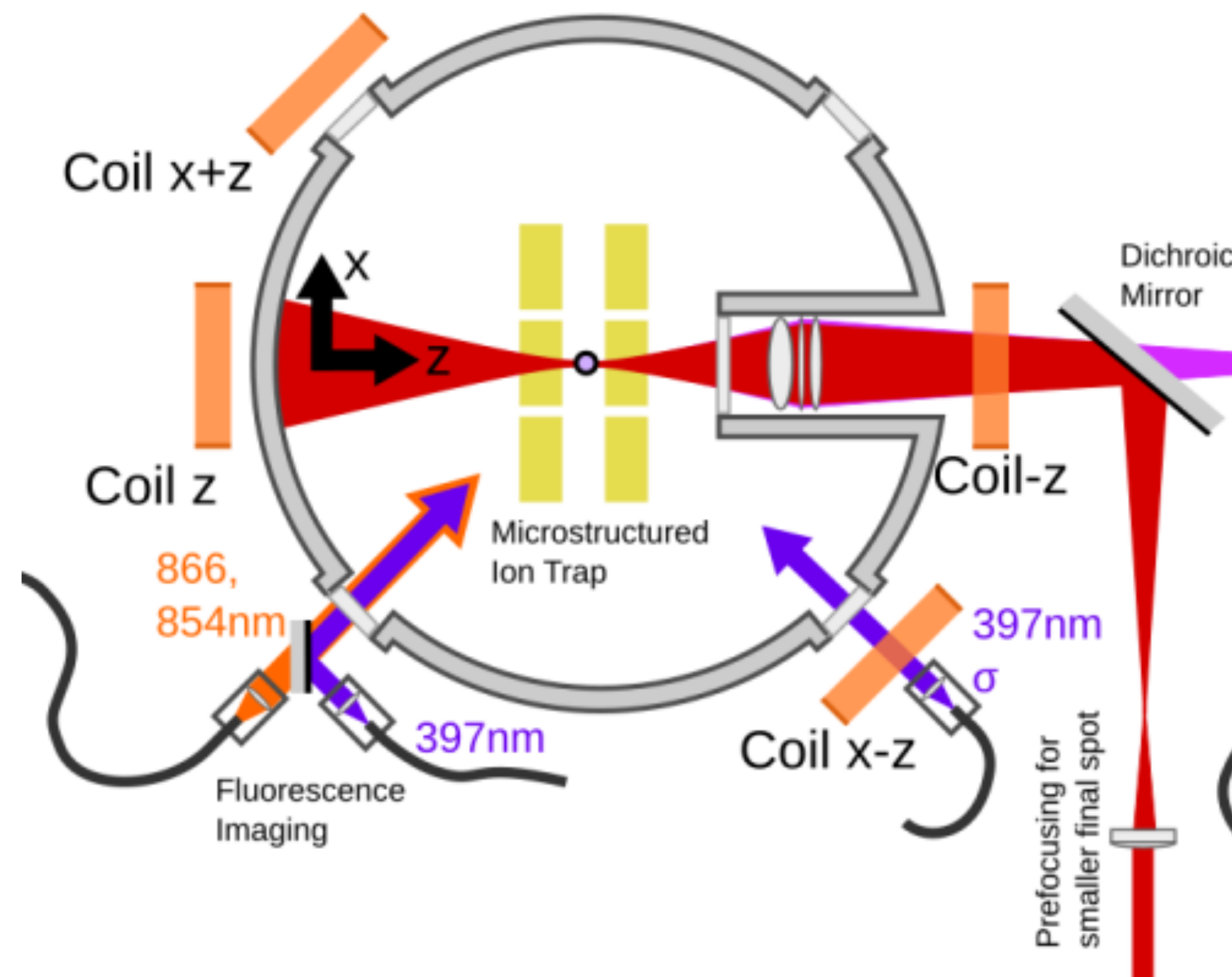
longitudinal momentum transfer

... but for structured beams

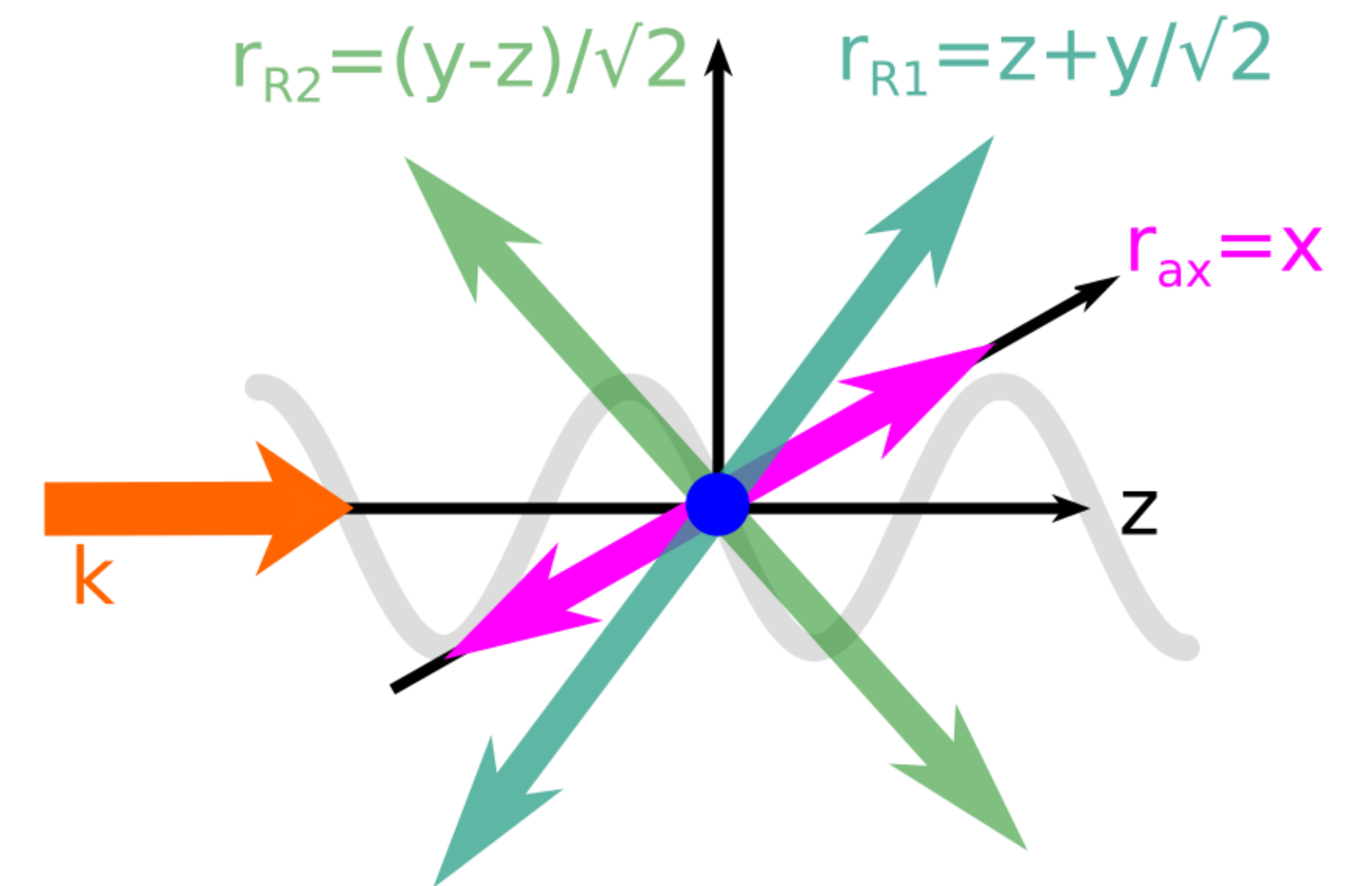
$$E = E_0 e^{ikz} \rho \longrightarrow \Delta p = \hbar \hat{\rho} / w_0$$

trasnverse momentum transfer

Moving in the dark the center of mass, trasnversal radiation pressure



Trap and beam geometry



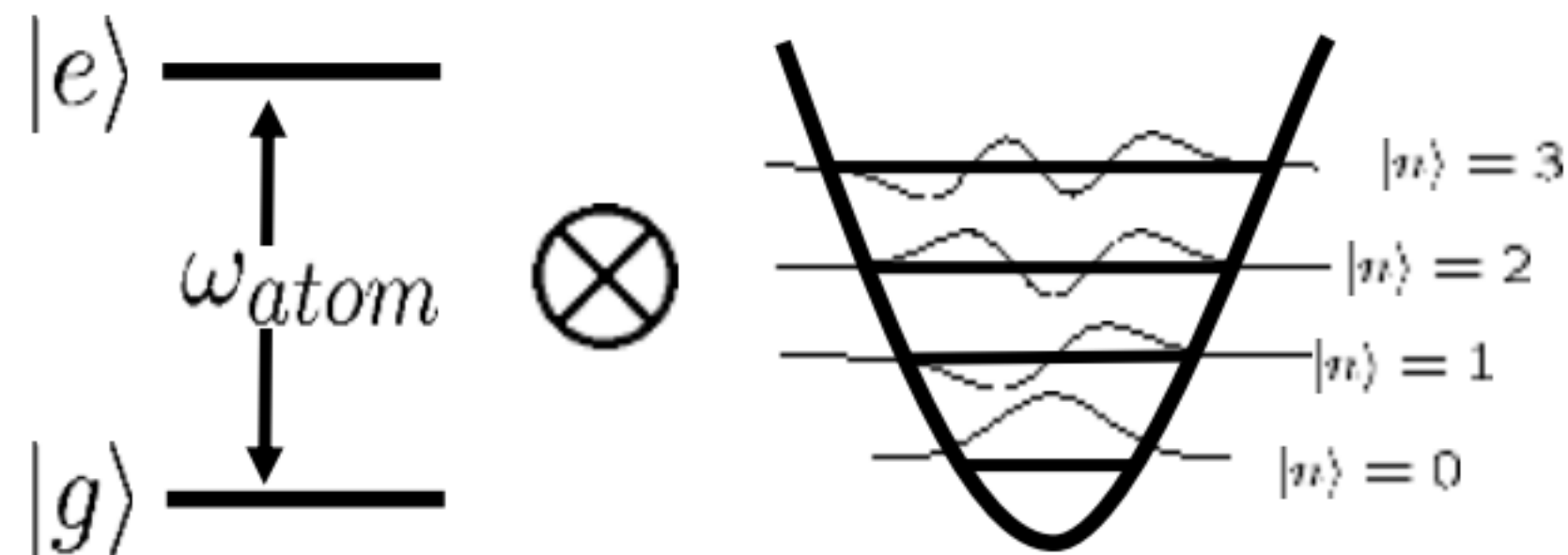
x-axial direction is trasnverse to the beam propagation direction

Moving in the dark trapped atom - light interaction physics

Jaynes-Cummings Hamiltonian

2-level-atom

harmonic trap

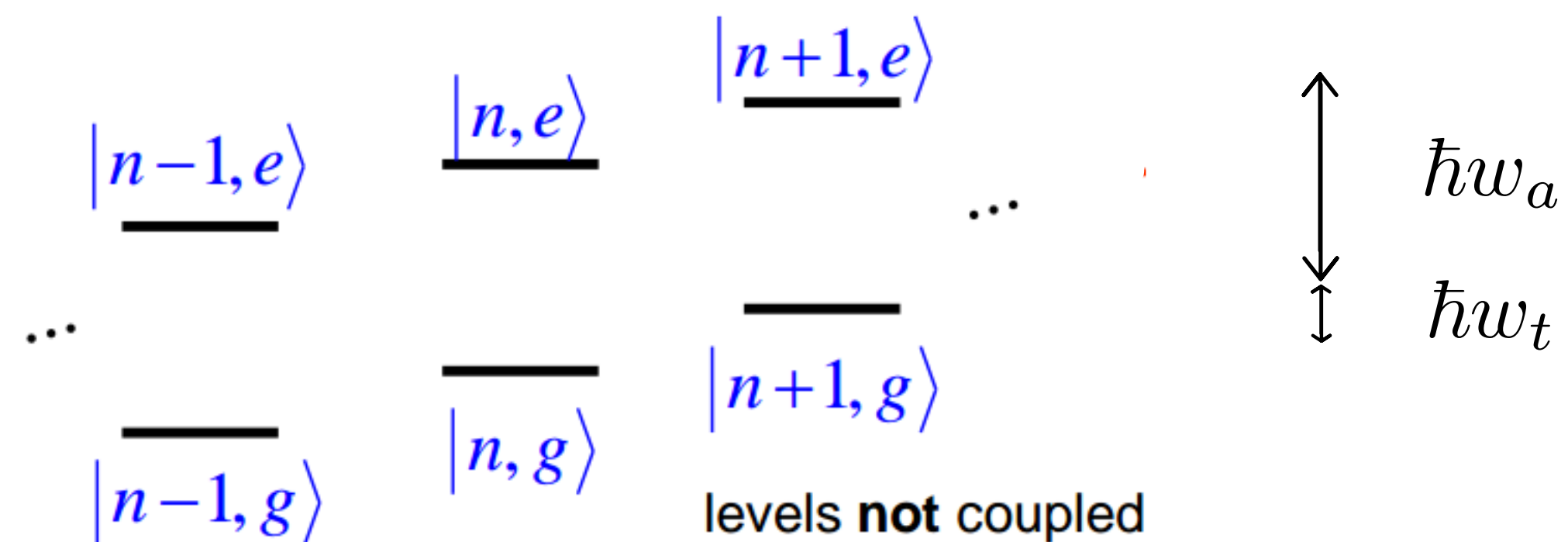


$$H_0 = \frac{1}{2}\omega_a\sigma_z + \frac{p^2}{2m} + \frac{1}{2}m\omega_t^2x^2$$

electronic

center of mass

Ladder representation



Interaction Hamiltonians

for dipole transitions

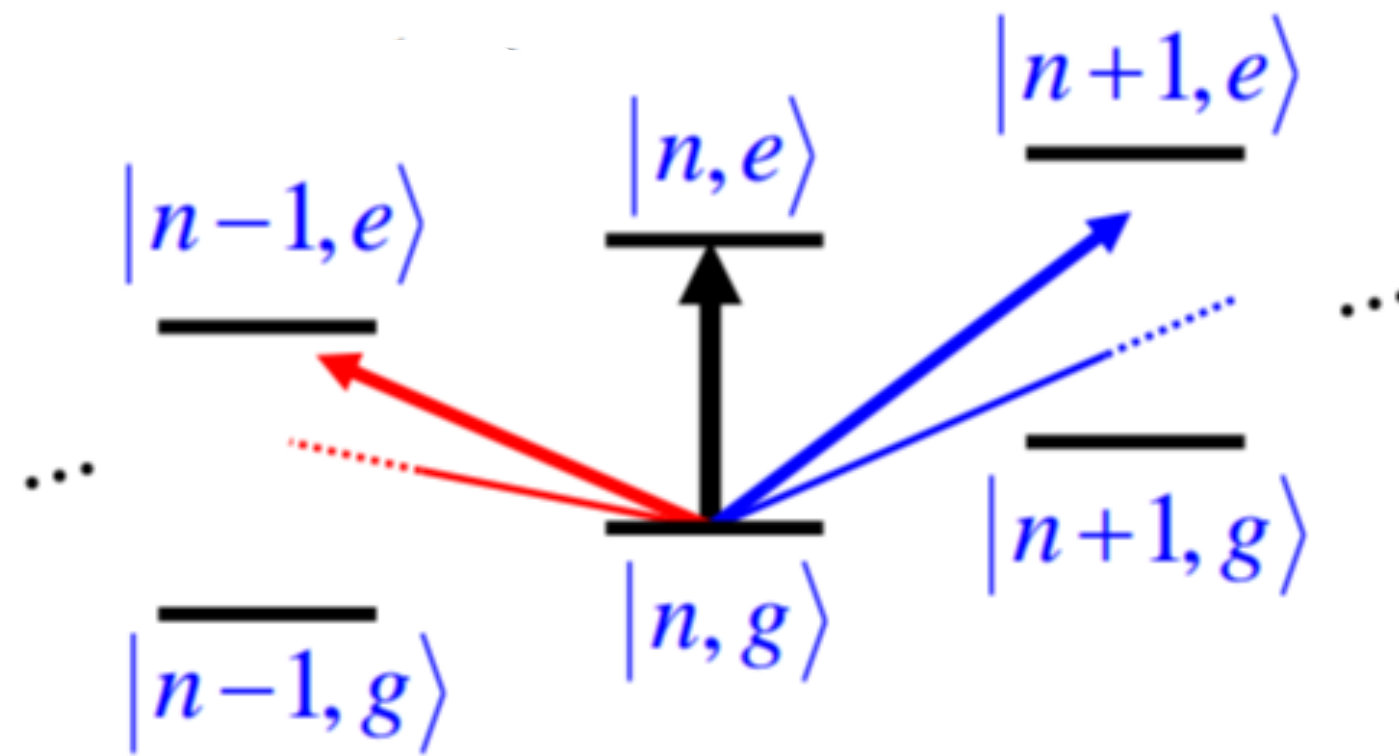
$$H_{ge} = -\vec{d} \cdot \vec{E}$$

for quadrupole transitions

$$H_{ge} = -Q_{ij} \frac{\partial E_i}{\partial x_j}$$

in the dipole case...

$$H_{ge} = \frac{\hbar\Omega}{2} (\sigma^+ + \sigma^-) \sin(kx - \omega t + \phi)$$



after Rotating wave approximation in the interaction picture

$$H_I = \frac{\hbar\Omega}{2} \left(\sigma^+ e^{i\eta(a+a^\dagger)} e^{-i\Delta t} + \sigma^- e^{-i\eta(a+a^\dagger)} e^{i\Delta t} \right)$$

quantum harmonic oscillator

$$x = \sqrt{\frac{\hbar}{2m\omega}} (a + a^\dagger)$$

lamb-Dicke parameter

$$\eta = k \sqrt{\frac{\hbar}{2m\omega}} = 2\pi \frac{x_0}{\lambda}$$

**for trapped ions
in quadrupole or
Raman transitions**

$$\eta \sim 0.05 - 0.2$$

Carrier transitions

order zero

$$H_{\text{carrier}} = \frac{\hbar\Omega}{2} (\sigma^+ + \sigma^-)$$

Red Sideband Transitions

order one

$$H_{\text{red}} = \frac{\hbar\Omega}{2} \eta (\sigma^+ a + \sigma^- a^\dagger)$$

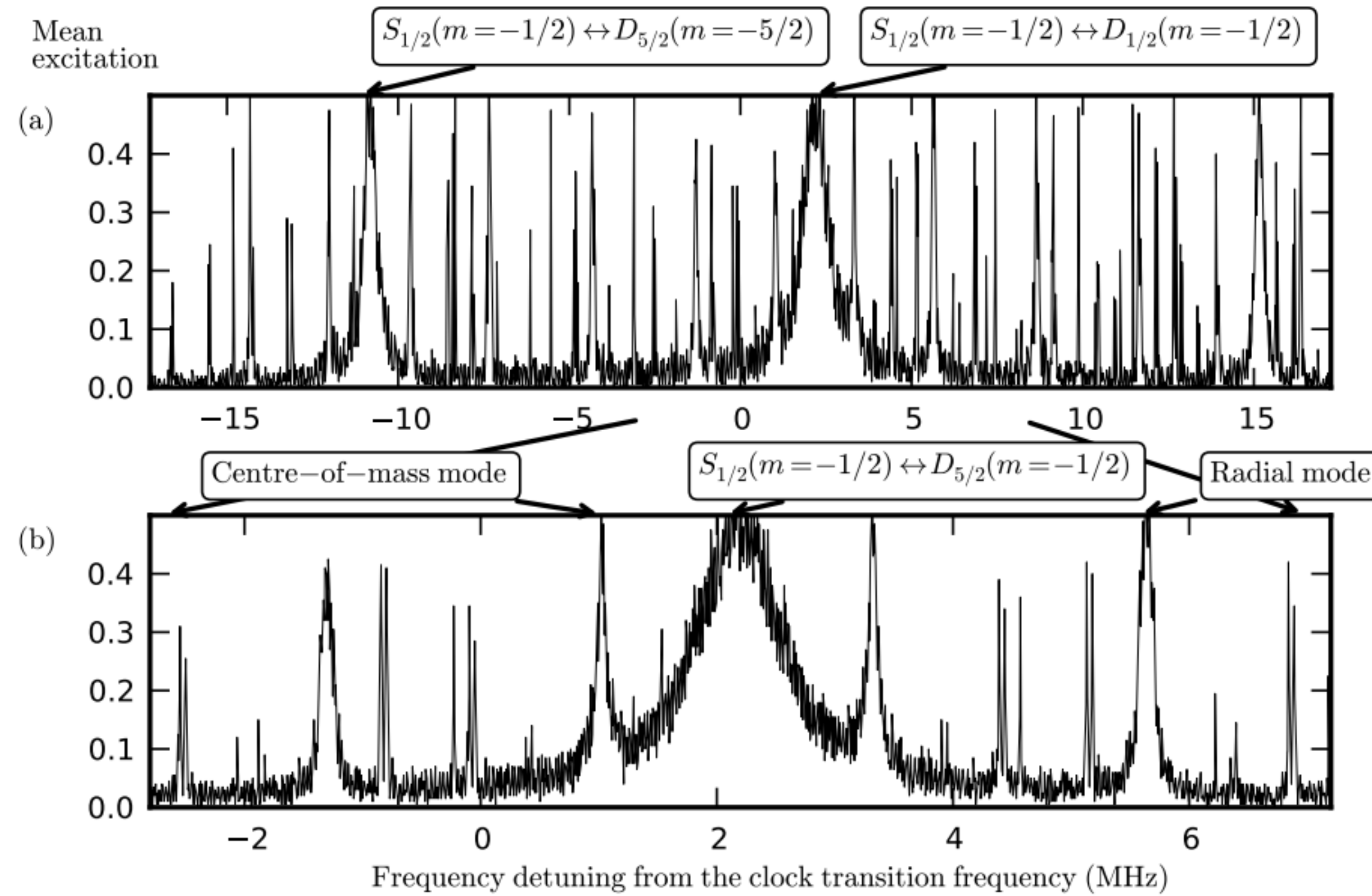
Blue Sideband Transitions

order one

$$H_{\text{blue}} = \frac{\hbar\Omega}{2} \eta (\sigma^+ a^\dagger + \sigma^- a)$$

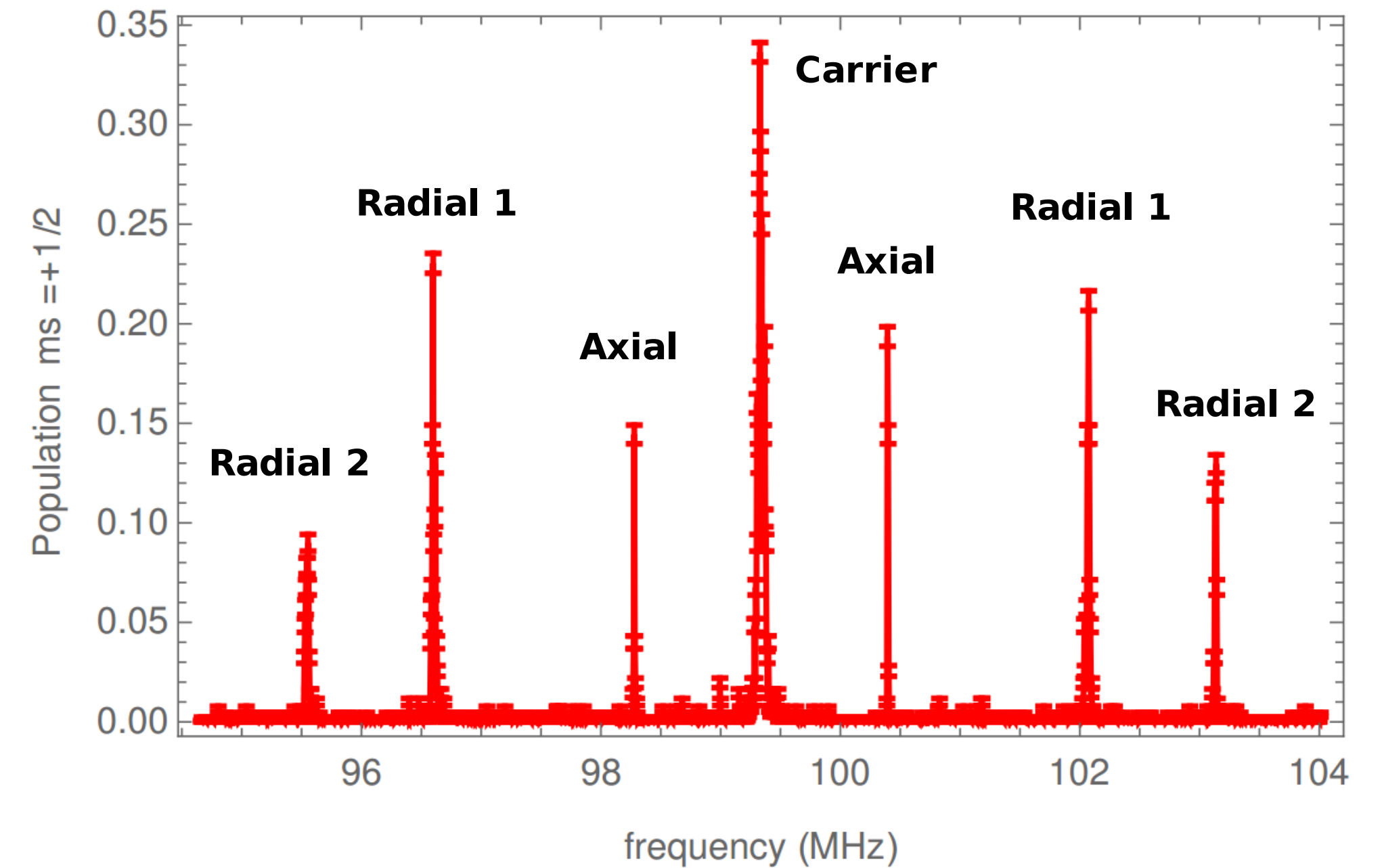
Moving in the dark

Detecting motion via resolved sidebands

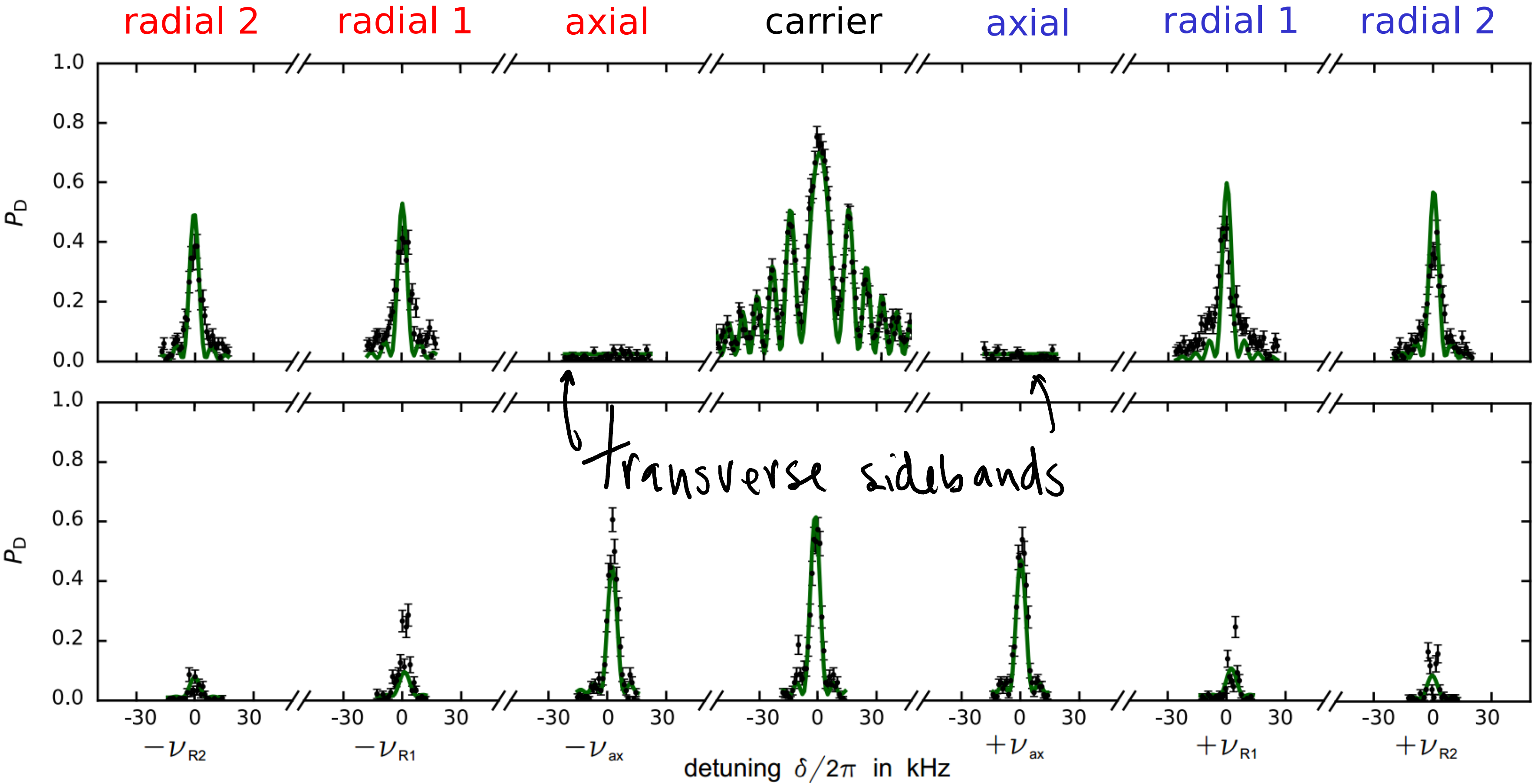
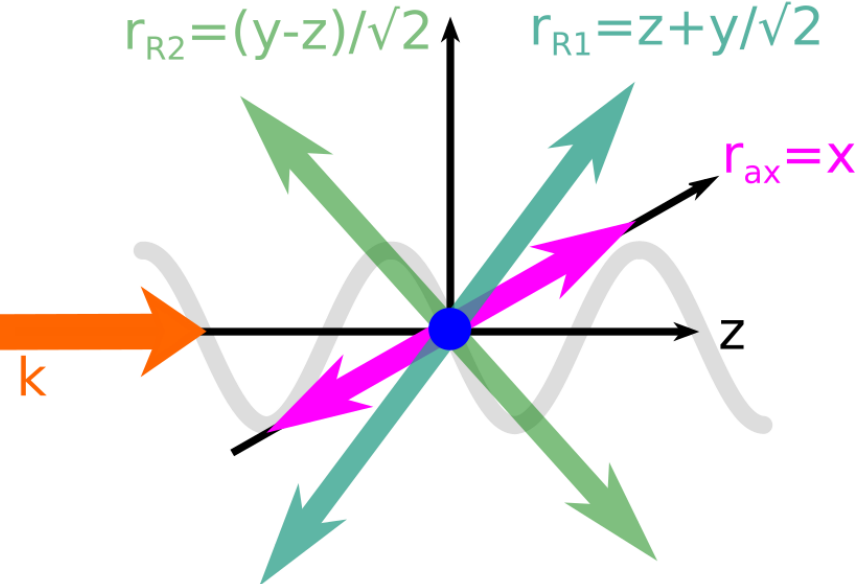


Black spectra borrowed from Monz, PhD Thesis

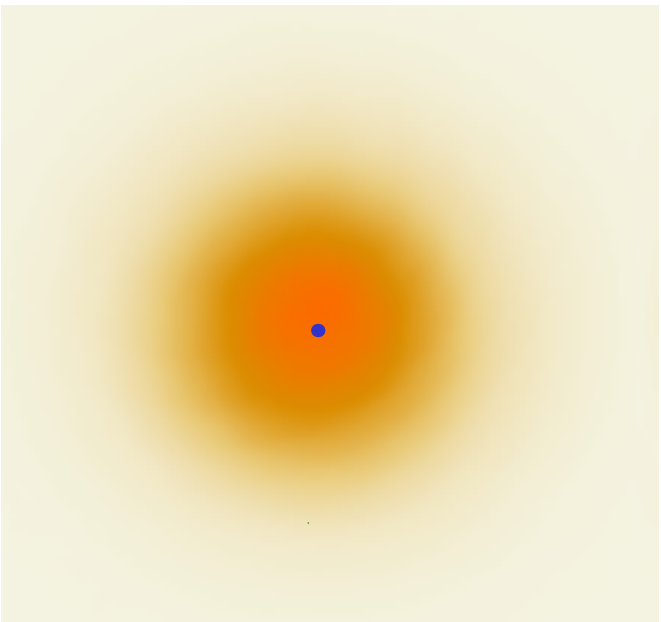
Very clear side-bands in the quadrupole spectrum



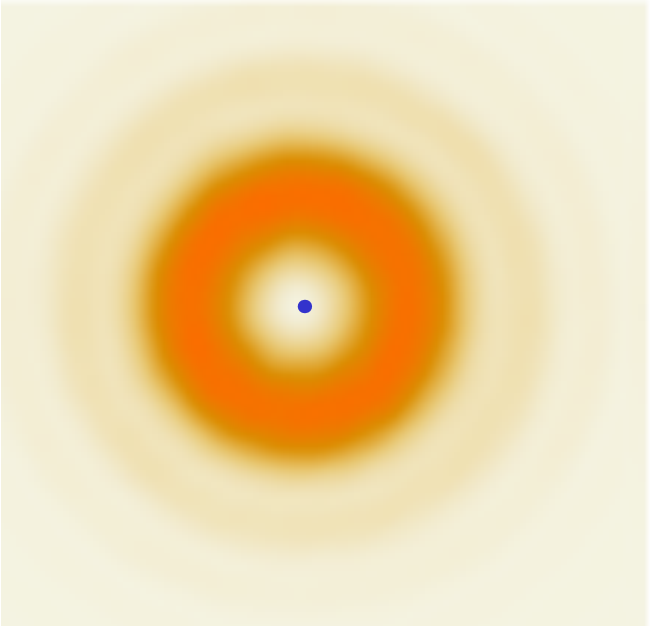
Moving in the dark Spectra: traveling wave vs transverse gradients



Gaussian

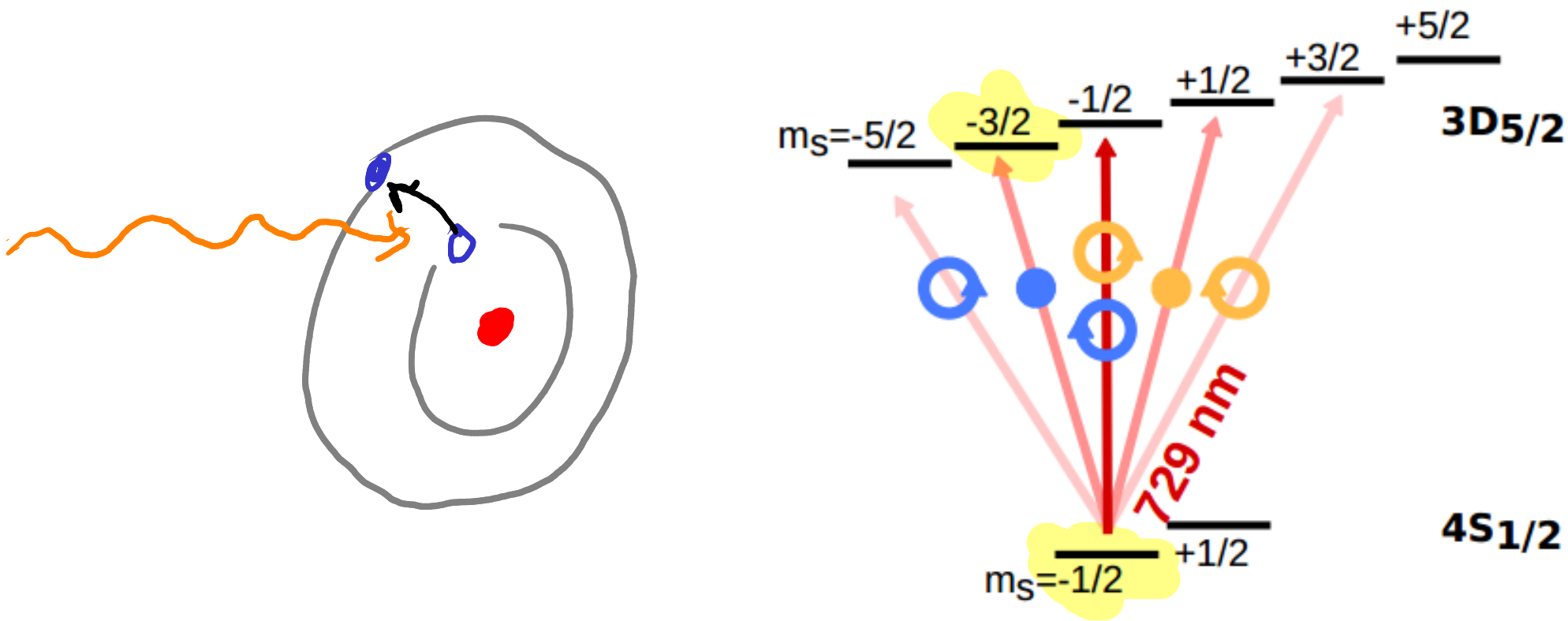


Vortex

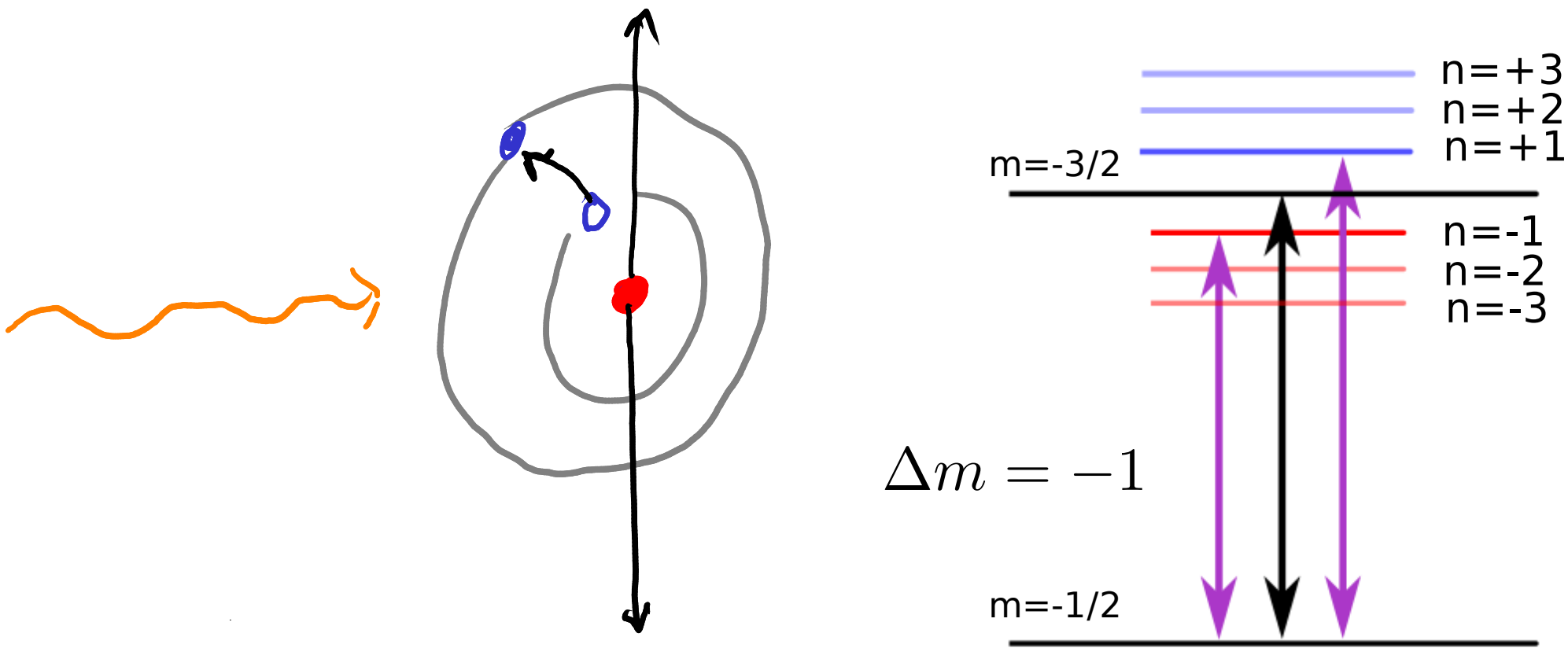


Moving in the dark who does what?

Polarization: change internal in motion



Structure: change in external motion quantized harmonic oscillator



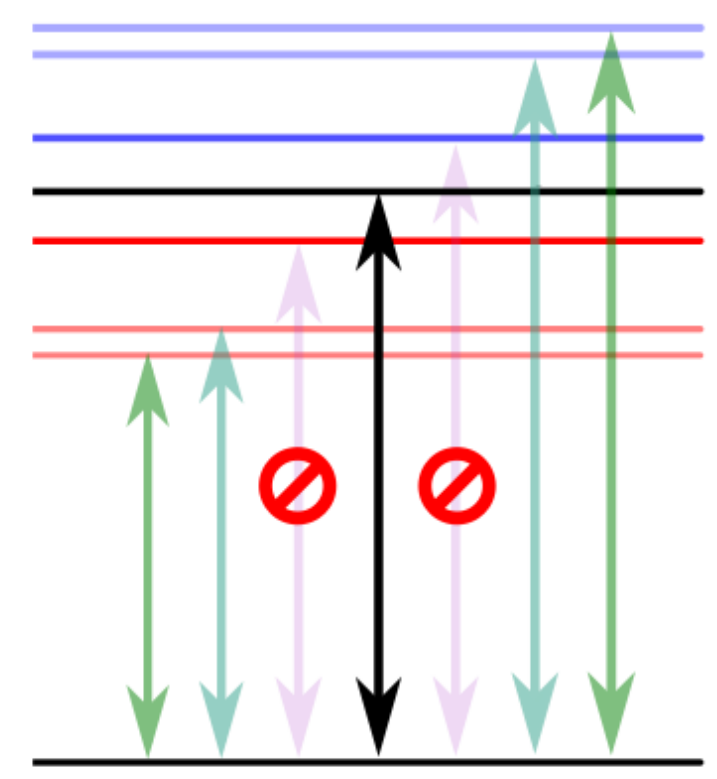
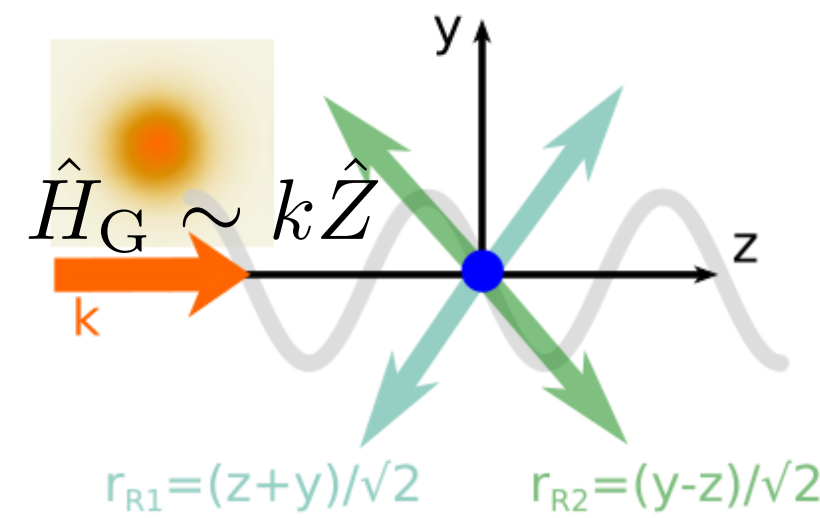
Moving in the dark EXTRA: theory of sidebands on quadrupole transitions

the general interaction term $\hat{H}_Q \sim \sum_{i,j} \hat{q}_i \hat{q}_j \left. \frac{\partial E_j^{(+)}}{\partial q_i} \right|_{\hat{Q}_i} e^{-i\omega t} + \text{h.c.},$

travelling wave term

$$\mathbf{E}_G^{(+)} \sim E_0(\mathbf{e}_x + \sigma i \mathbf{e}_y) \exp(ikz)$$

$$\hat{H}_G \sim k \exp\{ik\hat{Z}\}$$

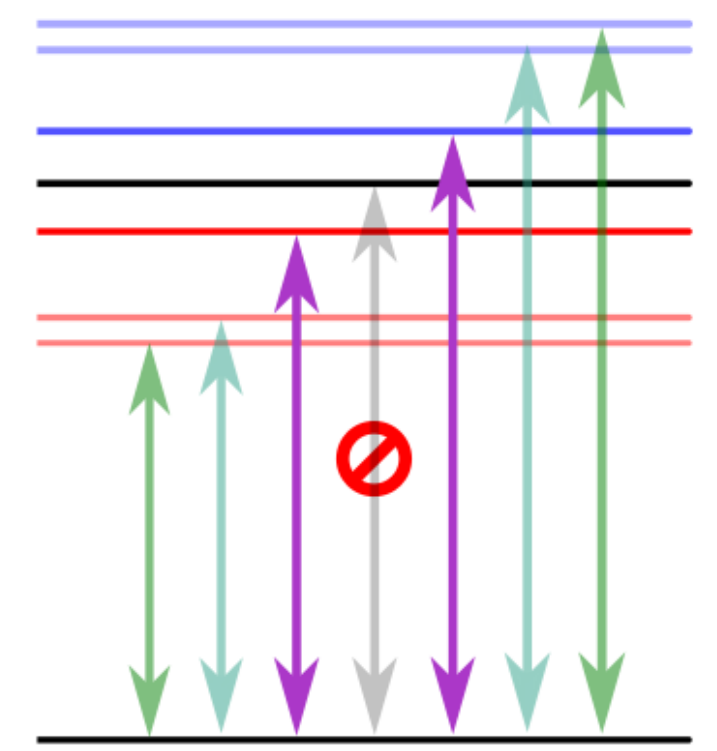
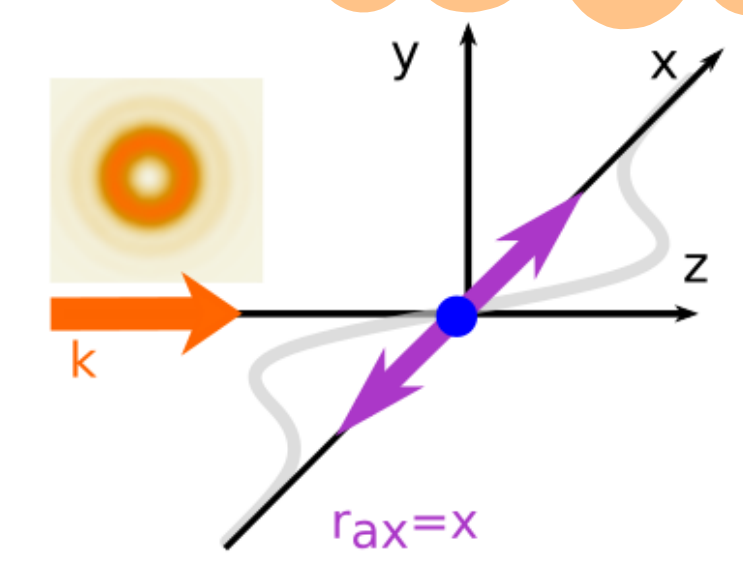


$$\eta_{\parallel} = kx_0$$

oam trasverse term

$$\mathbf{E}_{LG}^{(+)} \sim E_0 \sqrt{2} w_0^{-1} (\mathbf{e}_x + i\sigma \mathbf{e}_y) \exp(ikz)(x + iy)$$

$$\hat{H}_{LG}^{\perp} \sim \exp\{ik\hat{Z}\} \frac{\sqrt{2}}{w_0} (\hat{X} + i\hat{Y})$$

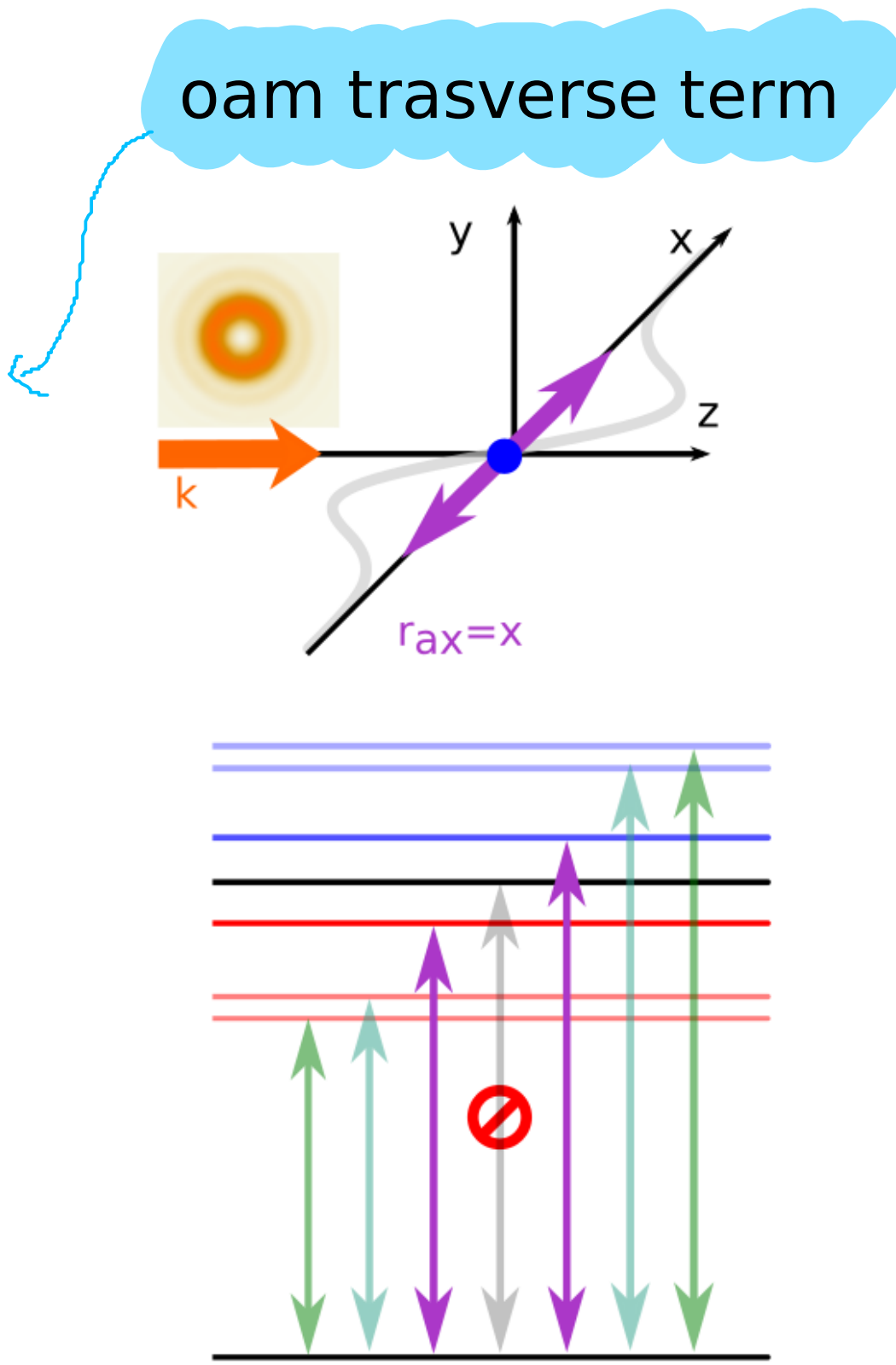
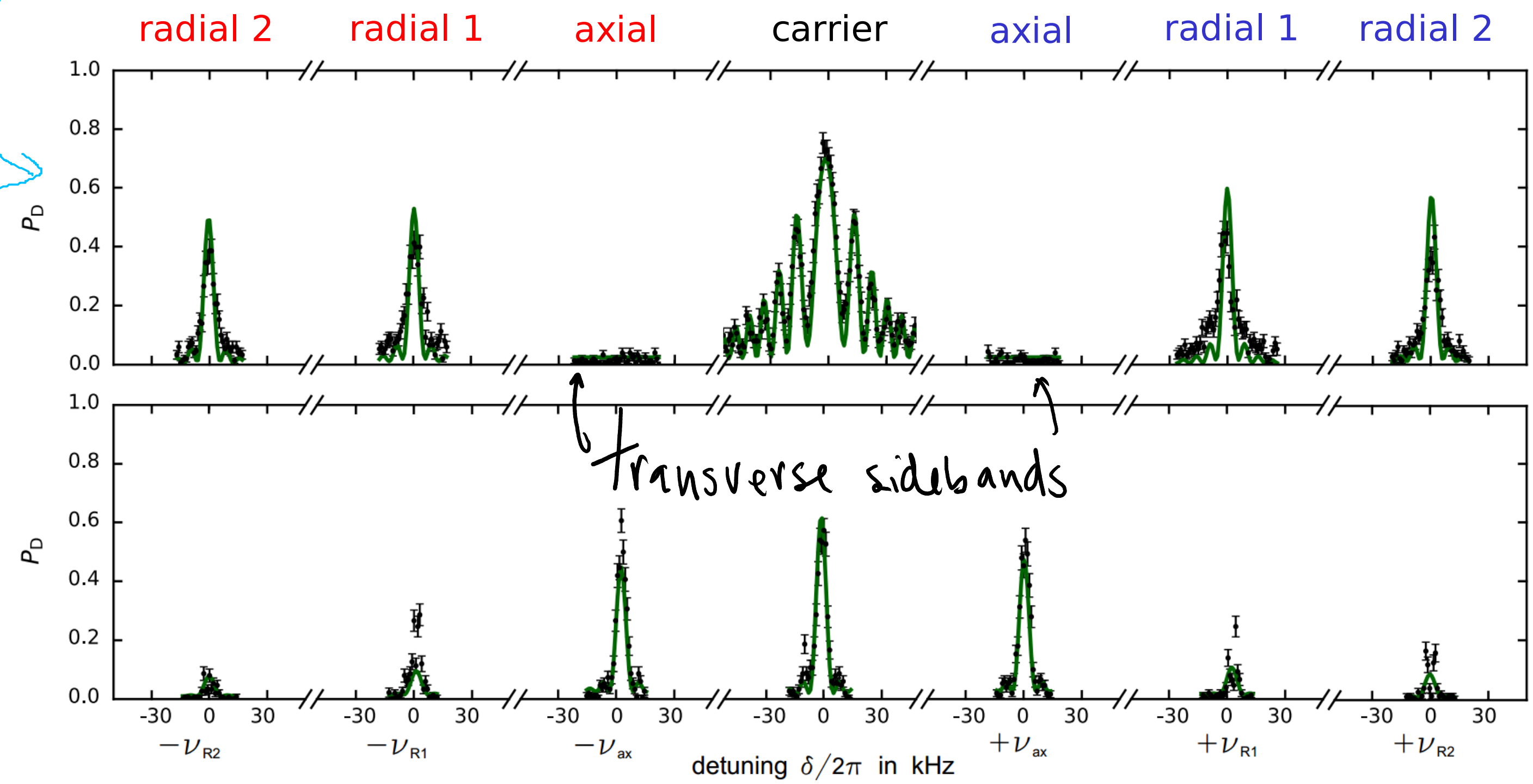
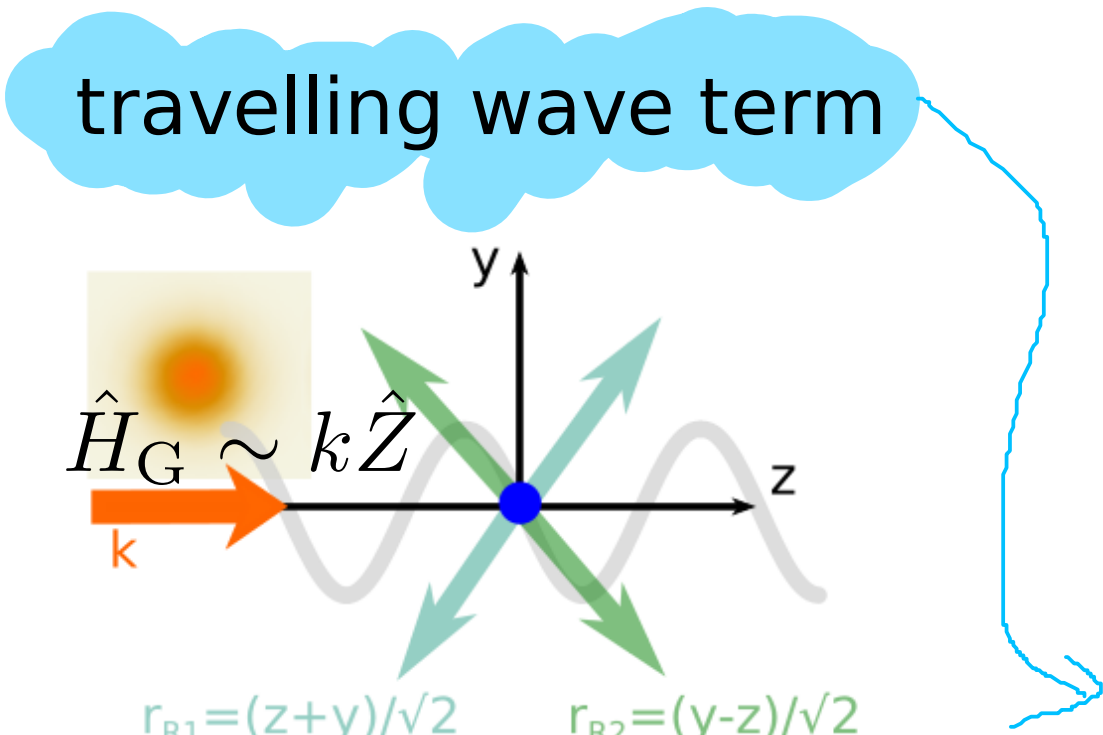


$$\eta_{\perp} = \sqrt{2} x_0 / w_0$$

Lamb-Dicke parameters determine the sideband interaction strengths

Moving in the dark

EXTRA: theory of sidebands on quadrupole transitions



Moving in the dark EXTRA: coherent dynamics

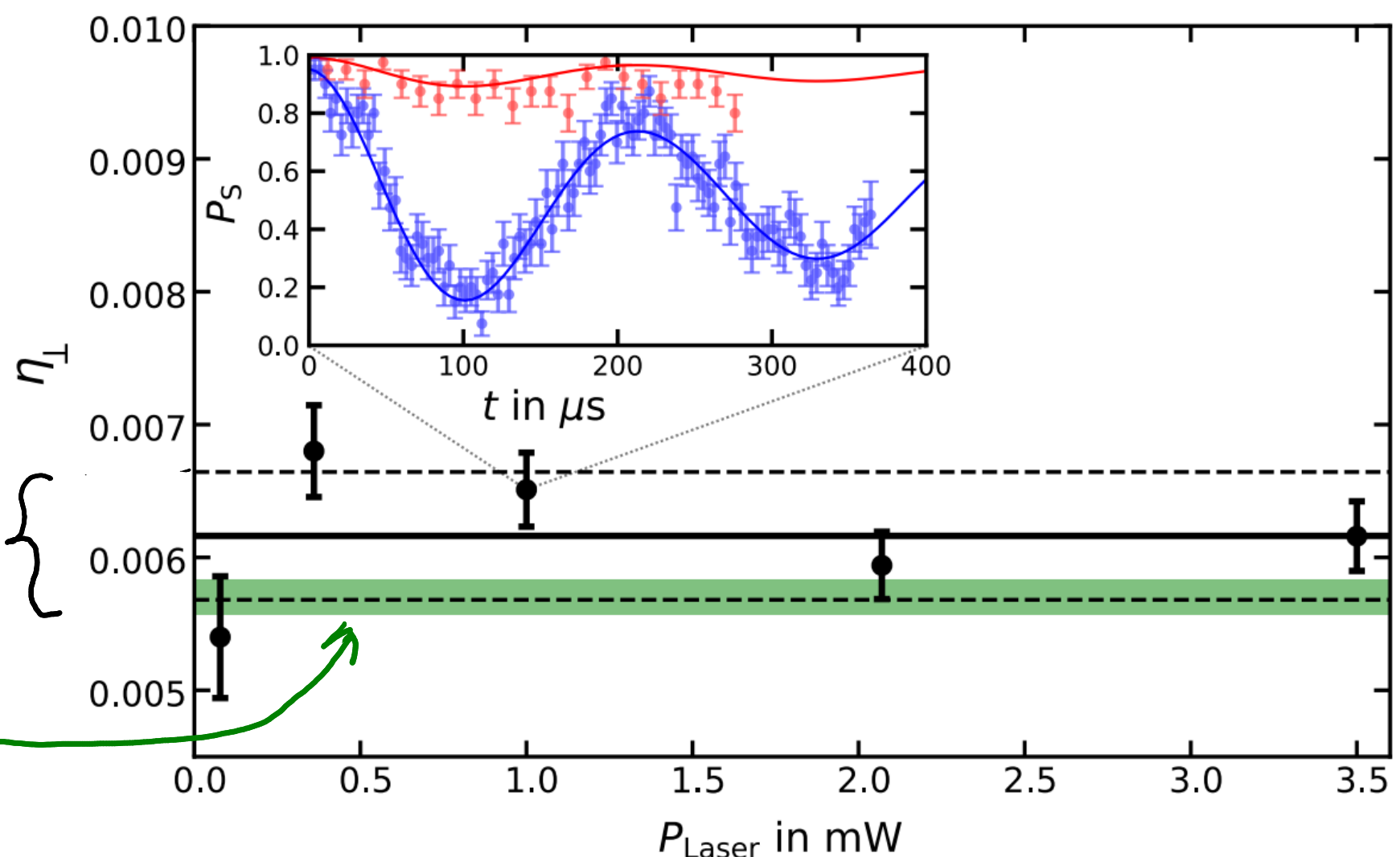
Determination of the transverse Lamb-Dicke parameter

exp: transverse sideband strength
with respect to carrier strength

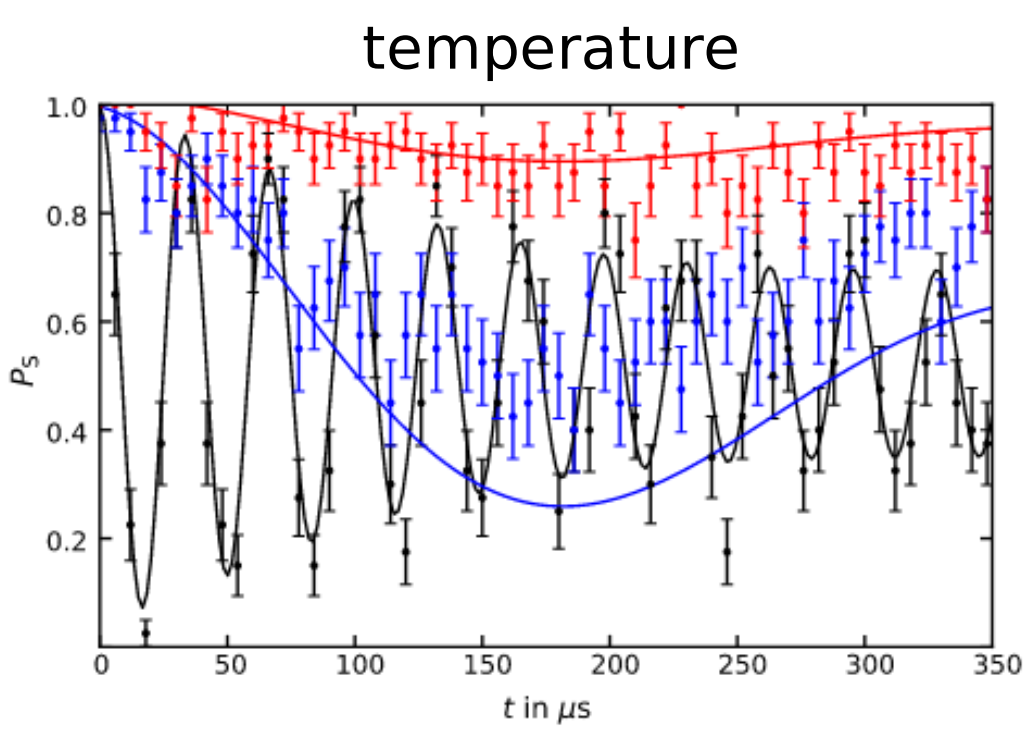
theo: $\eta_{\perp}^{\text{theo}} = \sqrt{2}x_0/w_0$

$\eta_{\perp}^{\text{exp}} = 0.0062(5)$

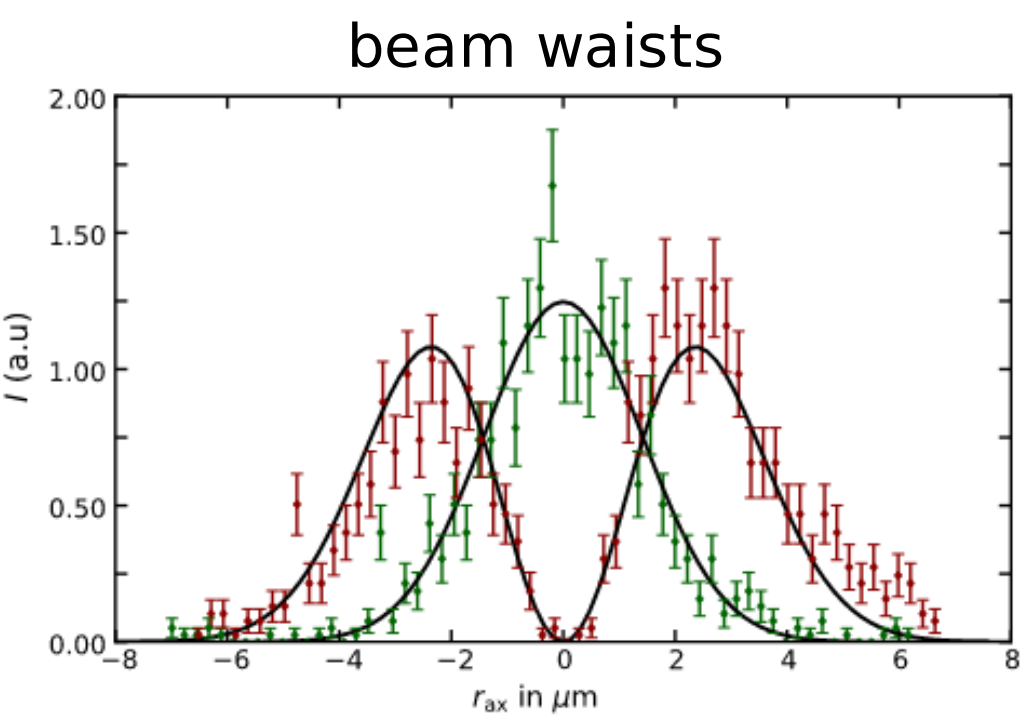
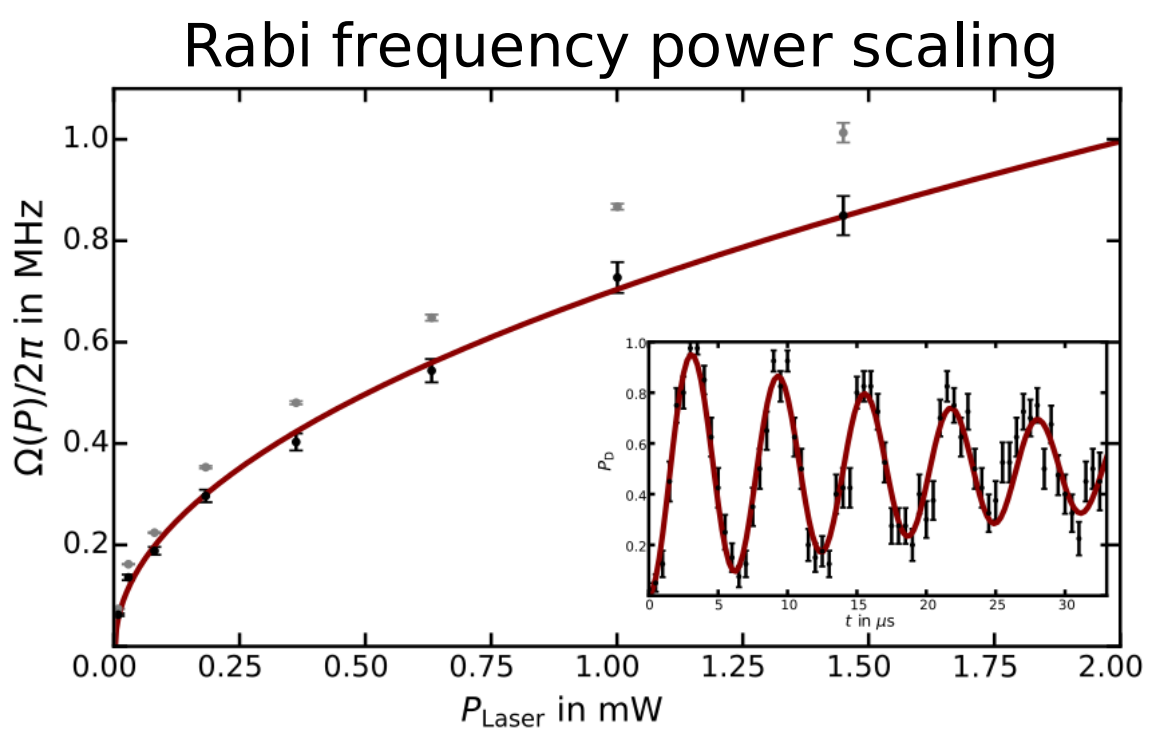
$\eta_{\perp}^{\text{theo}} = 0.0057(1)$



various calibration parameters



$\langle n_{\text{ax}} \rangle = 0.19(10)$



$w_V = 3.34(7) \mu\text{m}$

Outlook

Quadrupole-tuned vortices

Radially addressed axial gates

Thermometry on planar ion crystals

Dipole-tuned vortices

Type of force

Detuned - conservative

Resonant - incoherent

Type of Crystal

two ion rotation

2D shells

Day Three

Part 2 Stark Shift and Optical, spin-dependent, forces

Center of mass motion with resonant interaction.

AC Stark Shift, Autler-Townes effect hamiltonian and time evolution

Hamiltonian

$$\begin{aligned} H &= H_0 + H_{\text{int}} \\ H_0 &= \sigma_z \frac{\hbar \omega_a}{2} \\ &= \frac{\hbar \omega_a}{2} |e\rangle \langle e| - \frac{\hbar \omega_a}{2} |g\rangle \langle g| \\ H_{\text{int}} &= \hbar \Omega \sigma_x \cos(\omega_l t) \end{aligned}$$

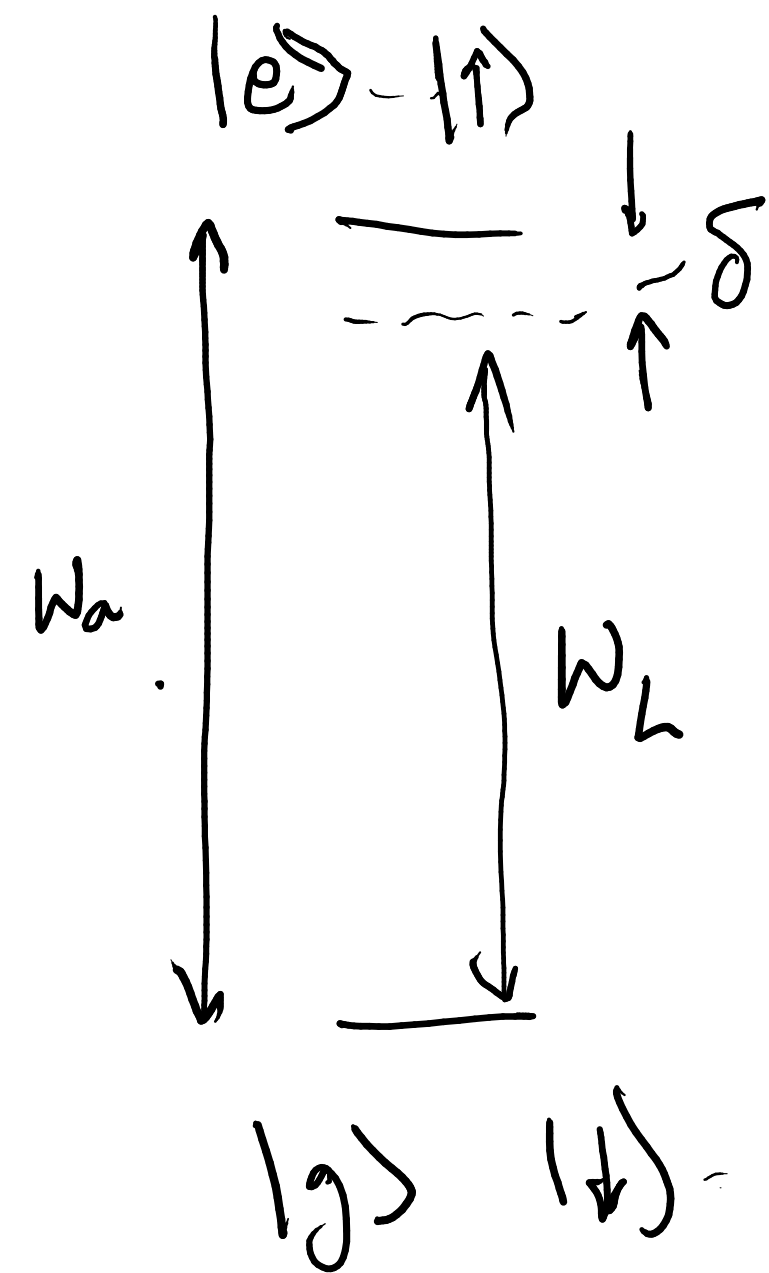
Going to a frame rotating as...

$$U = \exp\{-i\sigma_z(\omega_l - \delta)t/2\}$$

The hamiltonian, tranforms, in the rotating wave approximation to:

$$\begin{aligned} H' &\approx \frac{\hbar \delta}{2} \sigma_z + \hbar \Omega \sigma_x \\ H' &\approx \hbar \Omega' \left(\frac{\delta}{2\Omega'} \sigma_z + \frac{\Omega}{\Omega'} \sigma_x \right) \end{aligned}$$

where $\Omega' = \sqrt{\Omega^2 + \delta^2/4}$



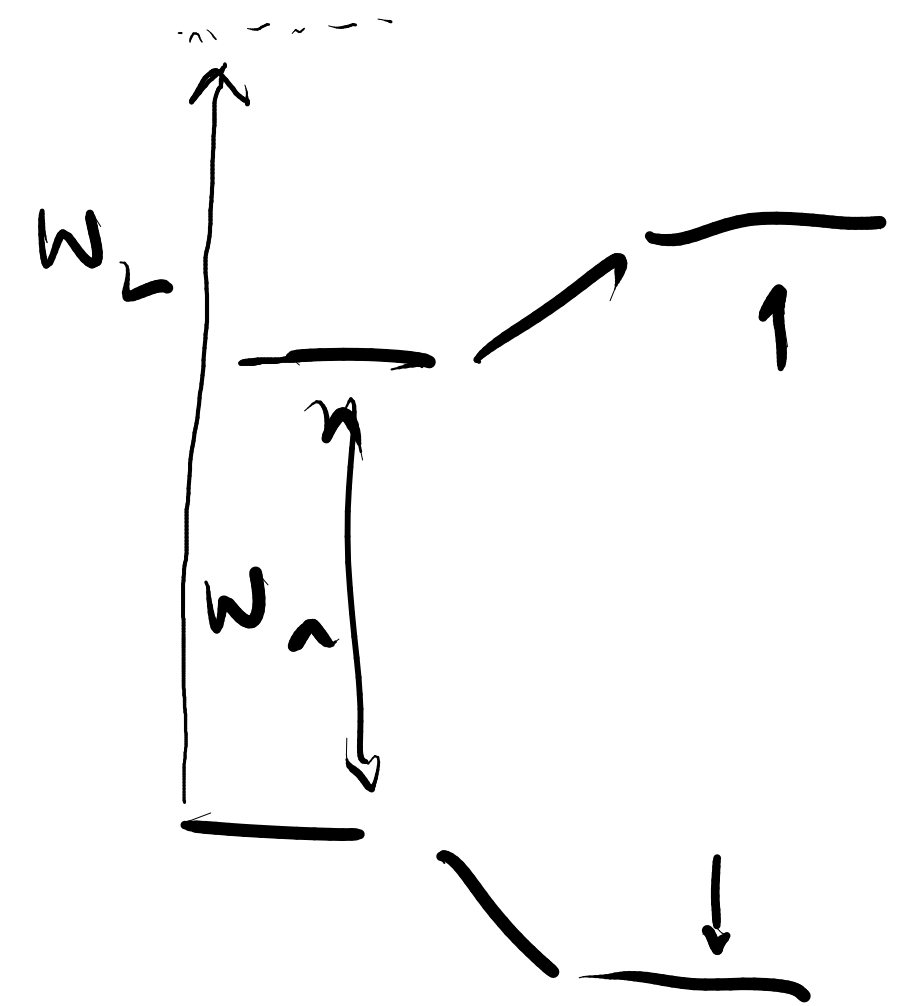
when $\delta \gg \Omega$

$$H' \approx \hbar \Omega' \left(\frac{\delta}{2\Omega'} \sigma_z + \frac{\Omega}{\Omega'} \sigma_x \right)$$

$\Omega' \rightarrow \frac{\delta^2}{2} + \frac{\Omega^2}{\delta}$

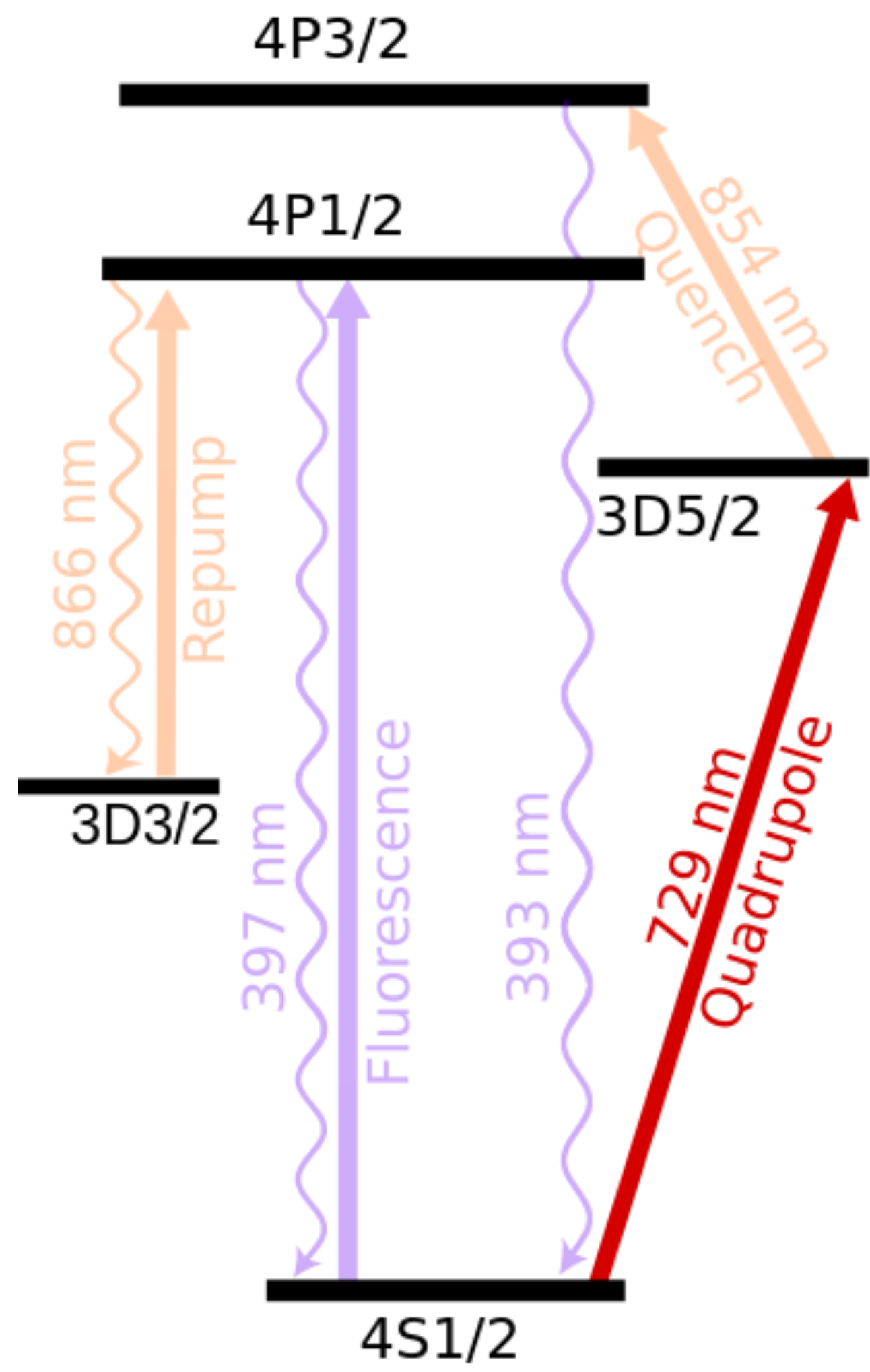
Trasnforming back

$$H = \sigma_z \left(\frac{\hbar \omega_a}{2} + \frac{\Omega^2}{\delta} \right)$$



AC Stark Shift problems and applications

Problems for frequency standards



We demonstrated a reduction in the AC stark shif of ~40x

AC Stark Shift problems and applications

Problems for frequency standards

PHYSICAL REVIEW LETTERS **129**, 253901 (2022)

Excitation of an Electric Octupole Transition by Twisted Light

R. Lange,¹ N. Huntemann^{1,*}, A. A. Peshkov^{1,2}, A. Surzhykov,^{1,2,3} and E. Peik¹

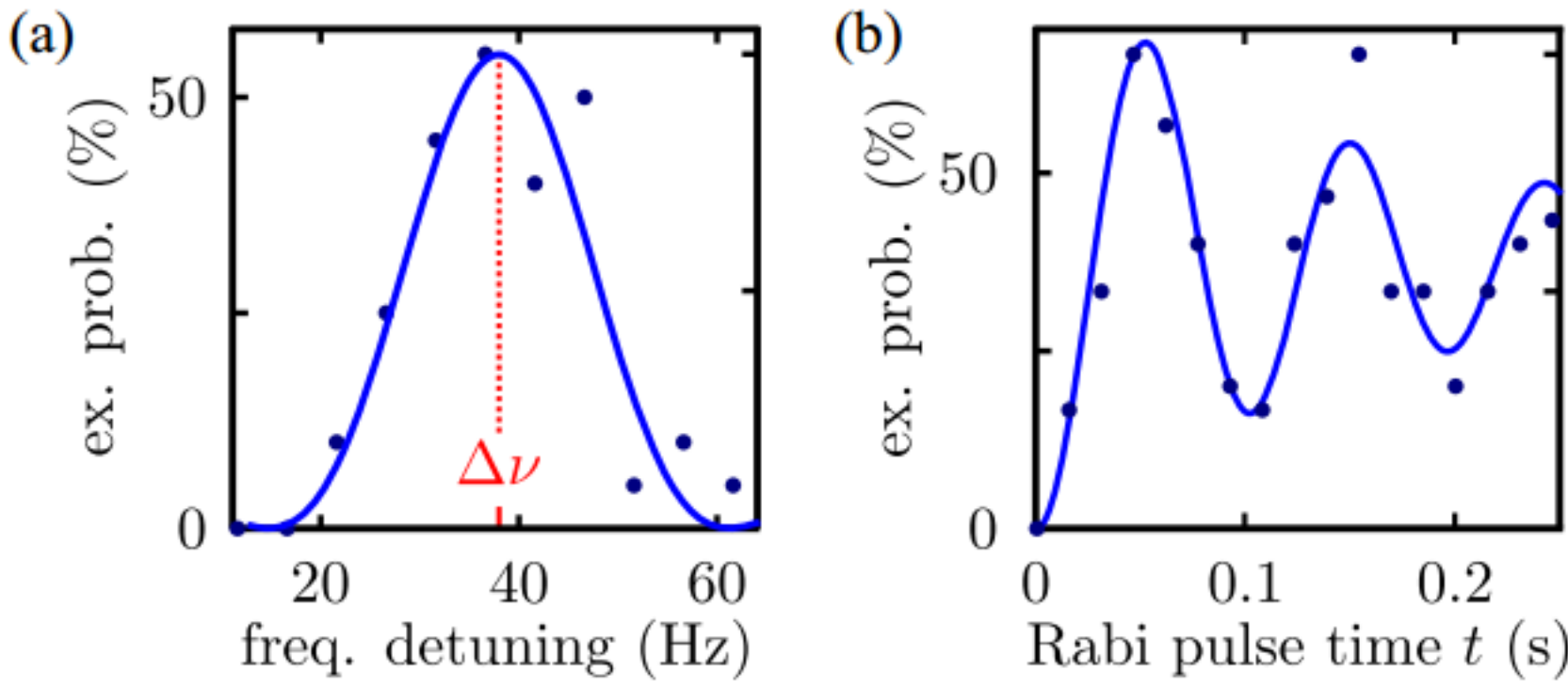
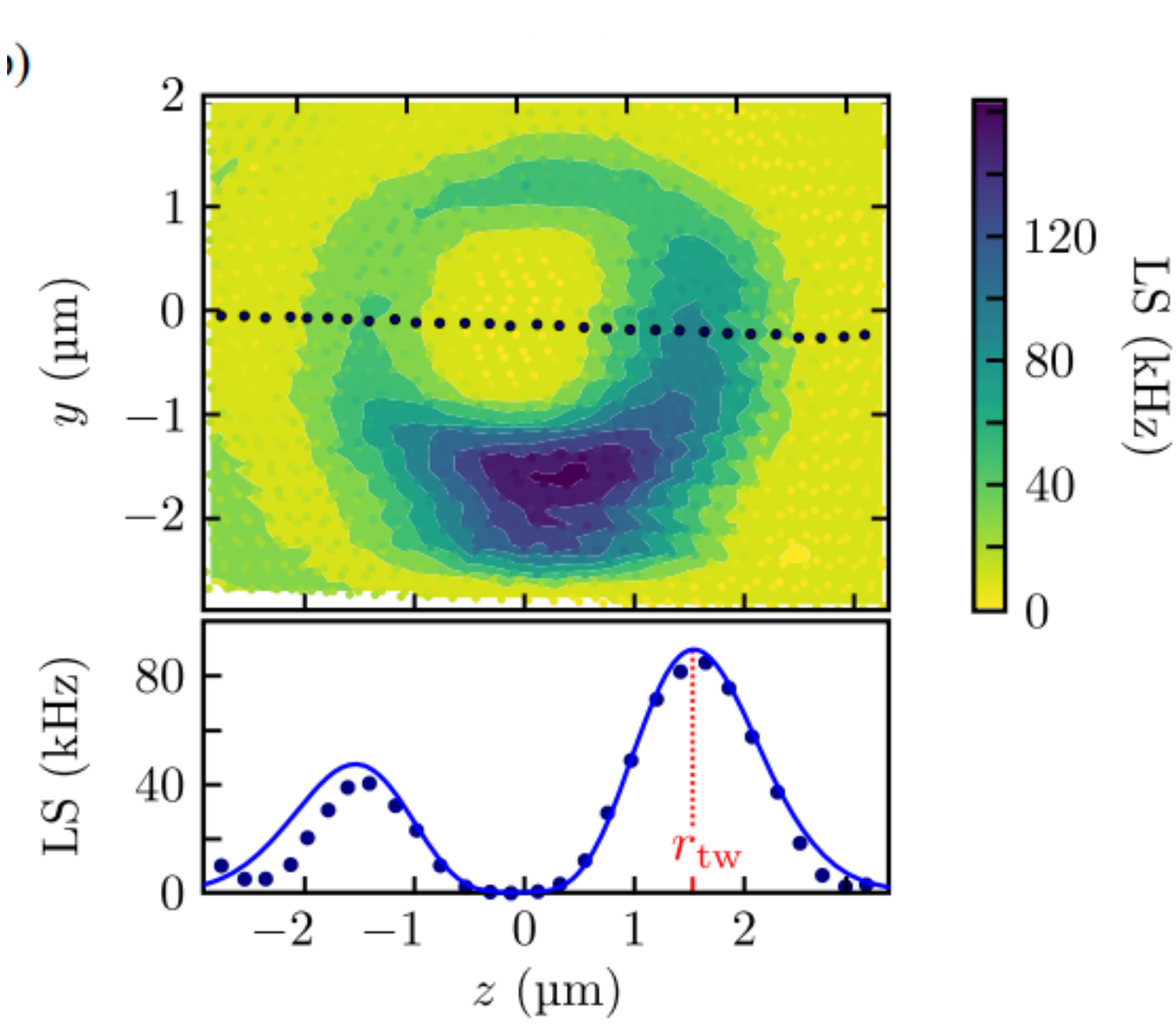
¹Physikalisch-Technische Bundesanstalt, Bundesallee 100, 38116 Braunschweig, Germany

²Institut für Mathematische Physik, Technische Universität Braunschweig, Mendelssohnstraße 3, 38106 Braunschweig, Germany

³Laboratory for Emerging Nanometrology, Langer Kamp 6a/b, 38106 Braunschweig, Germany



(Received 20 June 2022; accepted 14 November 2022; published 12 December 2022)



$$\xi = \Omega^2 / \Delta \nu$$

$$\xi_{\text{tw}} = 135(5) \text{ Hz}$$

$$\xi_{\text{pl}} = 30.3(9) \text{ Hz}$$

$$\xi_{\text{tw}} / \xi_{\text{pl}} = 4.5(2).$$

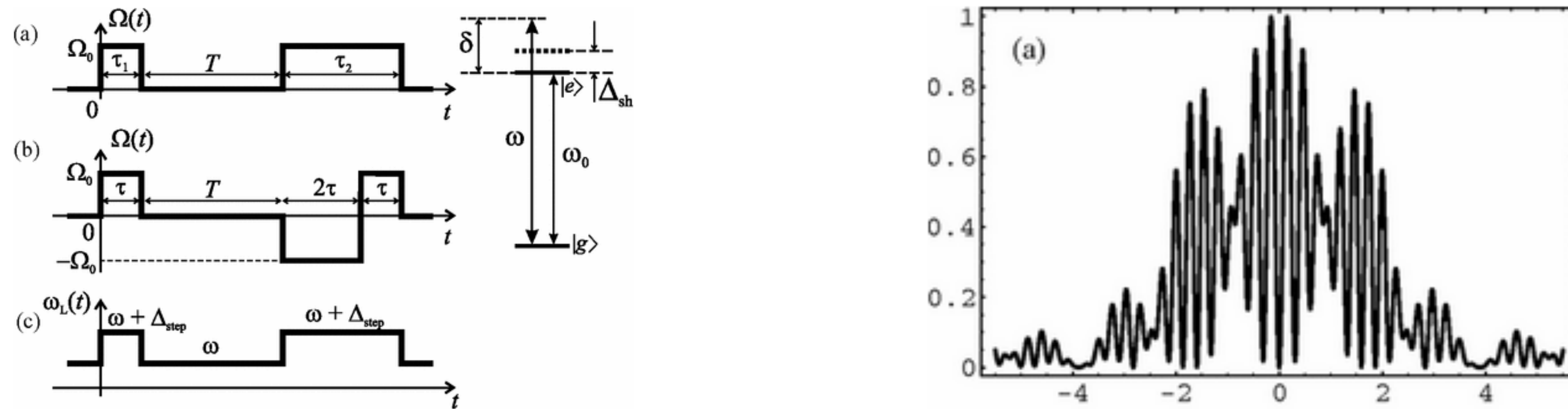
AC Stark Shift problems and applications

Problems for frequency standards

The devil's advocate: hyper-Ramsey and balanced-Ramsey spectroscopy

PHYSICAL REVIEW A **82**, 011804(R) (2010)

Hyper-Ramsey spectroscopy of optical clock transitions

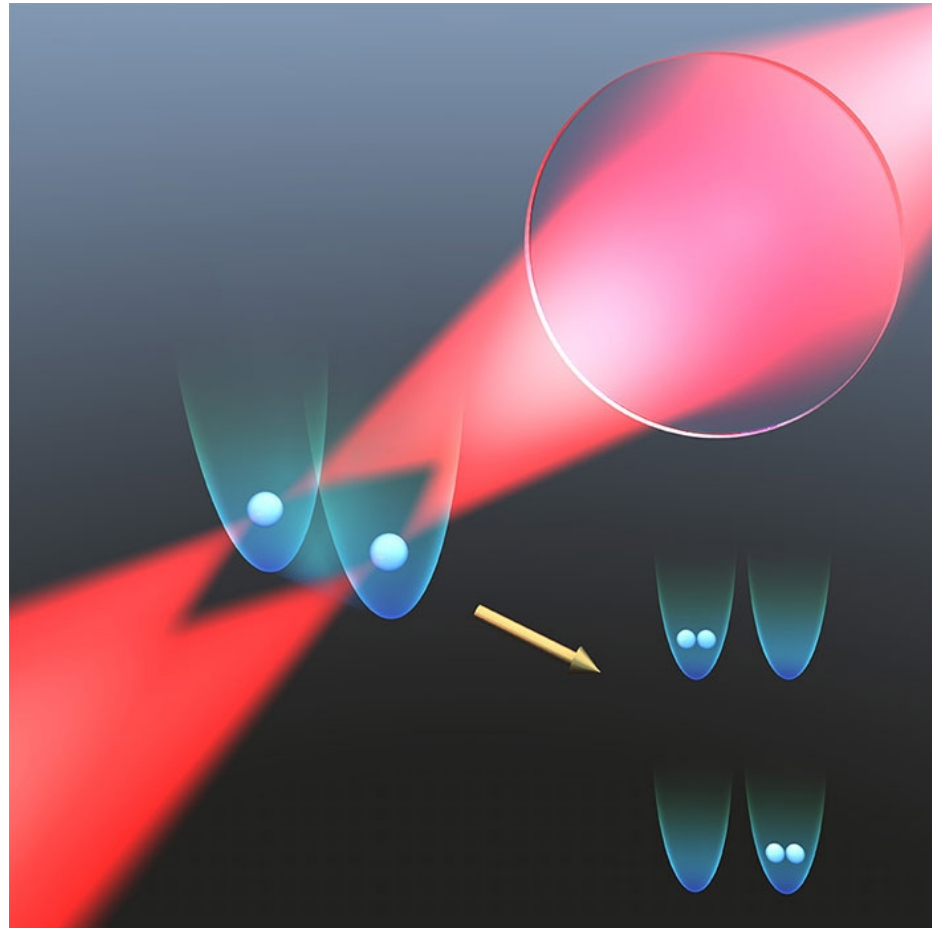


Suppression of AC stark Shift by 2-4 orders of magnitude

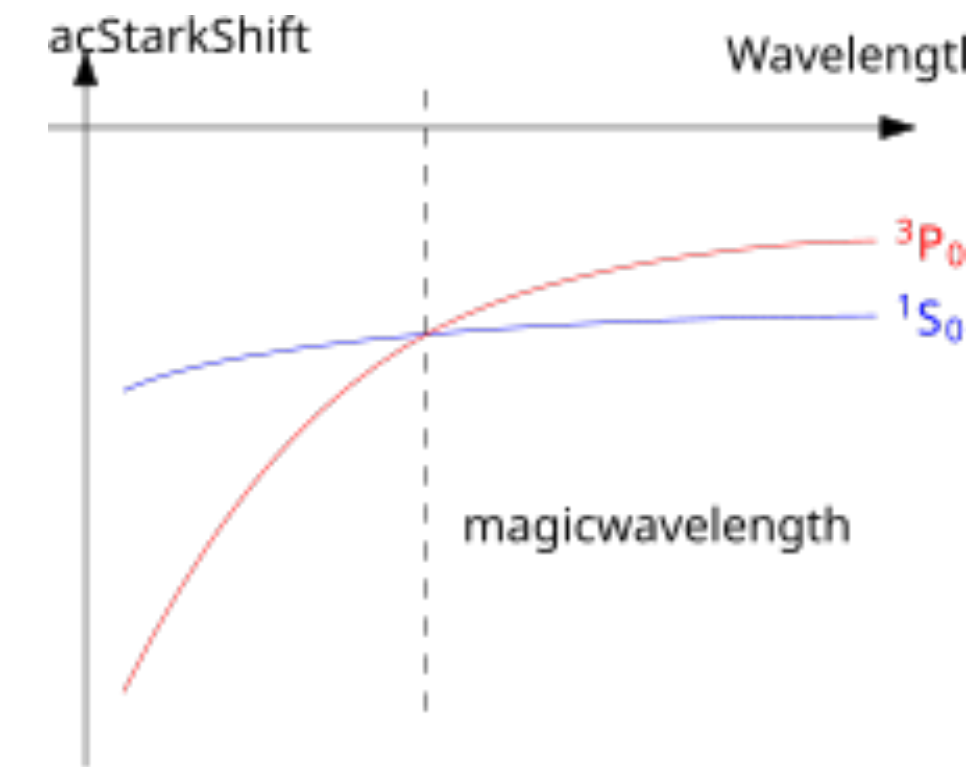
AC Stark Shift problems and applications

Optical Tweezers and Magic Wavelength

Low and high field seekers $\delta > 0$ or $\delta < 0$

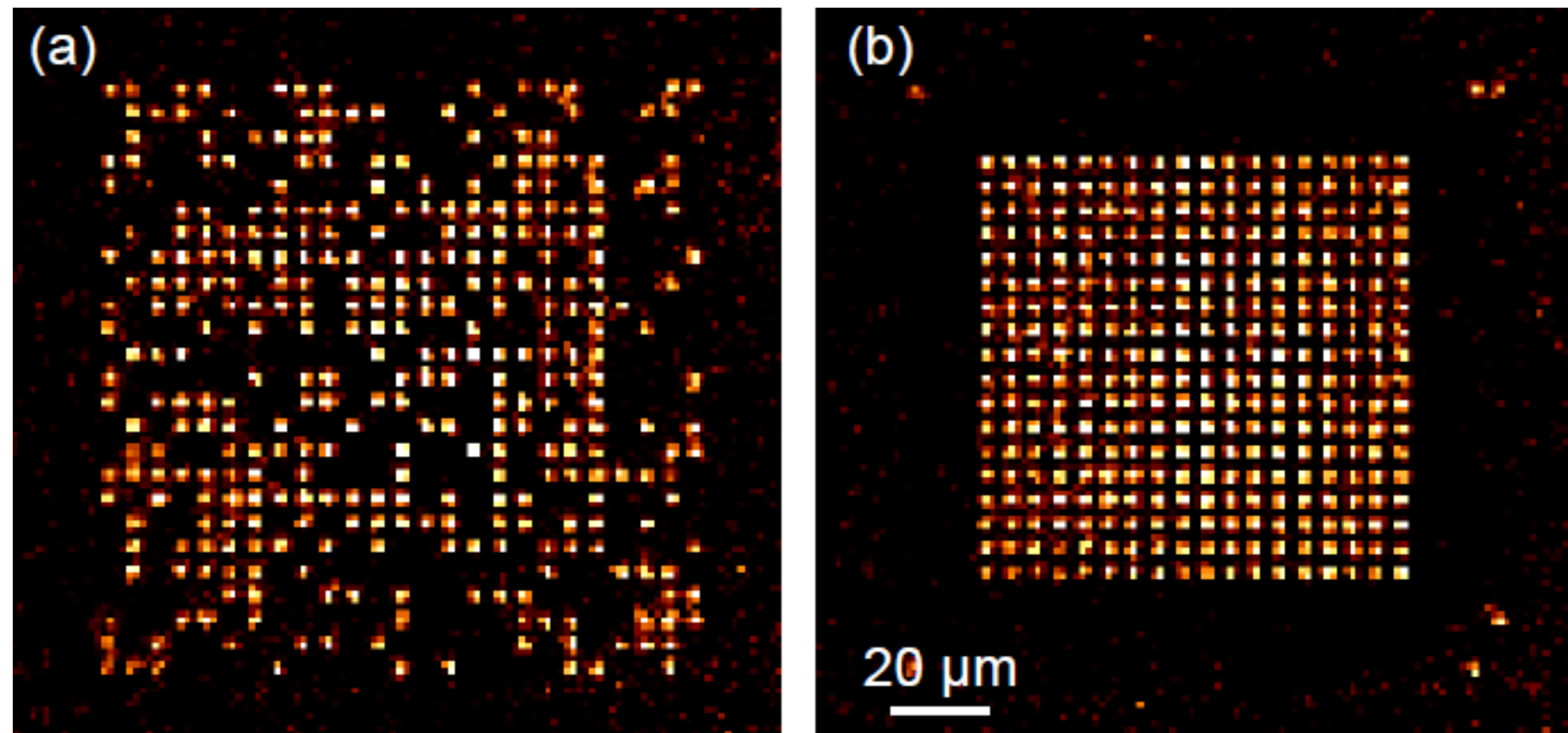


Magic Wavelength



Allows optical trapping,
leaving one (clock or qubit) transition undisturbed.

Atom arrays (record Quantum Volume by Lukin Group)

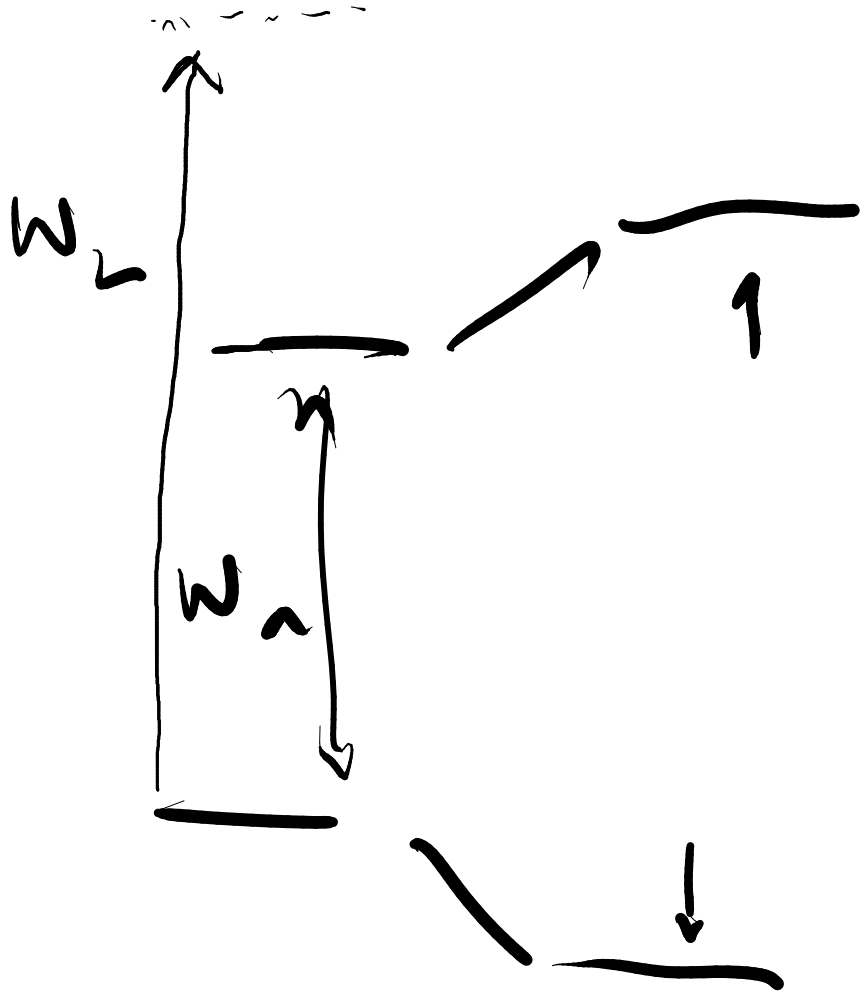


cred. Inst. d' Optique, Paris

AC Stark Shift problems and applications

Spin dependent forces.

Energy level shifts



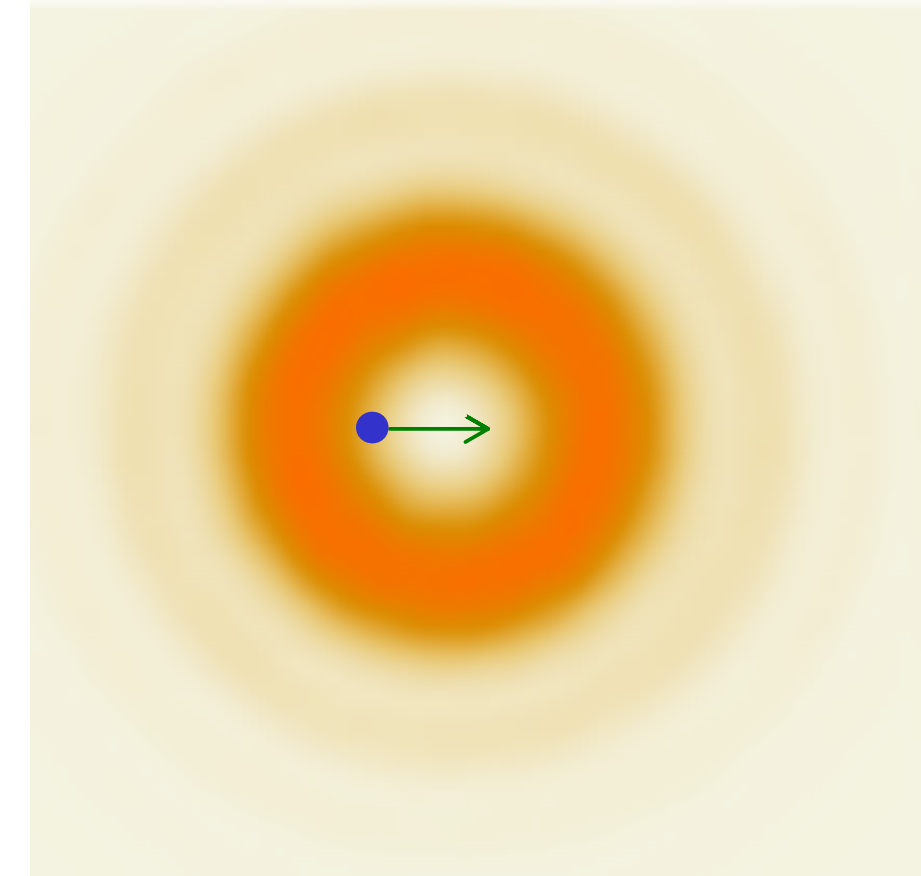
Standing Waves



Existing Applications

Gates between ions.
Generation of cat states.
Generation of squeezed states.
Spin dependent motional control of ions and atoms.

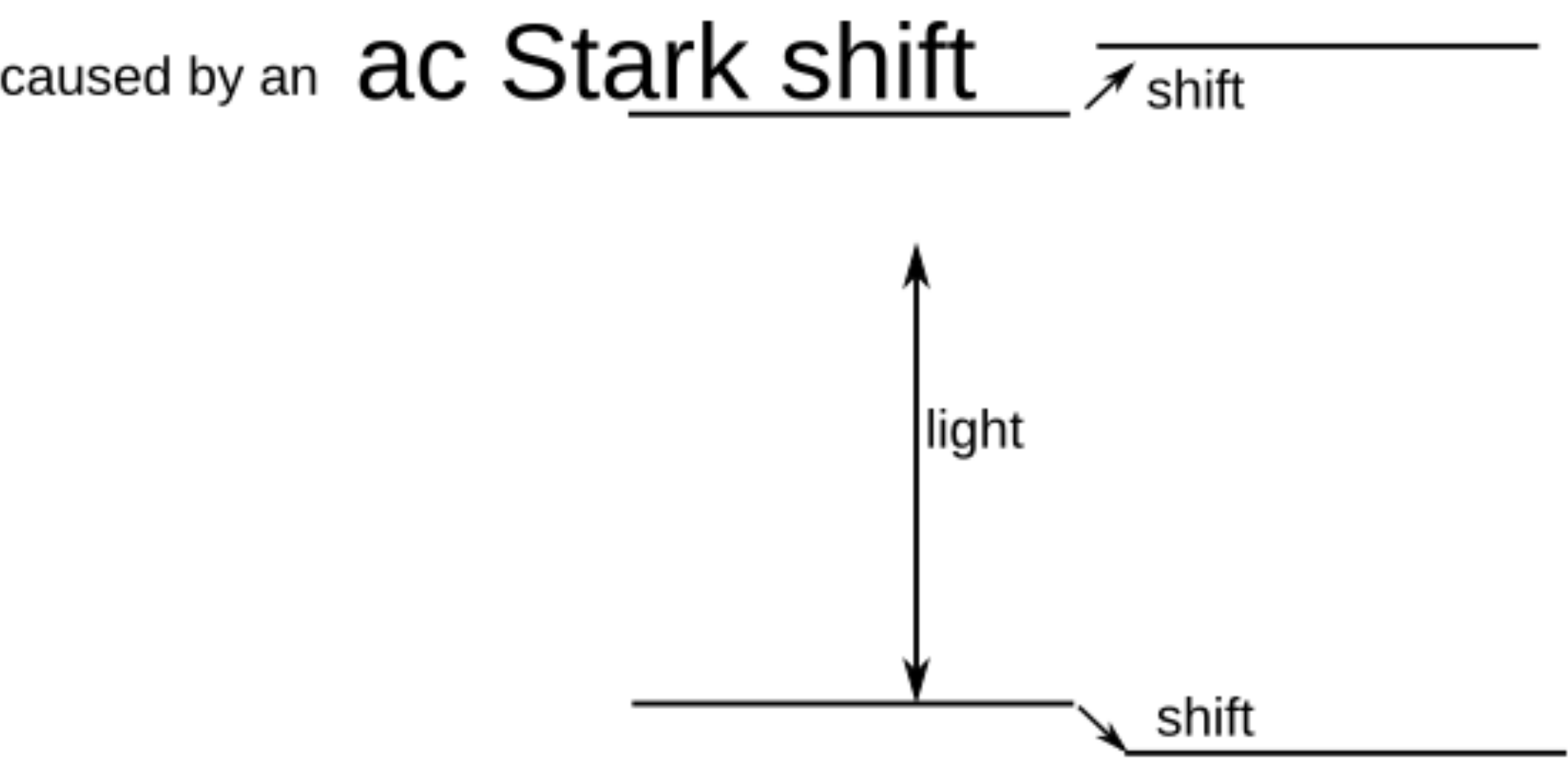
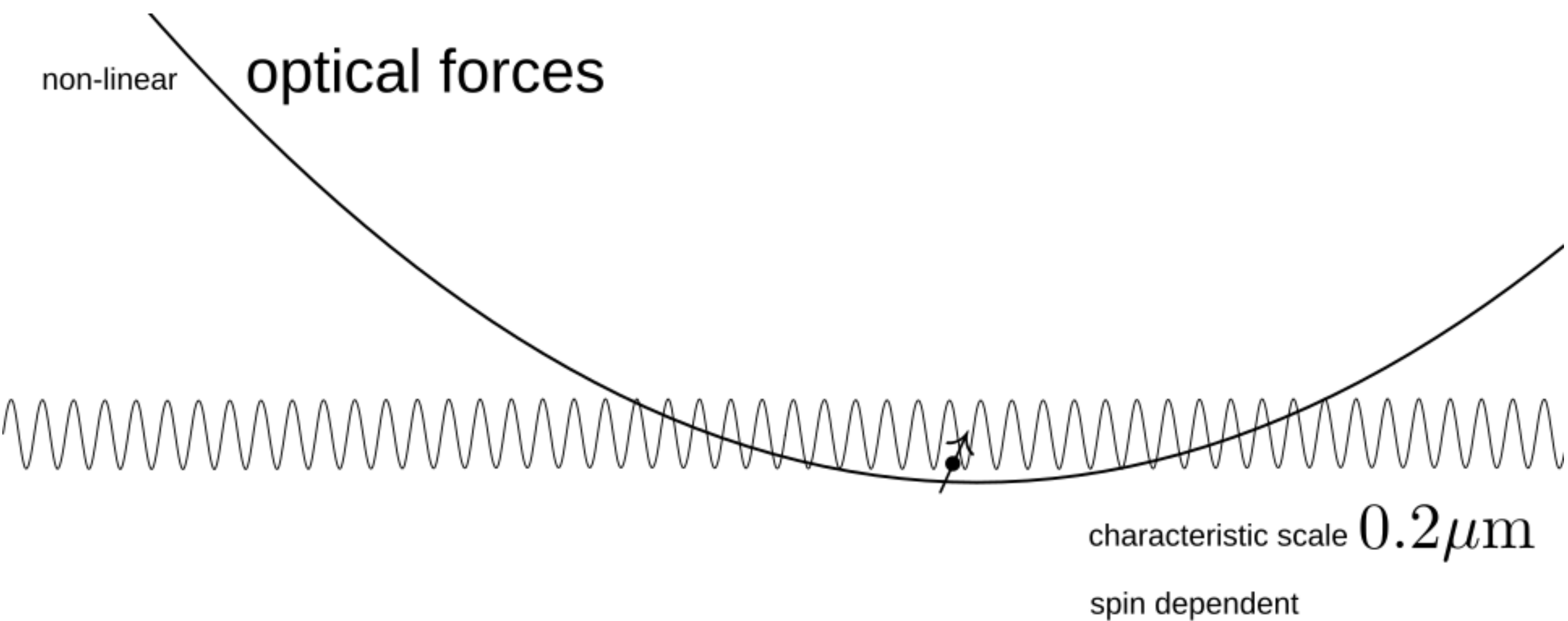
Structured Beams



Proposed Applications

Same, but without problems of phase stability!

Forces on ions



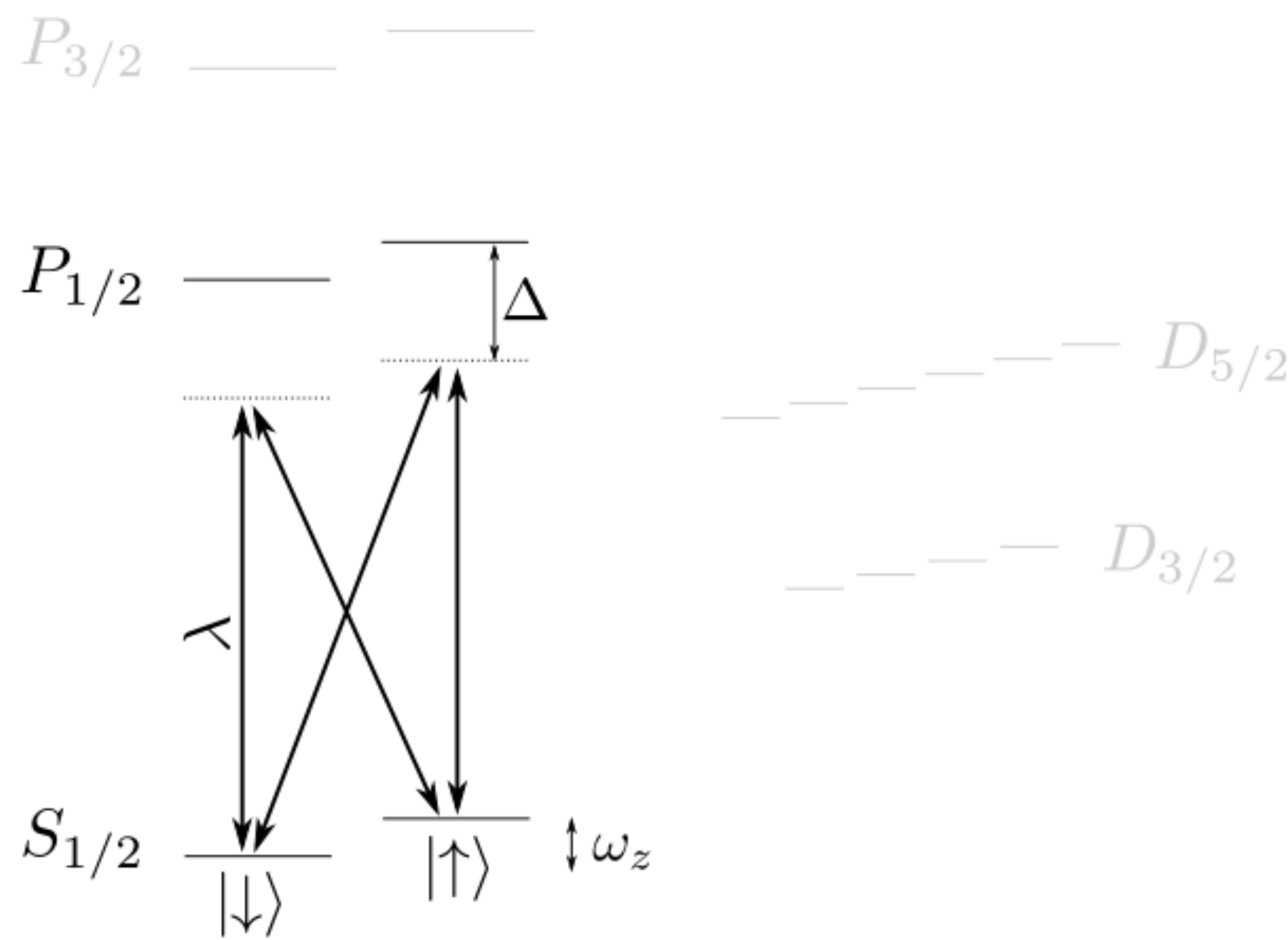
Forces on ions

our ion ^{40}Ca

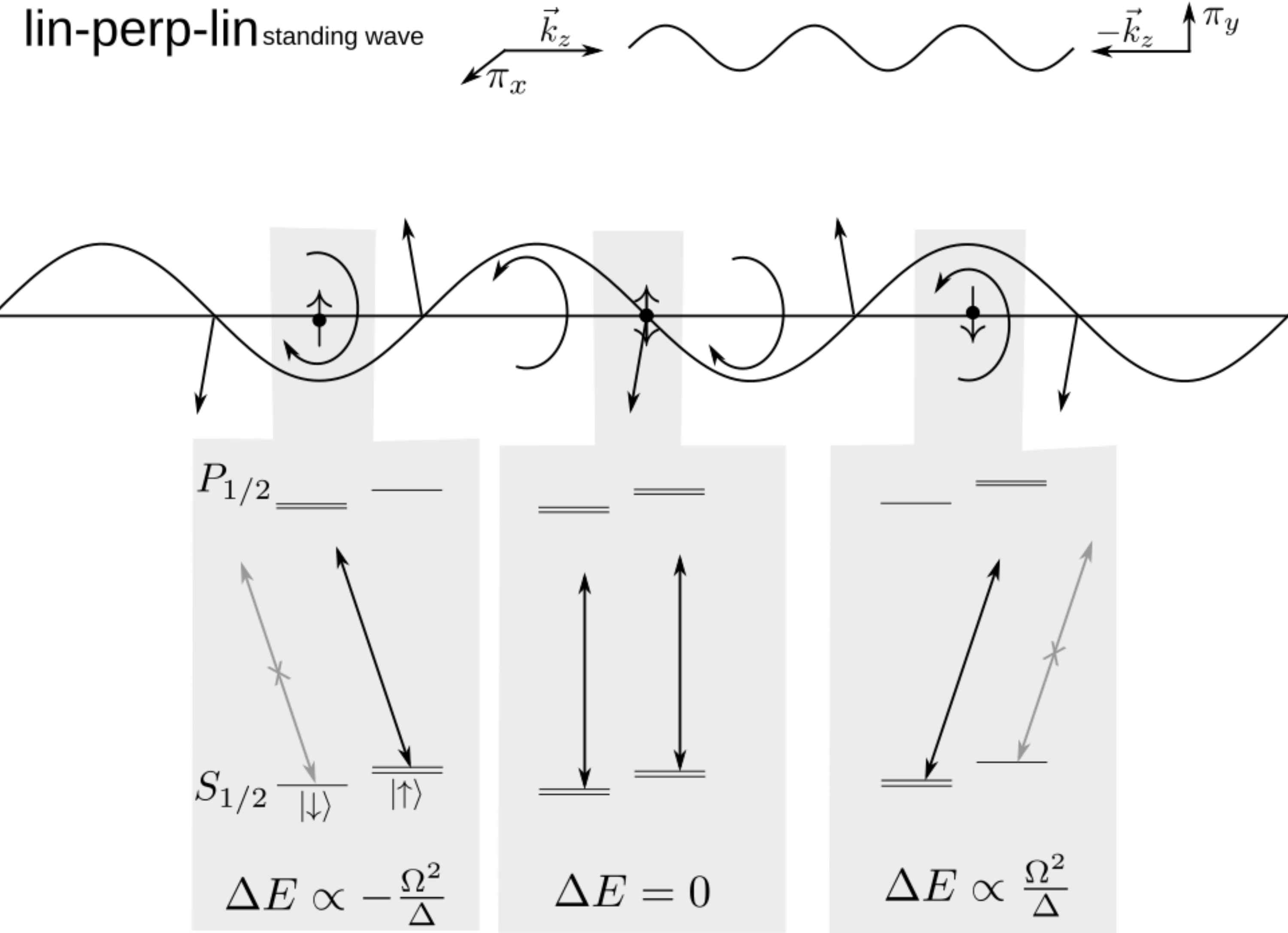
optical carrier $\lambda \approx 397\text{nm}$

detuning from transition $\Delta/2\pi \approx 30\text{GHz}$

Zeeman splitting $\omega_z/2\pi \approx 10\text{MHz}$

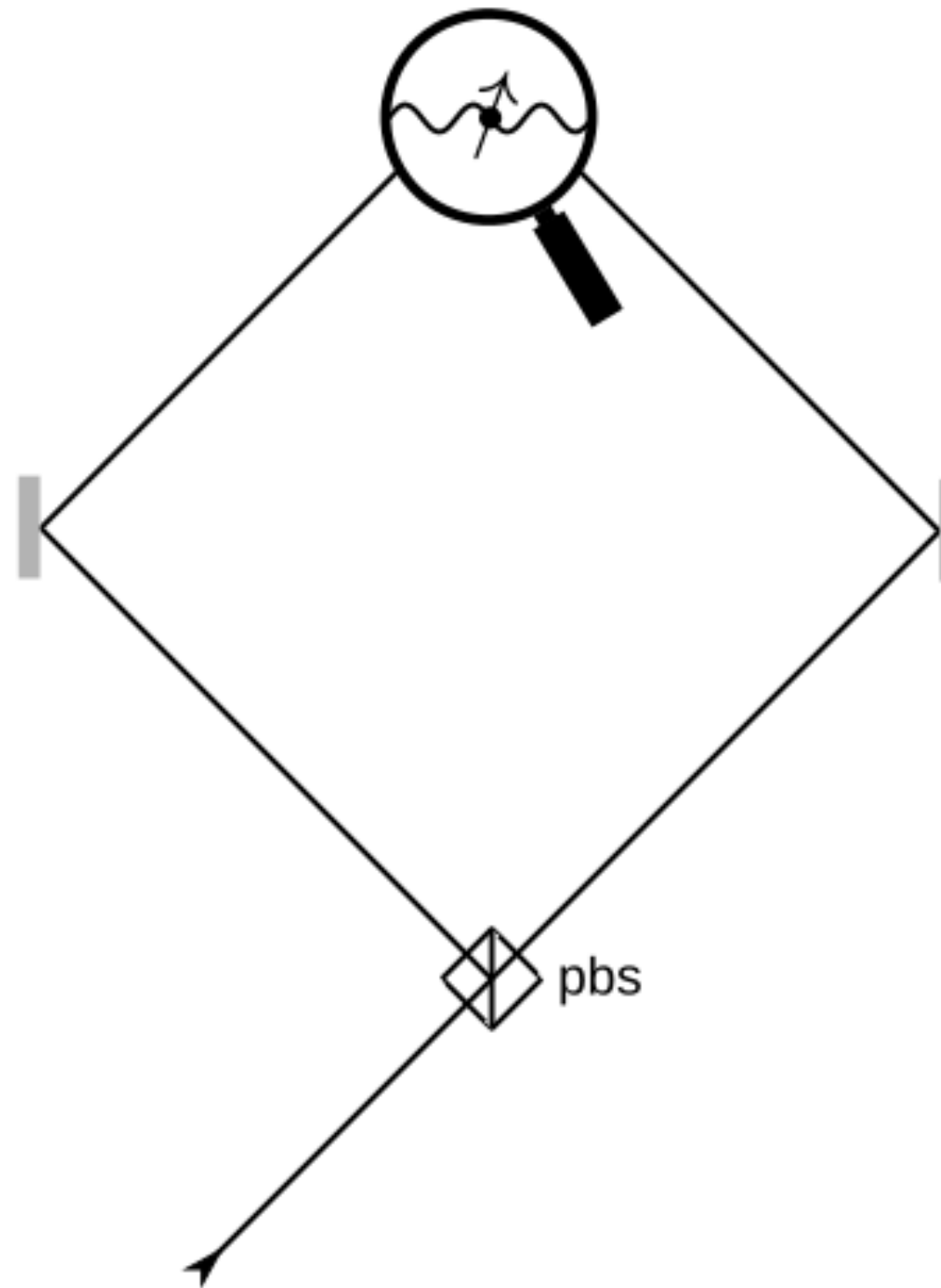


Forces on ions lin-perp-lin standing wave

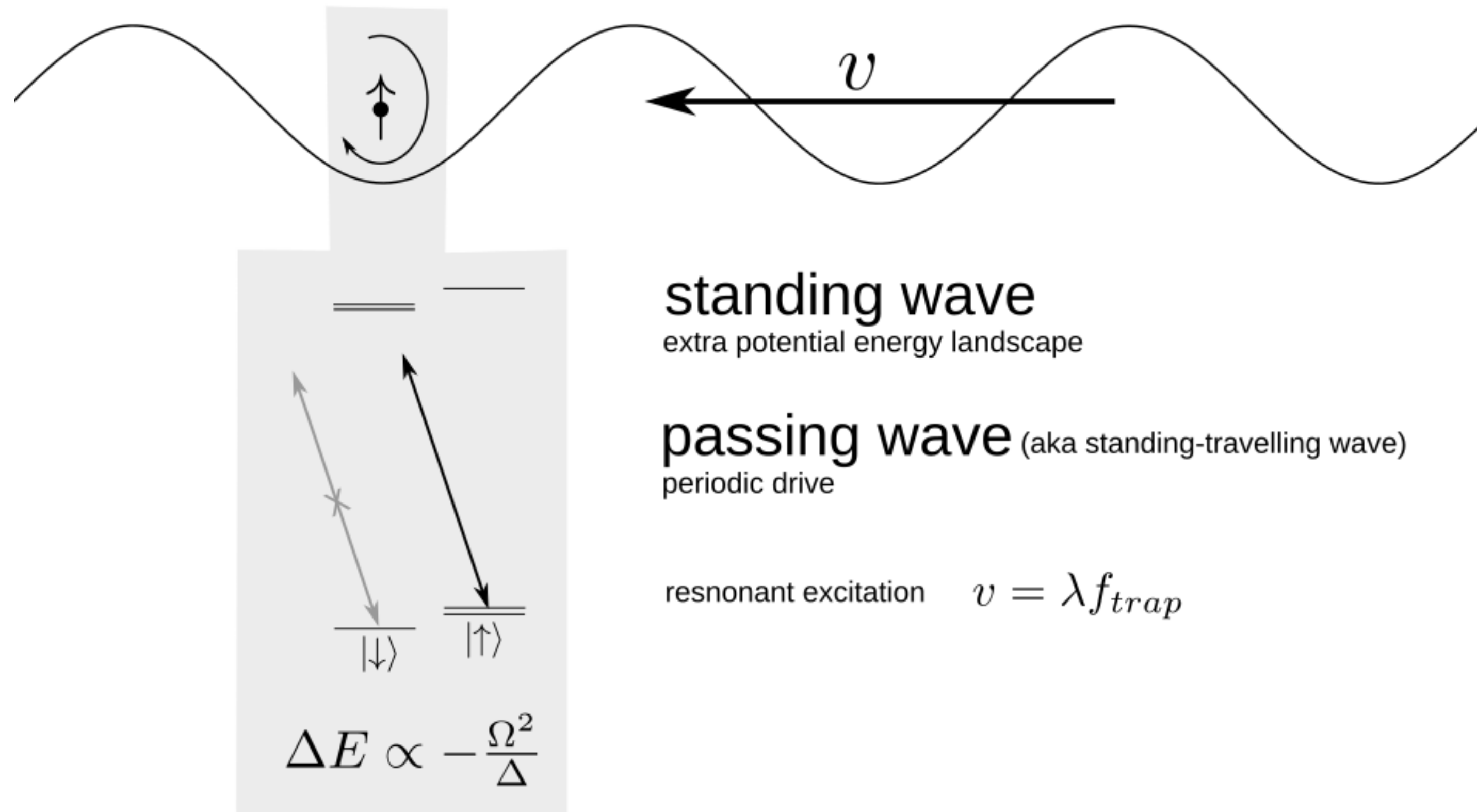


Forces on ions

lin-perp-lin standing wave

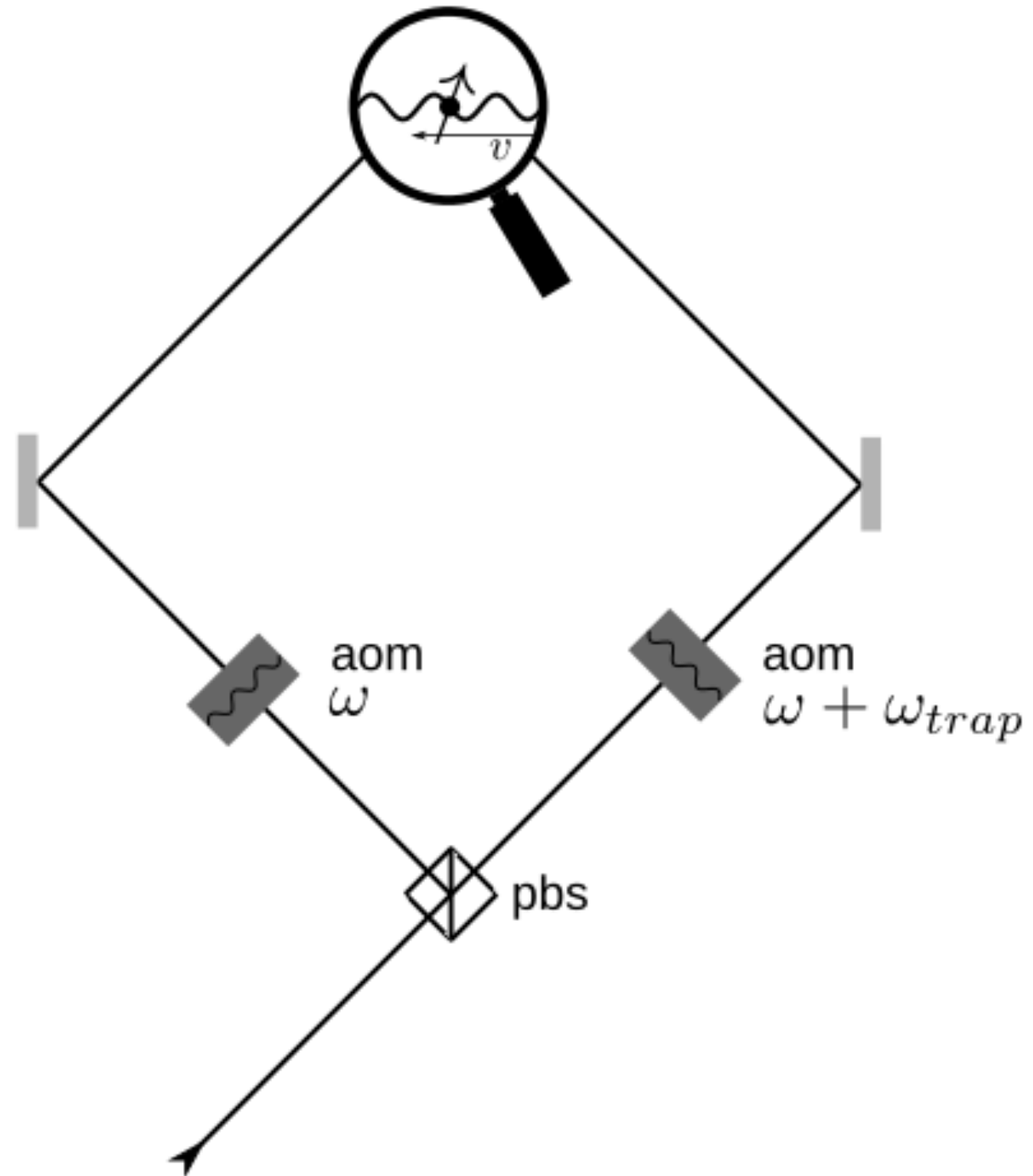


Forces on ions (off)-resonant motion excitation



Forces on ions

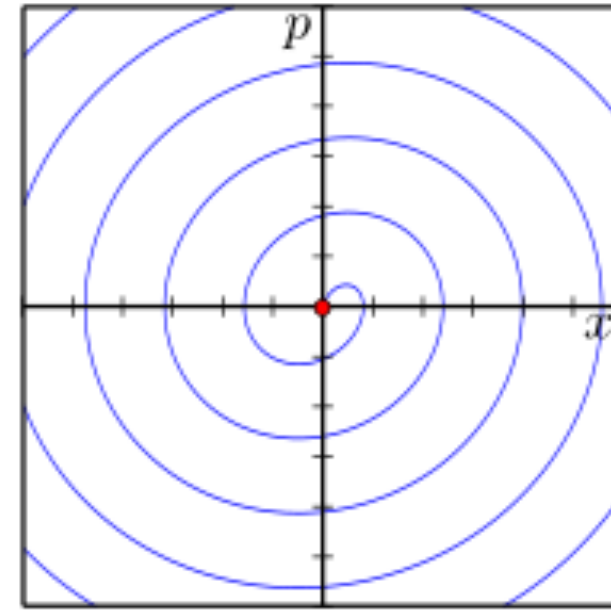
lin-perp-lin standing wave



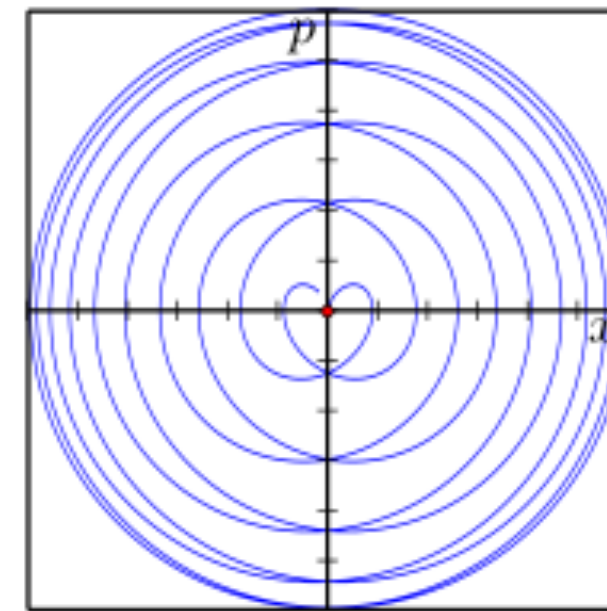
Forces on ions driven harmonic motion in phase space

phase space

resonant drive

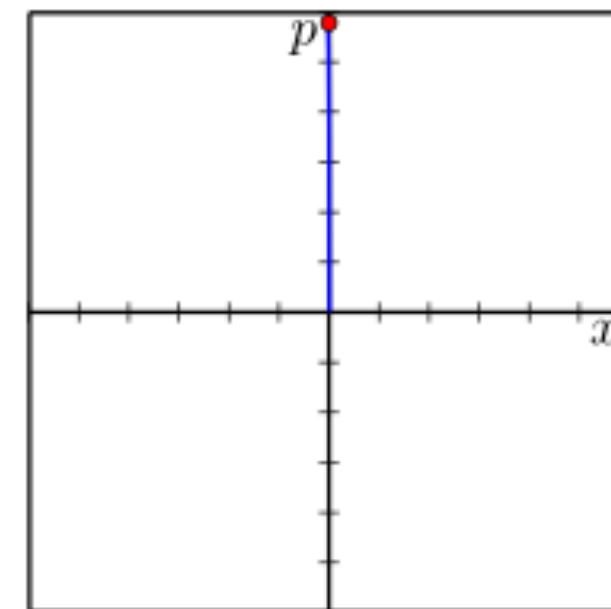


detuned drive

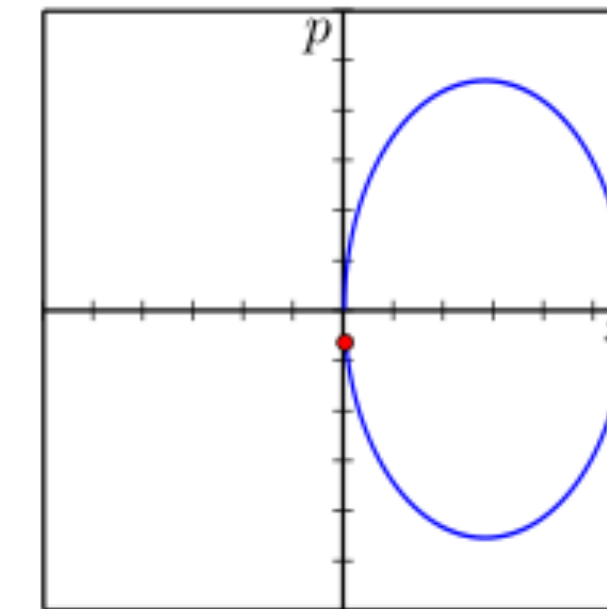


phase space rotating frame

resonant drive



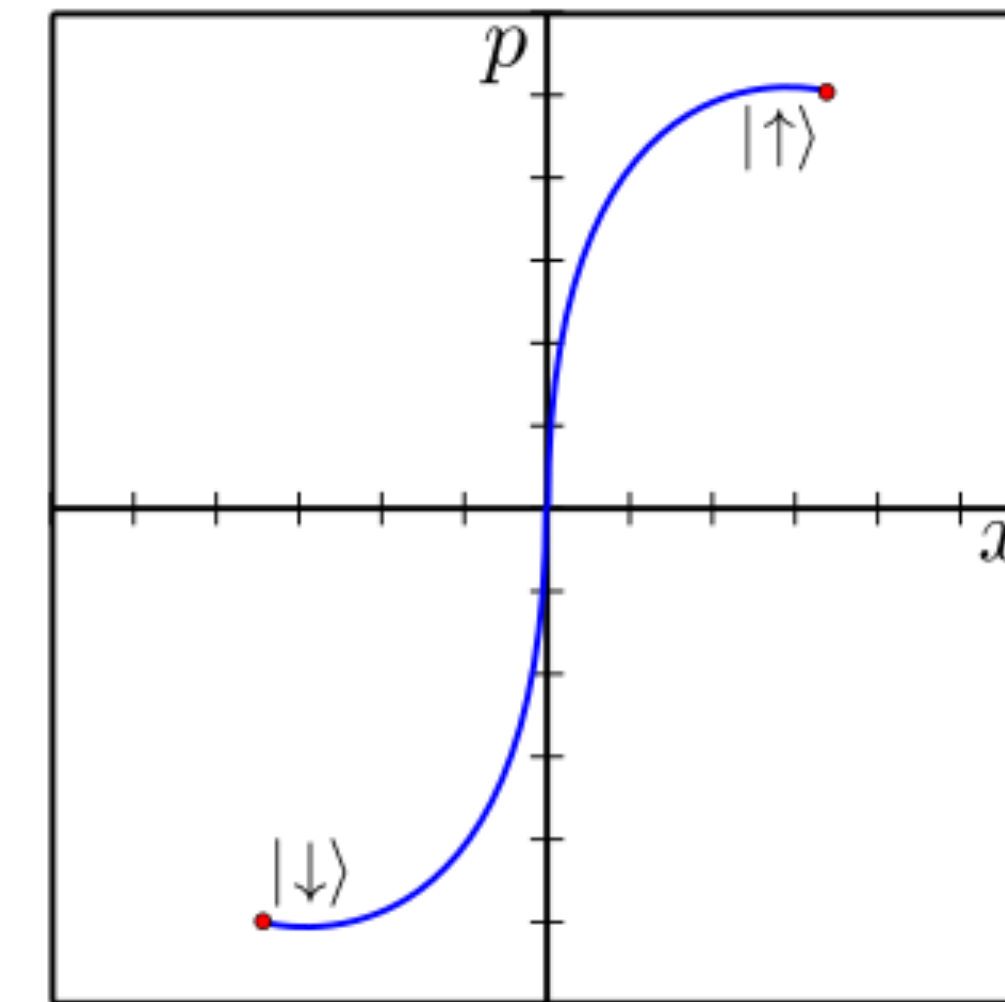
detuned drive



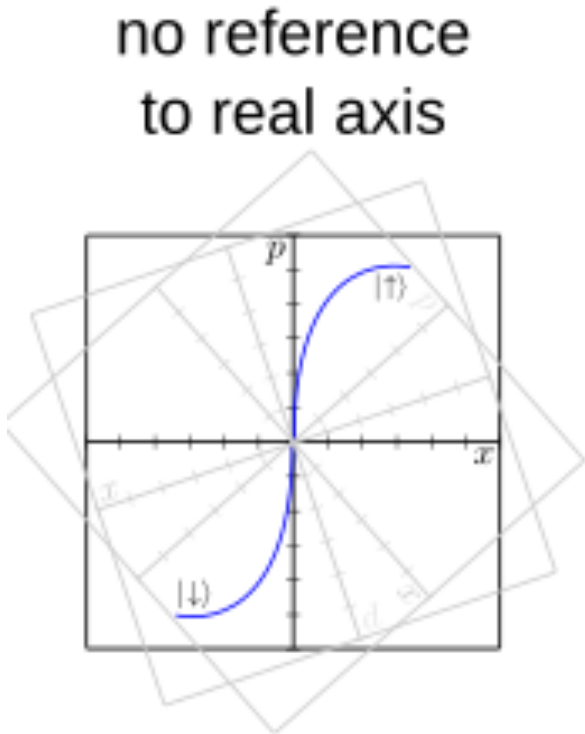
spin dependent force

cat states

$$(|\uparrow\rangle + |\downarrow\rangle)|0\rangle \rightarrow |\uparrow\rangle|\alpha\rangle + |\downarrow\rangle|-\alpha\rangle$$

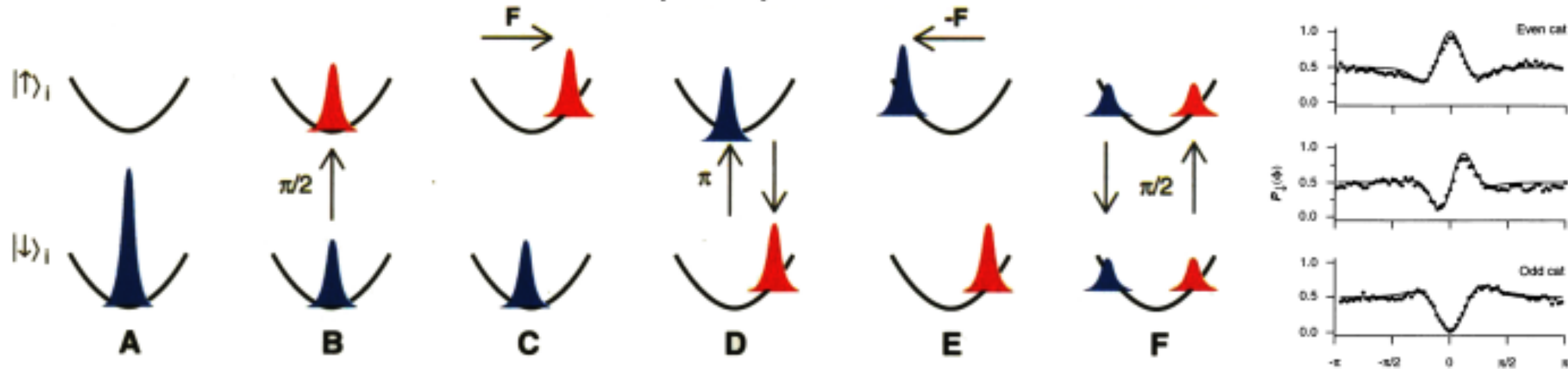


Forces on ions

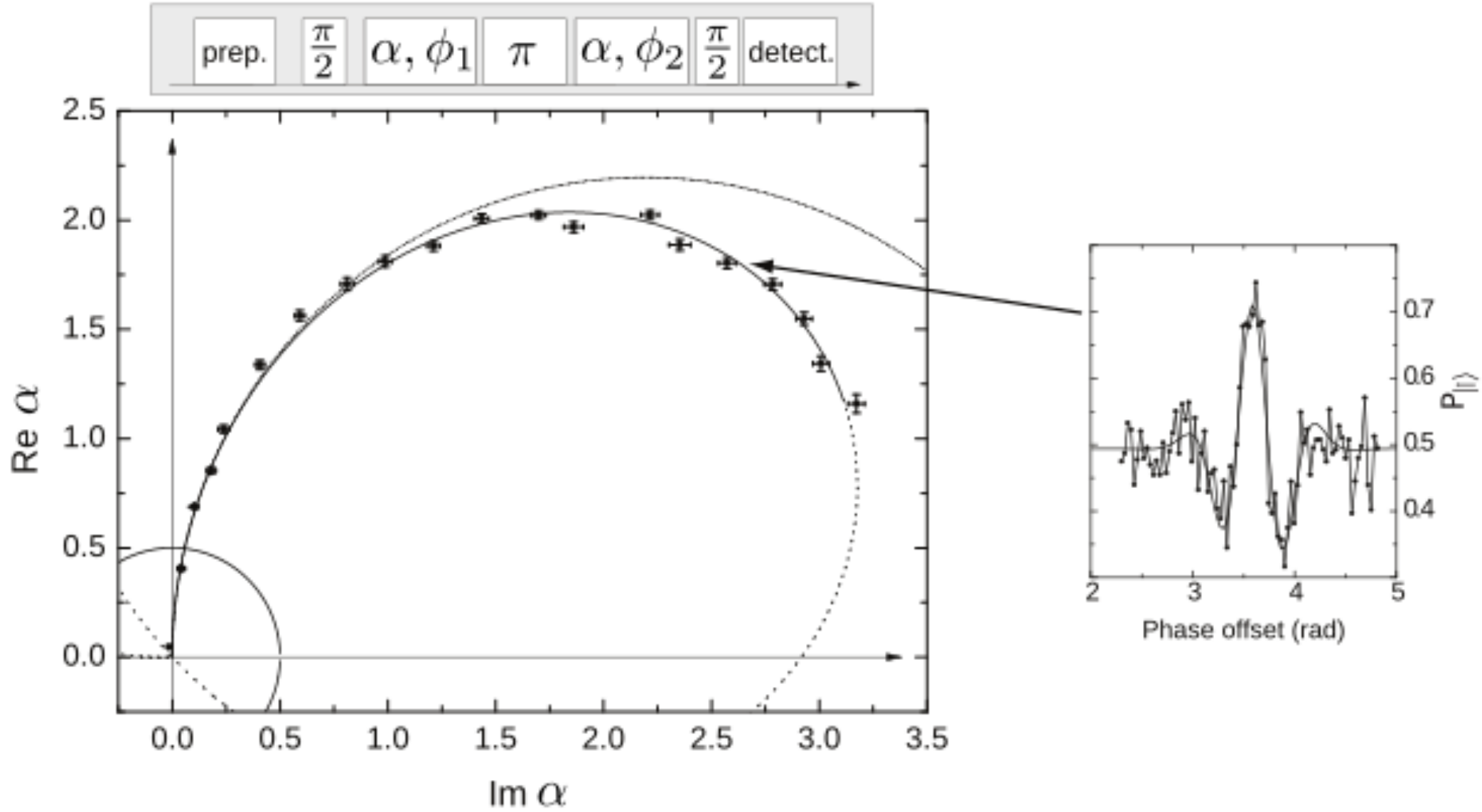


not a problem for interference singals

Schrödinger cat interference singals
Monroe et. al., Science 272, 1131 (1996)

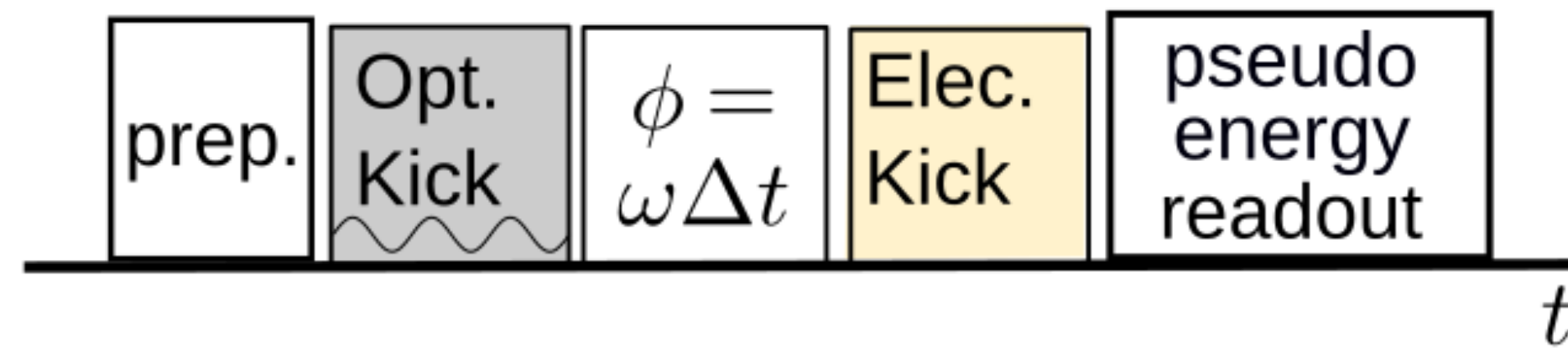
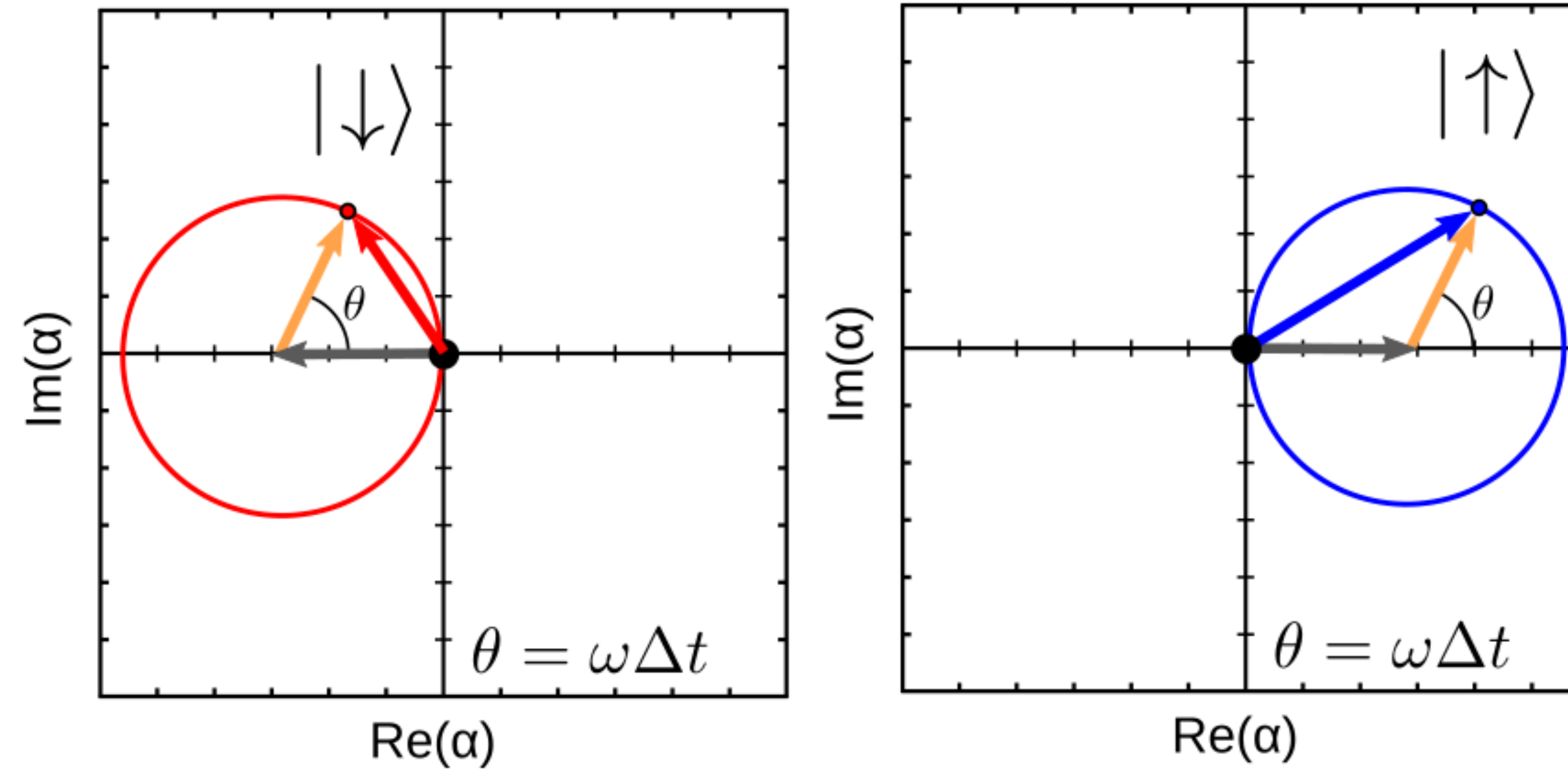


Schrödinger cat trajectory reconstruction
Poschinger et. al., PRL 105, 263602 (2010).



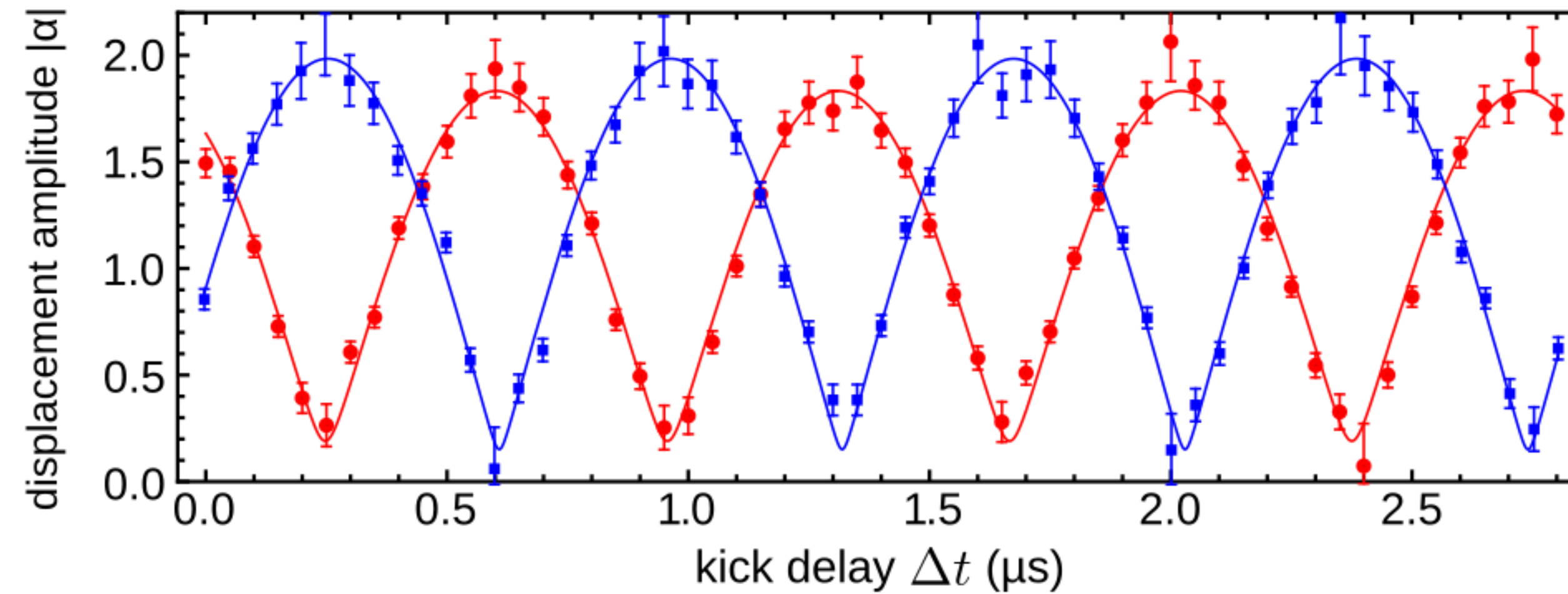
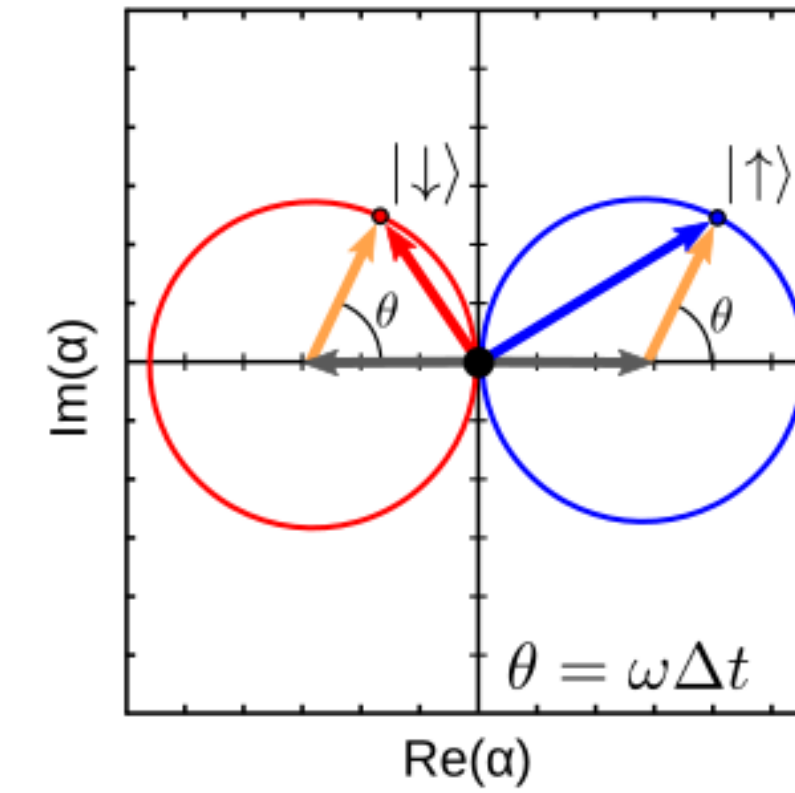
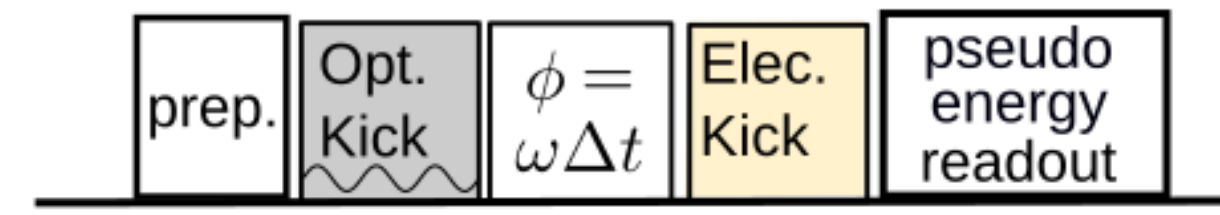
Forces on ions

phase stable optical forces
optical electrical kicks



Forces on ions

phase stable optical forces
optical electrical kicks



Forces on ions

spin heat engine

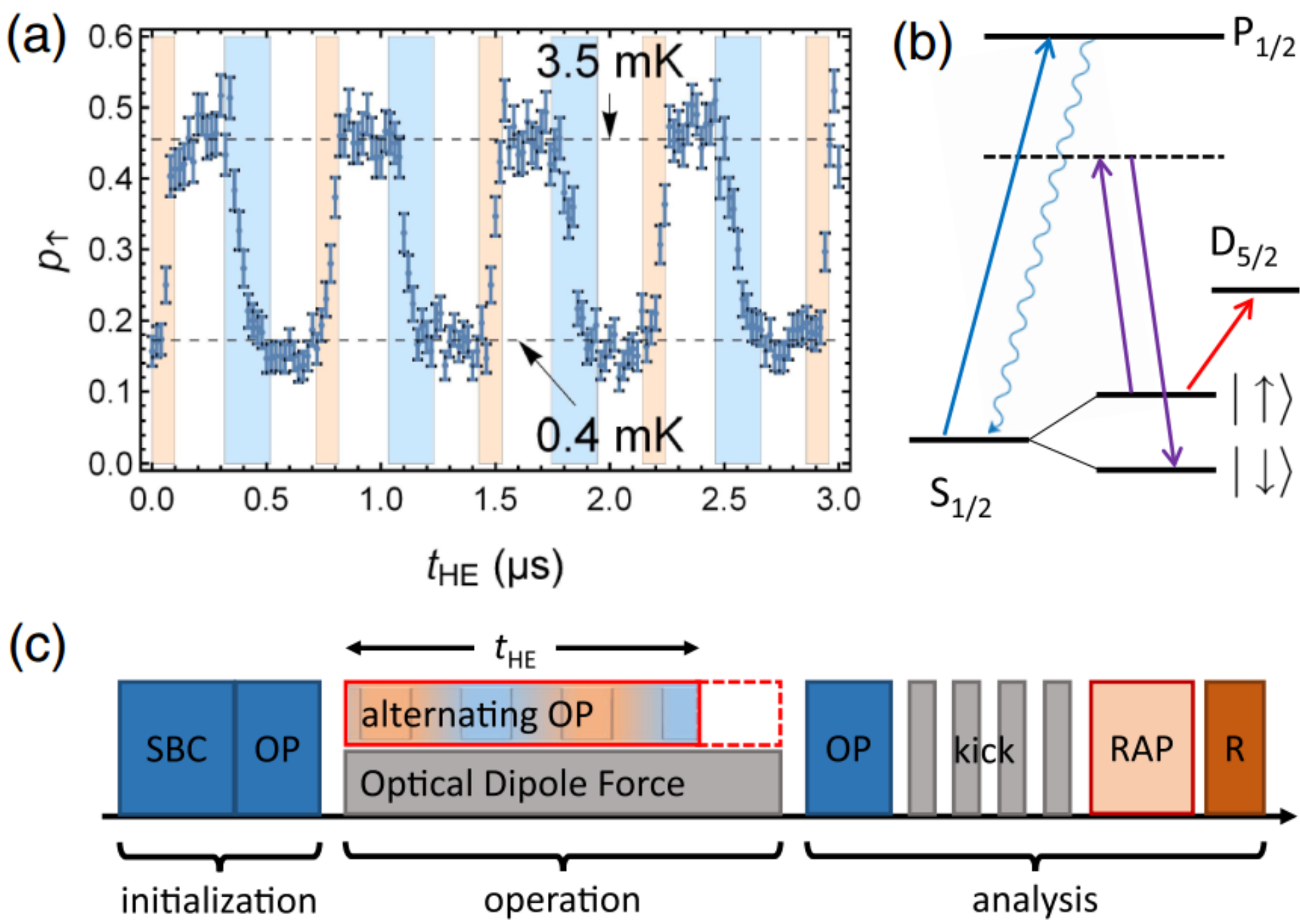
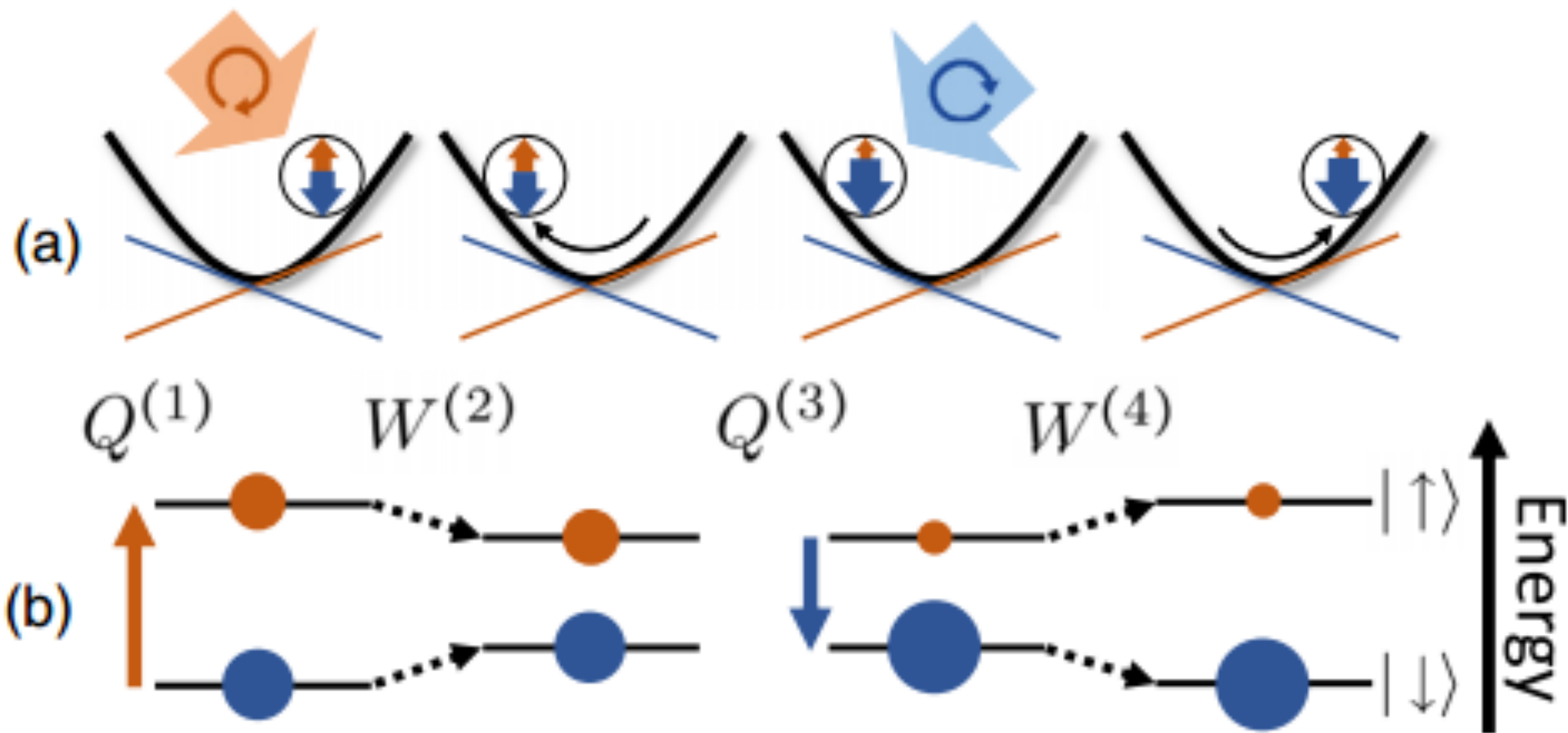
coupled to a harmonic oscillator flywheel

Spin Heat Engine Coupled to a Harmonic-Oscillator Flywheel

D. von Lindenfels,¹ O. Gräß,¹ C. T. Schmiegelow,^{1,*} V. Kaushal,¹ J. Schulz,¹ Mark T. Mitchison,² John Goold,²
F. Schmidt-Kaler,¹ and U. G. Poschinger^{1,†}

¹QUANTUM, Institut für Physik, Universität Mainz, Staudingerweg 7, 55128 Mainz, Germany

²School of Physics, Trinity College Dublin, College Green, Dublin 2, Ireland

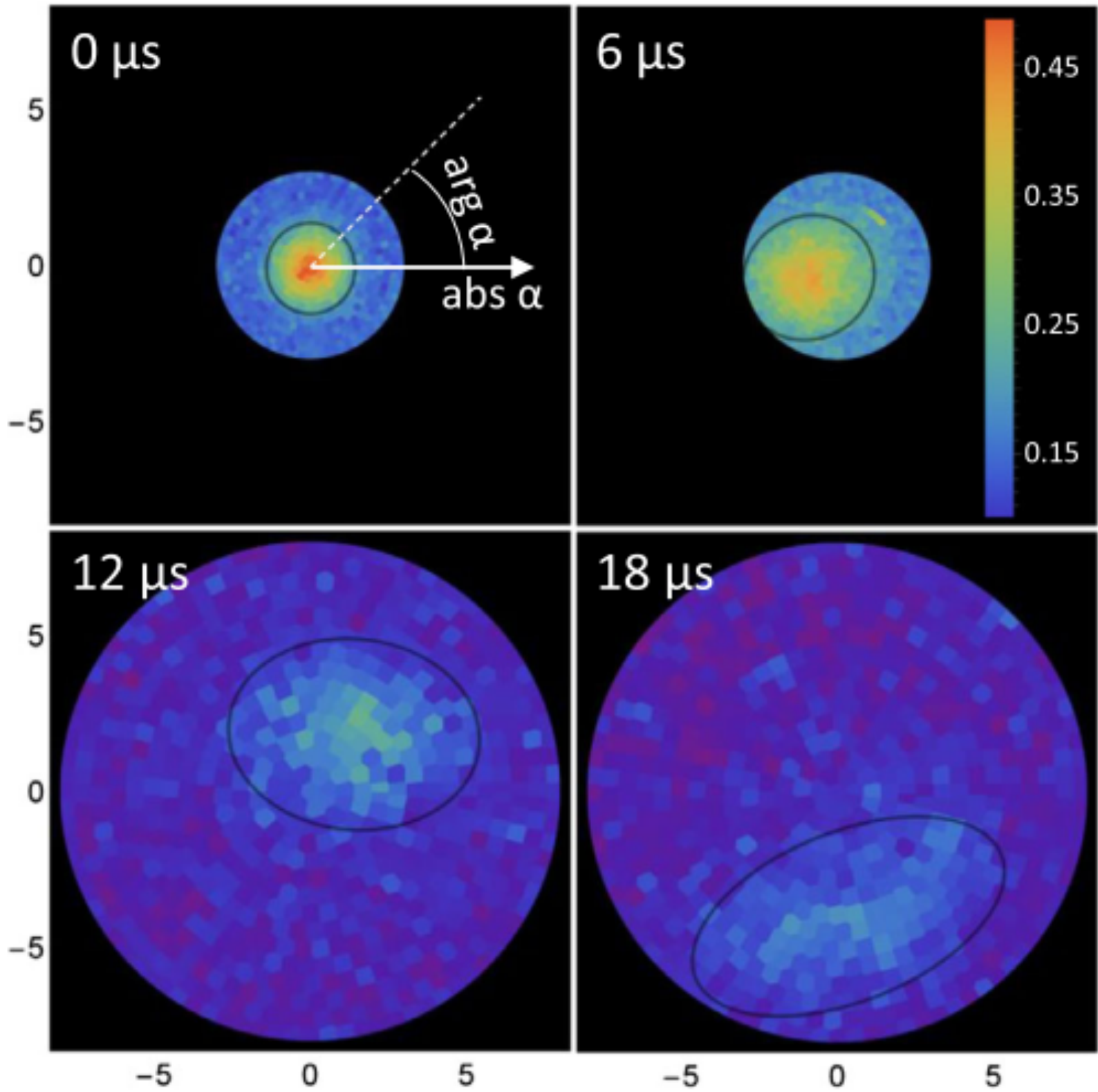


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²*School of Physics, Trinity College Dublin, College Green, Dublin 2, Ireland*

Time evolution of the phase space distributions.



Onset of the Spin Heat engine.

Forces on ions

Outlook and why go to structured beams.

Day Three

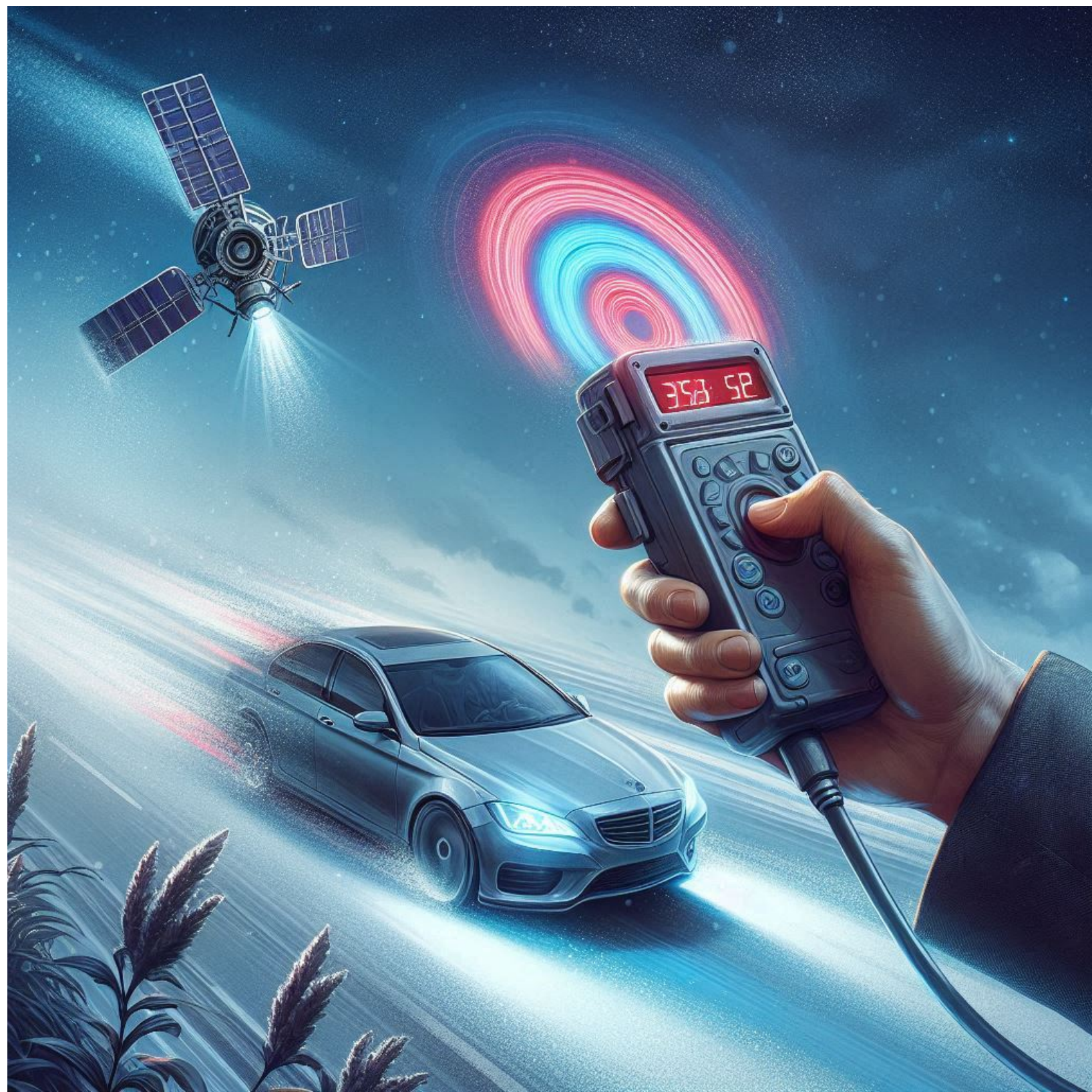
Part 3

More on interaction with gradients. Doppler shifts.

Super Doppler shifts - the other side of Super-kicks

Rotating ambulances

the rotational doppler Effect



Nicolás
Nuñez Barreto
PhD



Muriel
Bonetto
PhD Student



Marcelo
Luda
Associate
researcher



Cecilia
Cormick
Researcher

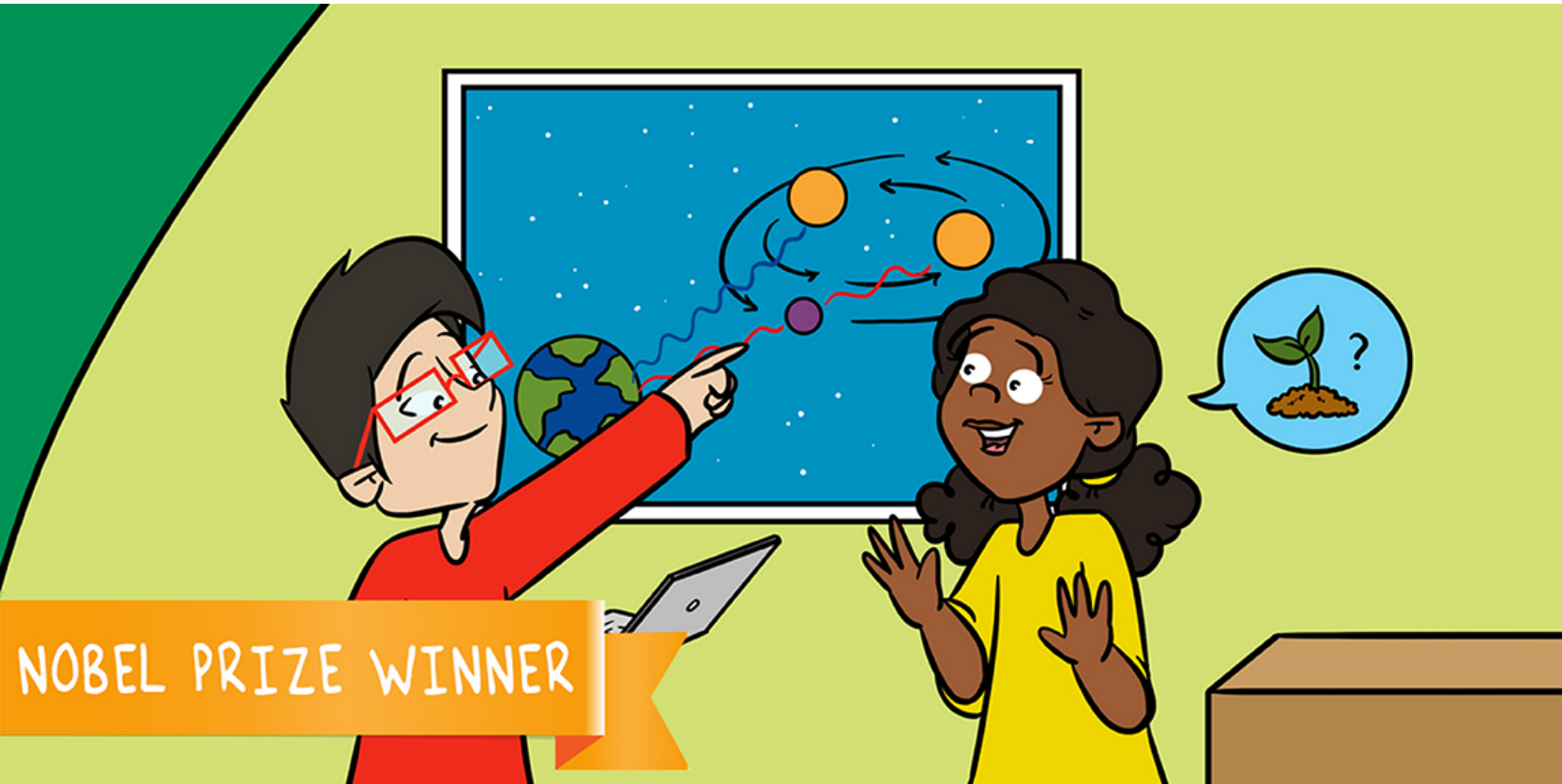
Observation of Space-Dependent Rotational Doppler Shifts with a Single Ion Probe

NA Nuñez Barreto, M Bonetto, MA Luda, C Cormick, CT Schmiegelow
Physical Review Letters 133 (18), 183601 (2024)

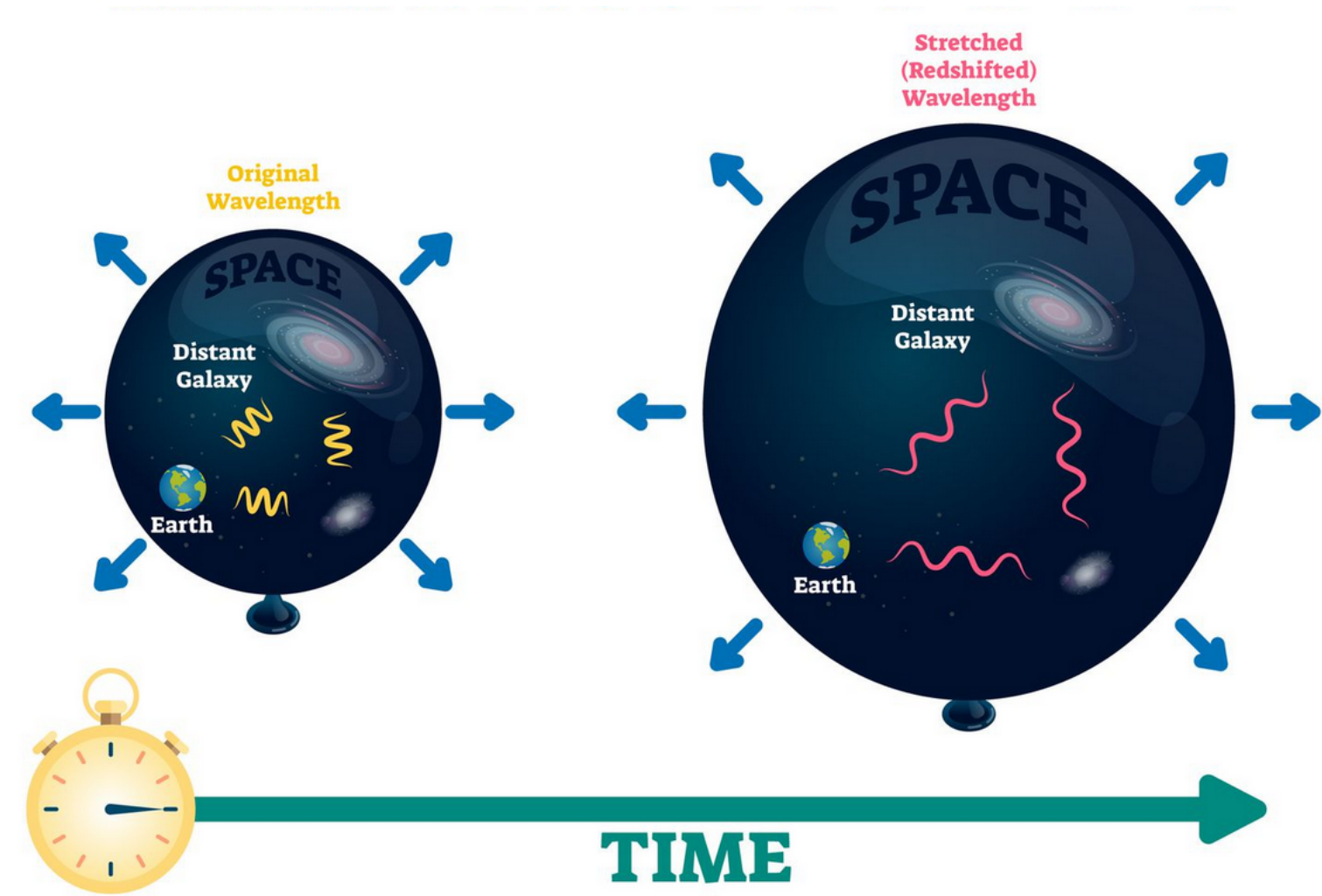
inspired by
Barreiro, S., Tabosa, J. W. R., Failache, H., & Lezama, A. (2006).
Spectroscopic observation of the rotational Doppler effect.
Physical Review Letters, 97(11), 113601.

Doppler shifts atómicos - ubicuos en la física moderna

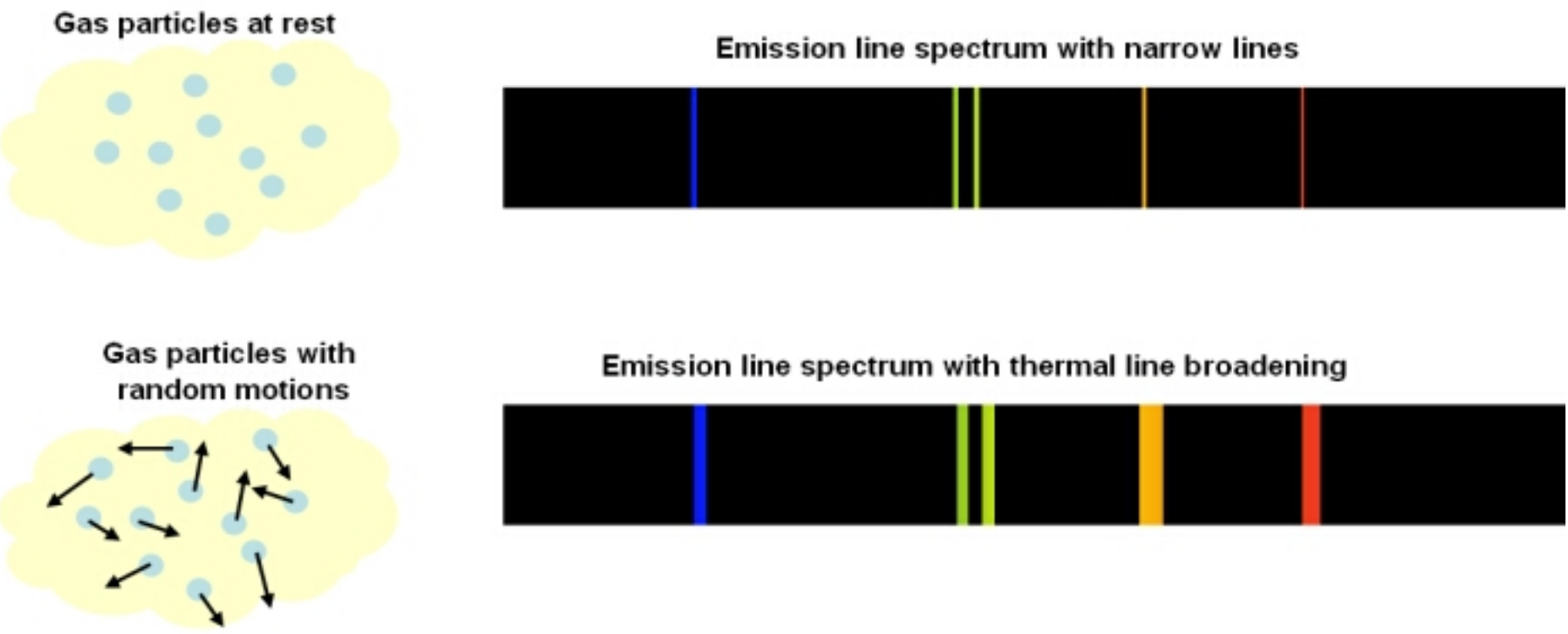
Astronomía
- velocidad de las fuentes



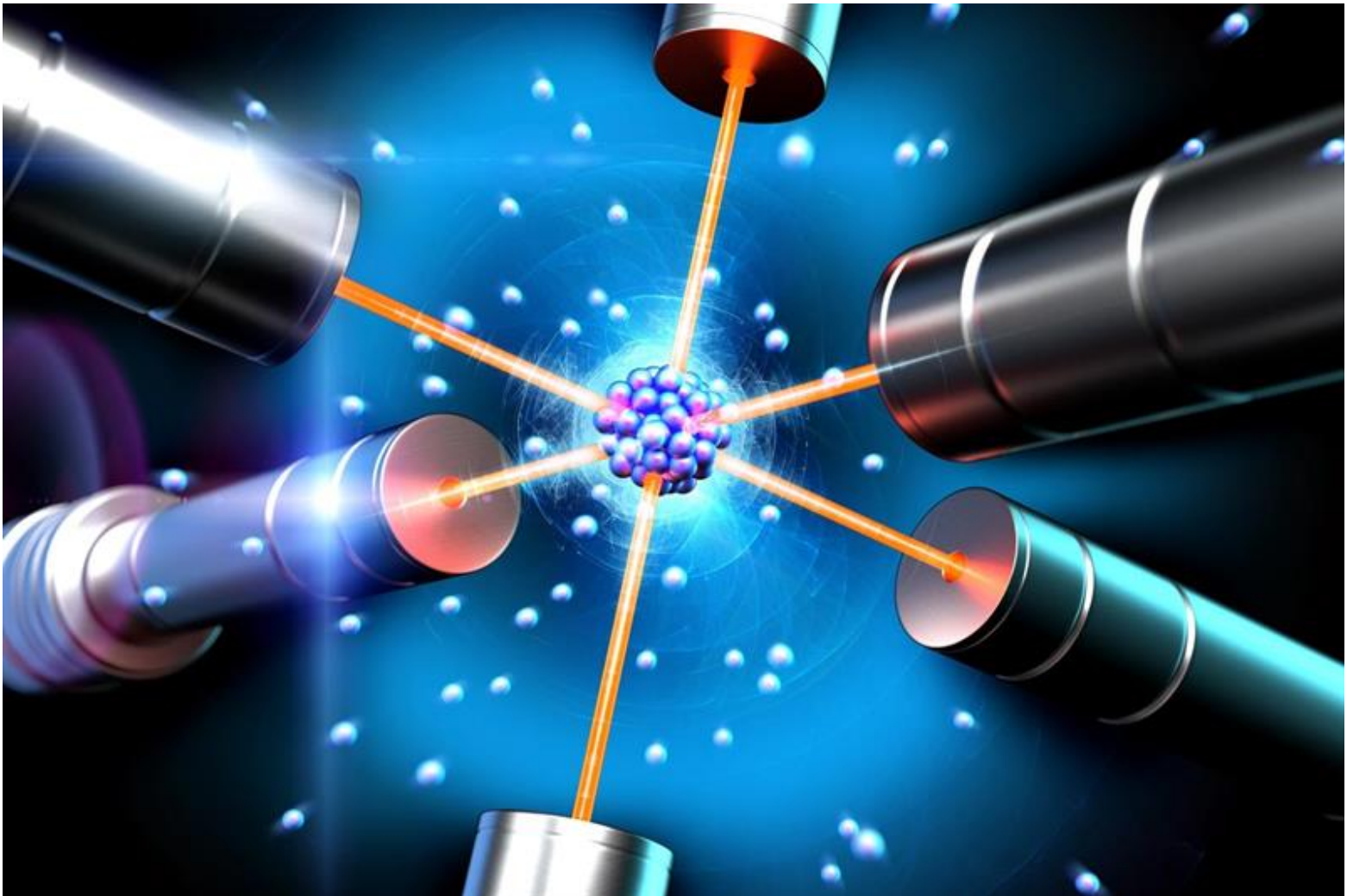
Cosmología
- edad de las fuentes



Espectroscopía
- temperatura de un gas

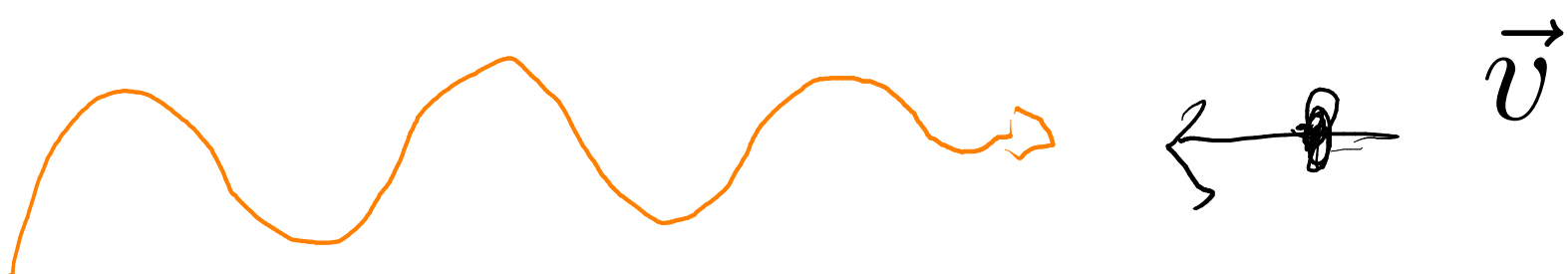


Óptica Cuántica
- enfriamiento y manipulación láser de átomos



Super-Doppler shifts - every actuator is a a sensor

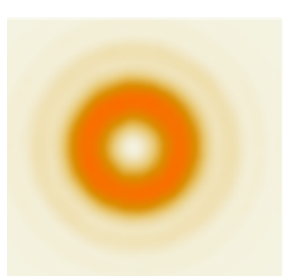
Doppler effect for a plane wave



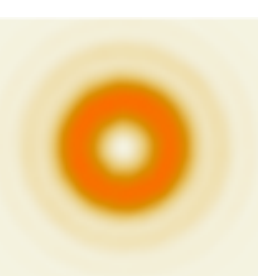
$E = E_0 e^{i k z}$
 $\omega_{\text{atomo}} = \omega_{\text{labo}} + \underbrace{\vec{k} \cdot \vec{v}}_{\delta}$

Doppler effect for a generic wave

$$\delta = \frac{\vec{\nabla} E}{|E|} \cdot \vec{v}$$



Doppler effect for a Laguerre-Gauss Wave



$$\delta_{LG} = - \left[k + \frac{k r^2}{2(z^2 + z_R^2)} \left(\frac{2z^2}{z^2 + z_R^2} - 1 \right) - \frac{(2p + |l| + 1) z_R}{z^2 + z_R^2} \right] V_z - \left(\frac{k r z}{z^2 + z_R^2} \right) V_R - \left(\frac{l}{r} \right) V_\phi$$

Linear

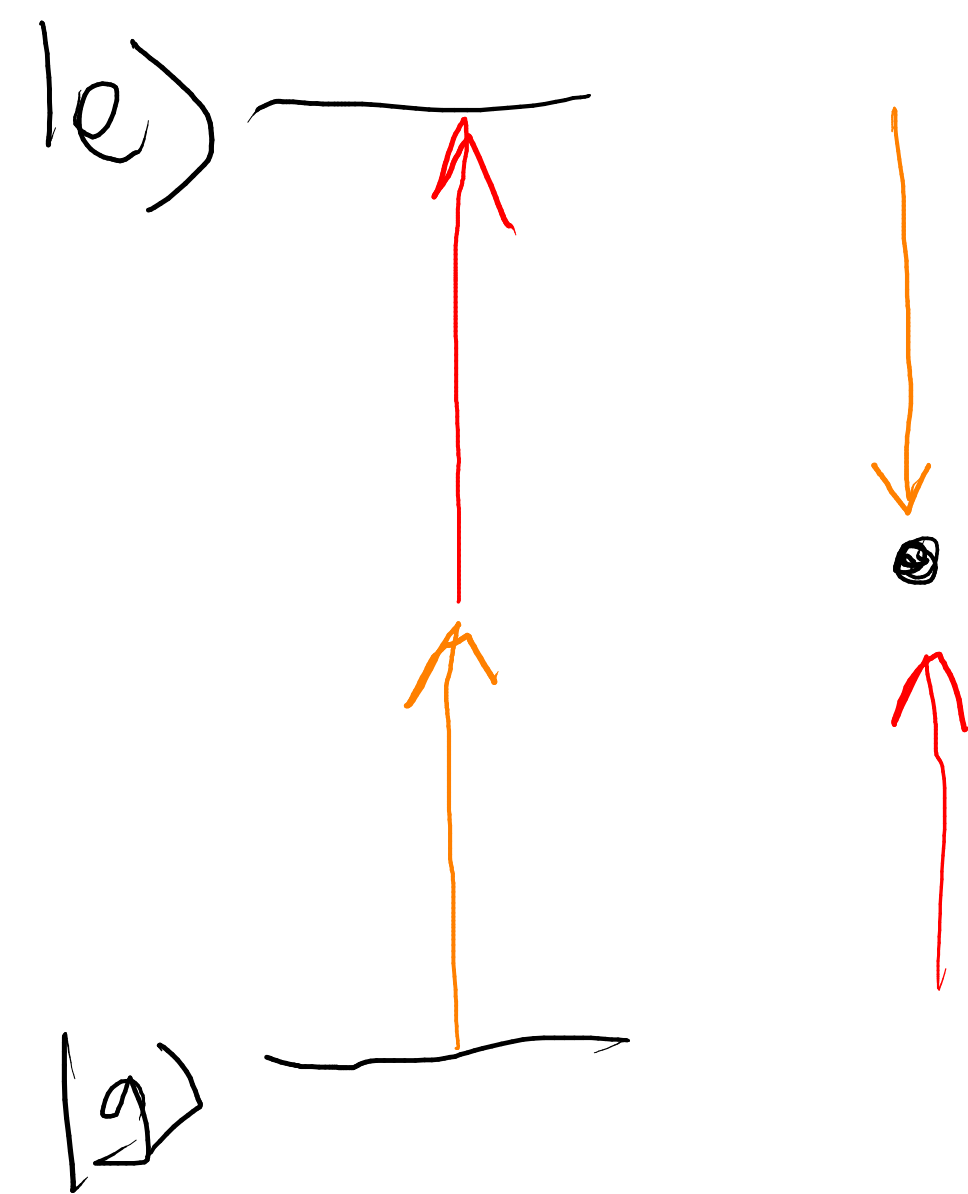
Curvature

Gouy

Curvature

Azimuthal

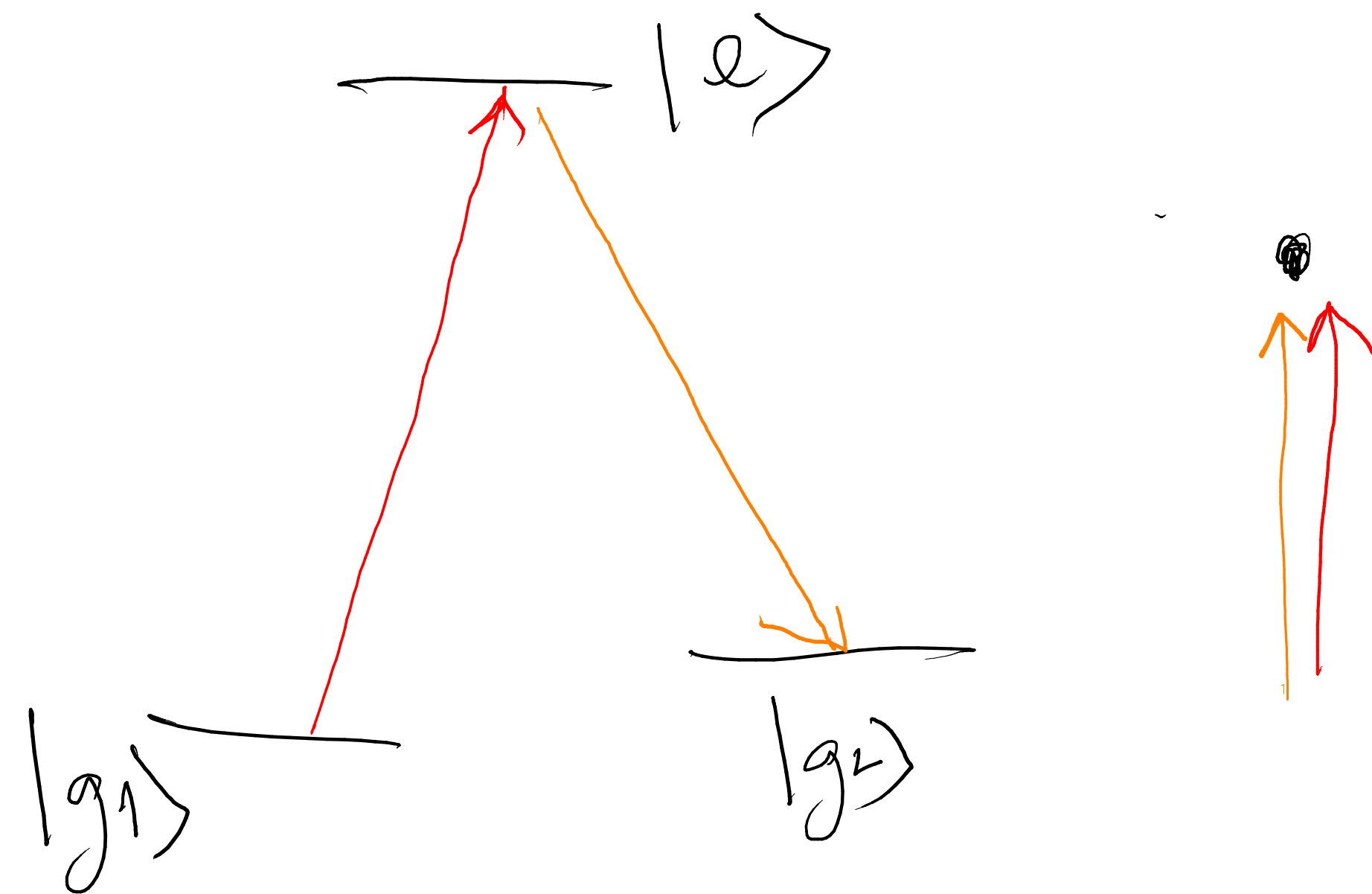
Transición de dos Fotones



$$\Delta\delta = \delta_{k_1} - \delta_{k_2} = k_1 v - k_2 v$$

$$k_1 = k_2 \longrightarrow \Delta\delta = 0$$

Transición Raman Estimulada



$$\Delta\delta = \delta_{k_1} + \delta_{k_2} = k_1 v + k_2 v$$

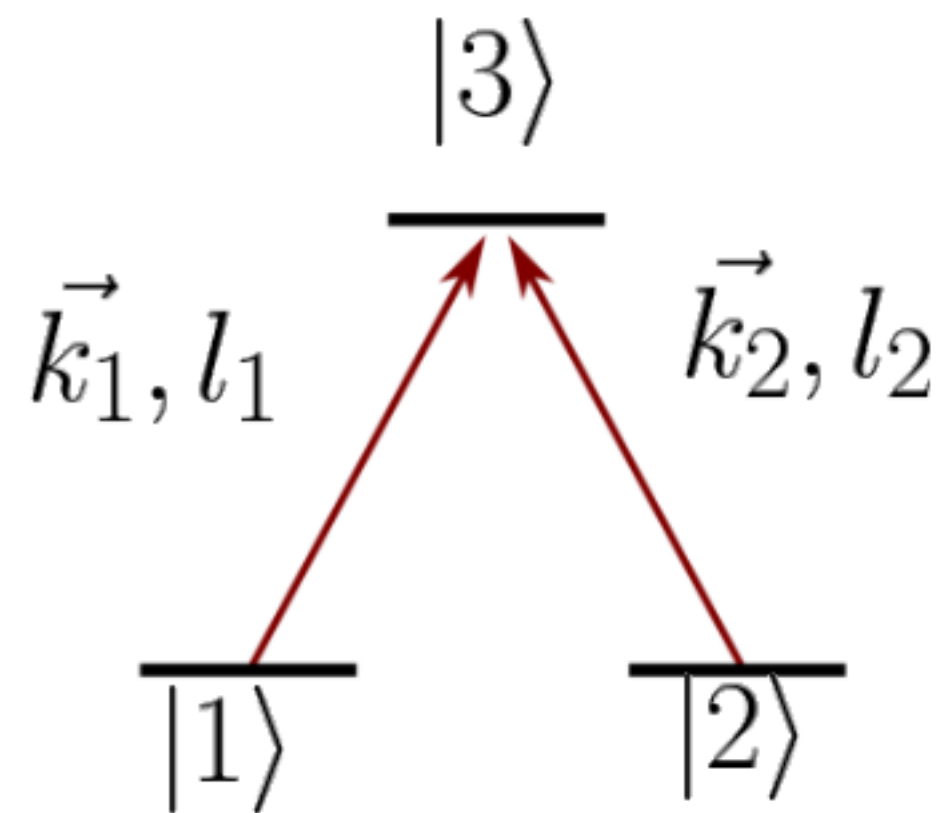
$$k_1 = -k_2 \longrightarrow \Delta\delta = 0$$

Super Doppler shifts - on two photon transitions

Doppler shift in a Laguerre-Gauss beam

$$\delta_{LG} = - \left[k + \frac{kr^2}{2(z^2 + z_R^2)} \left(\frac{2z^2}{z^2 + z_R^2} - 1 \right) - \frac{(2p + |l| + 1)z_R}{z^2 + z_R^2} \right] V_z - \left(\frac{krz}{z^2 + z_R^2} \right) V_R - \left(\frac{l}{r} \right) V_\phi$$

Two photon transitions



...they occur at equal detunings.

$$\Delta_1 = \Delta_2$$

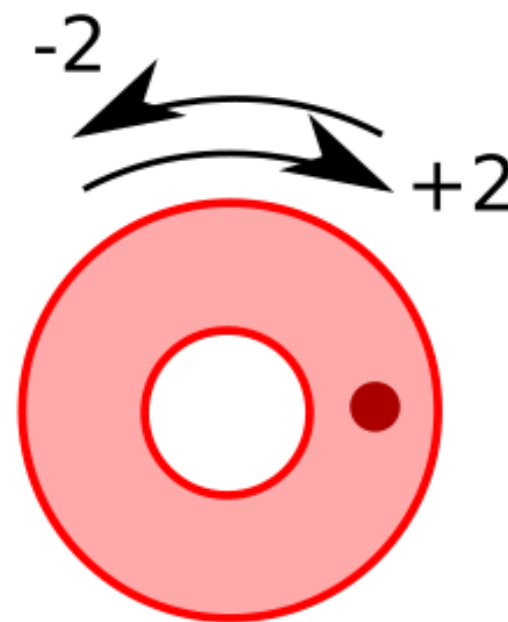
Plus, the Doppler shift for each beam!

$$\Delta_1 + \delta_{LG_1} = \Delta_2 + \delta_{LG_2}$$

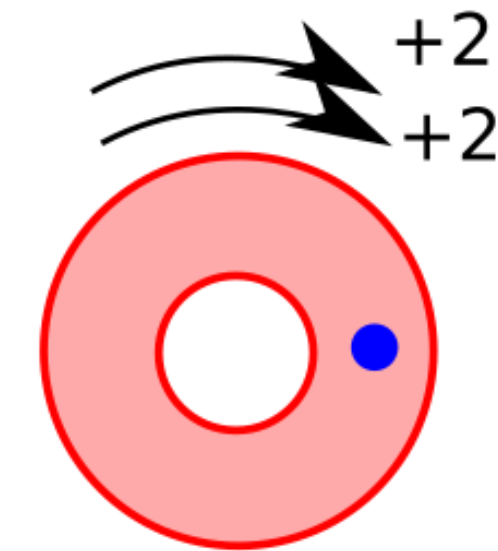
For two co-propagating beams

... all shift, except azimuthal are eliminated.

$$\Delta\delta \equiv \delta_{LG_1} - \delta_{LG_2} = \left(\frac{l_1 - l_2}{r} \right) V_\phi$$



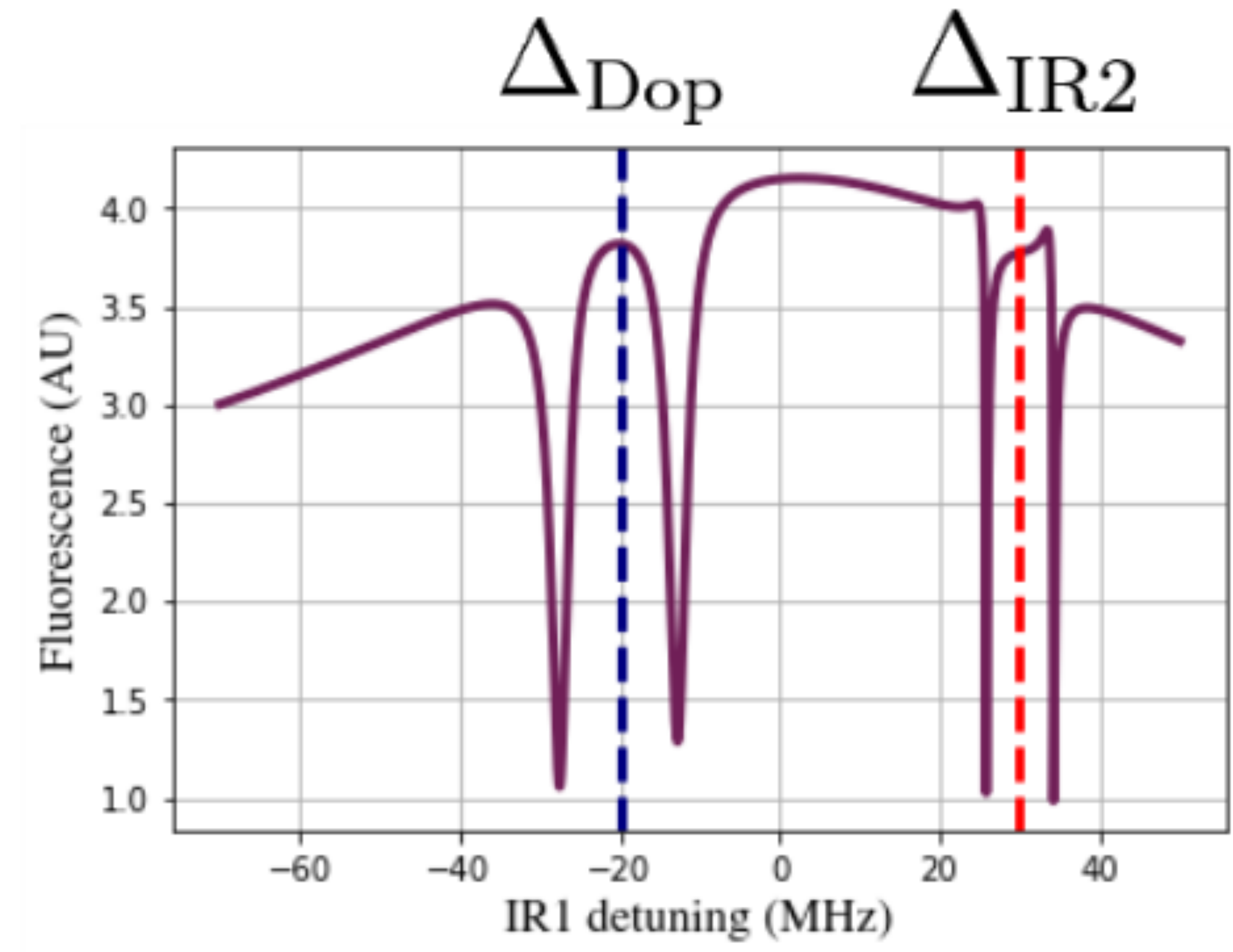
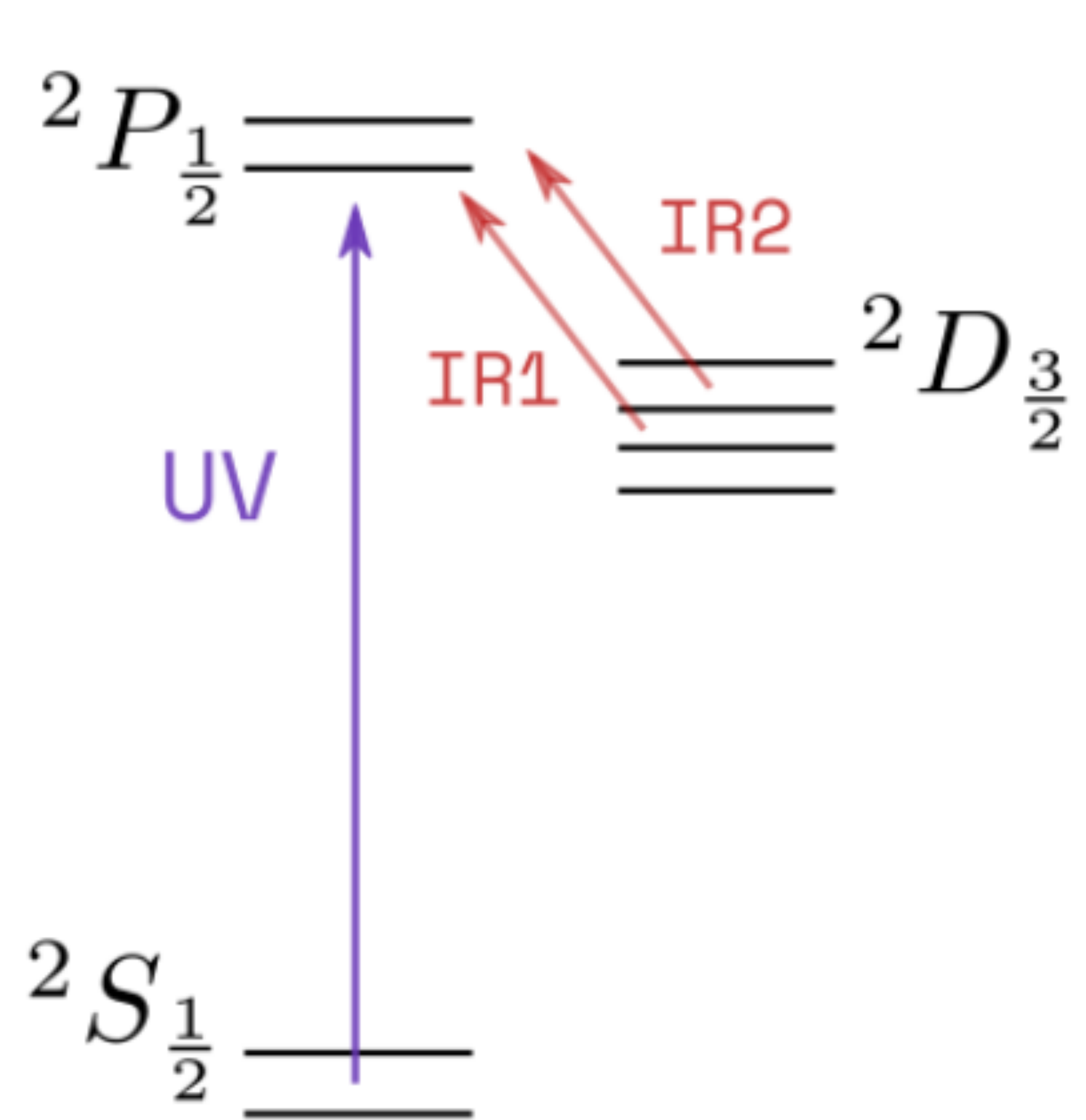
$$\Delta\delta = 0$$



$$\Delta\delta = \frac{4}{r} V_\phi$$

Super Doppler shifts EXTRA: CPT spectra in Calcium ions

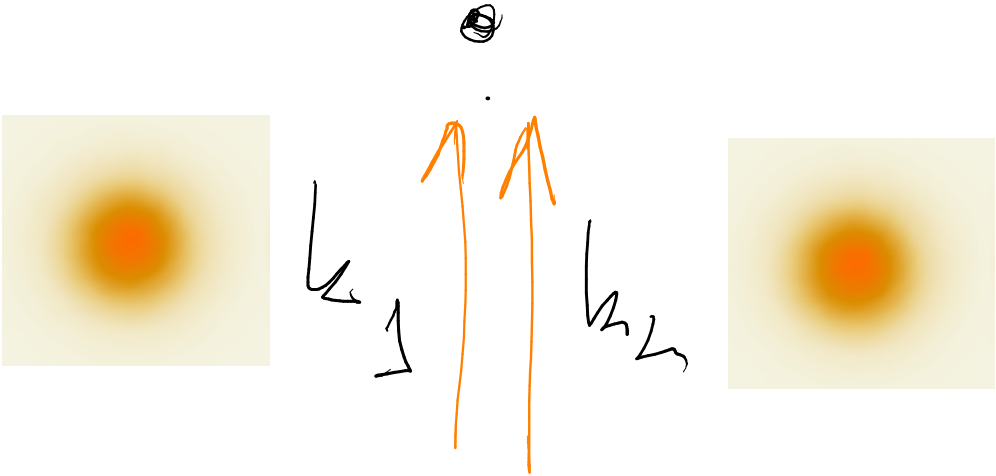
Experimental scheme with a trapped Ca^+ ion and three lasers: **dark resonances**



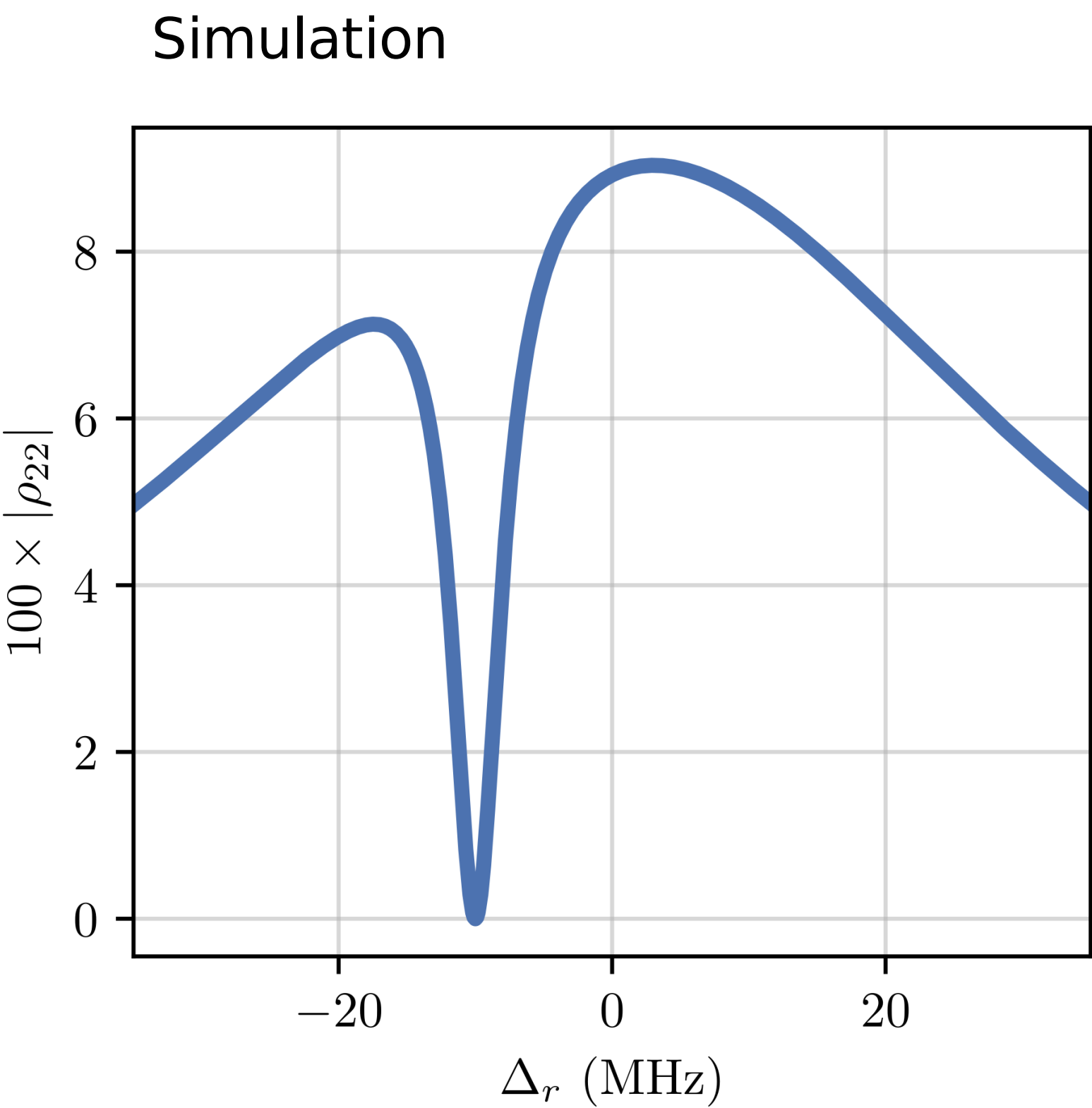
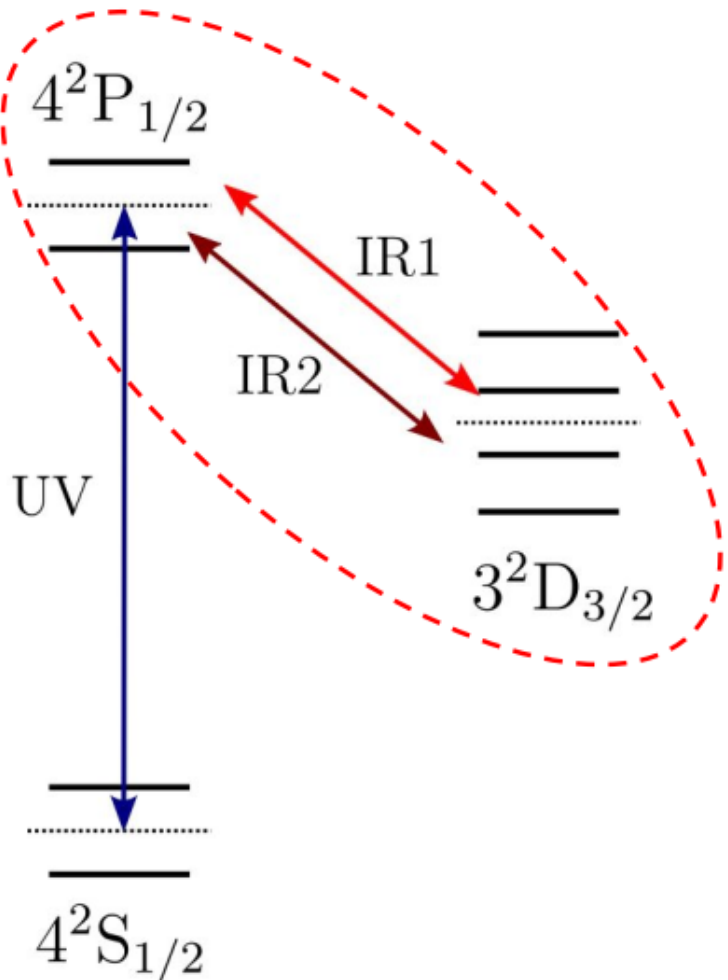
Movement insitivity - two identical beams

Stimulated Raman Transition

Expected shift

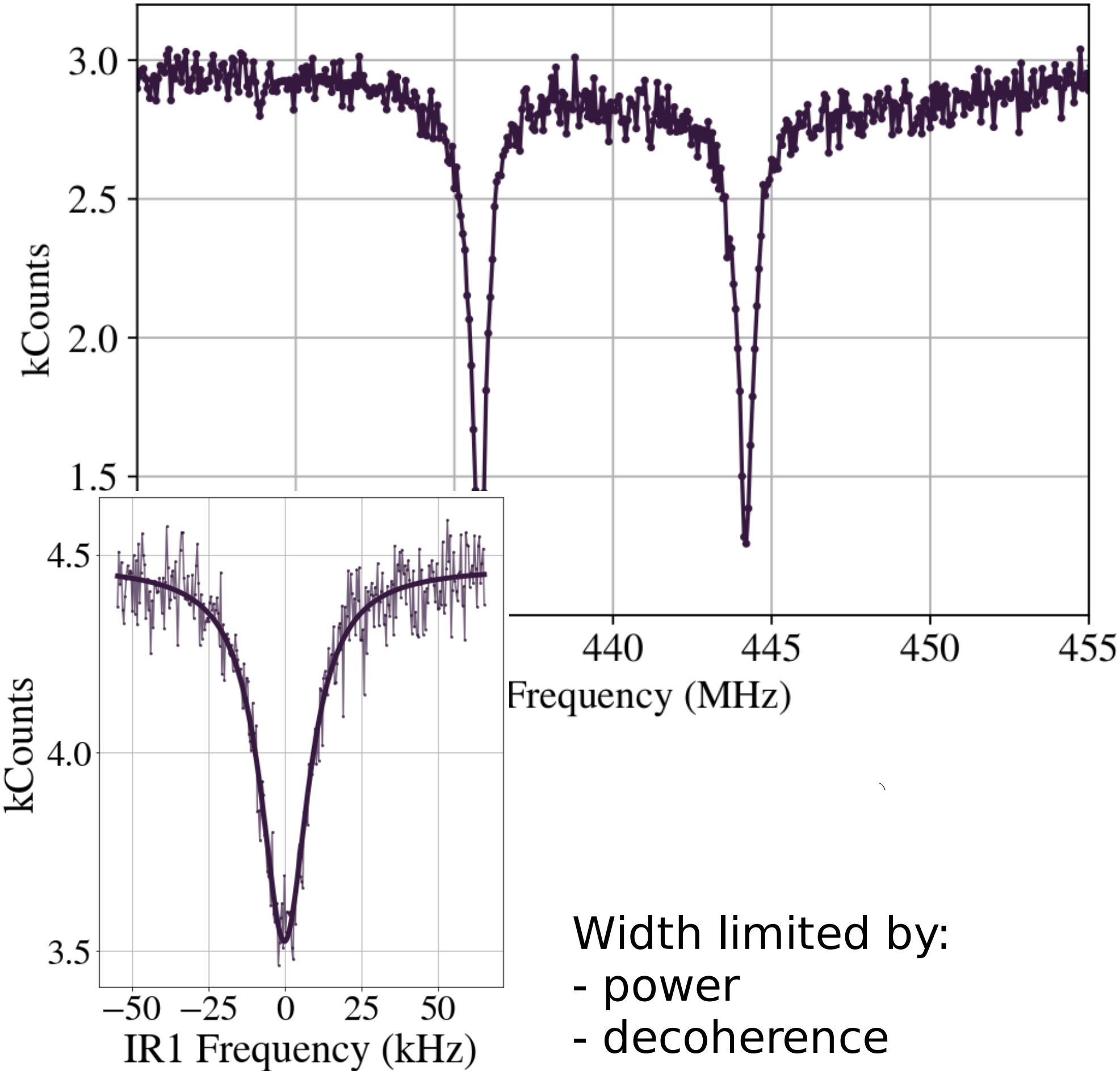


$$\Delta\delta = k_1 v - k_2 v = 0$$



- dipolar transition has ~ 10 MHz width
- dips have < 10 kHz width

Results



Width limited by:

- power
- decoherence

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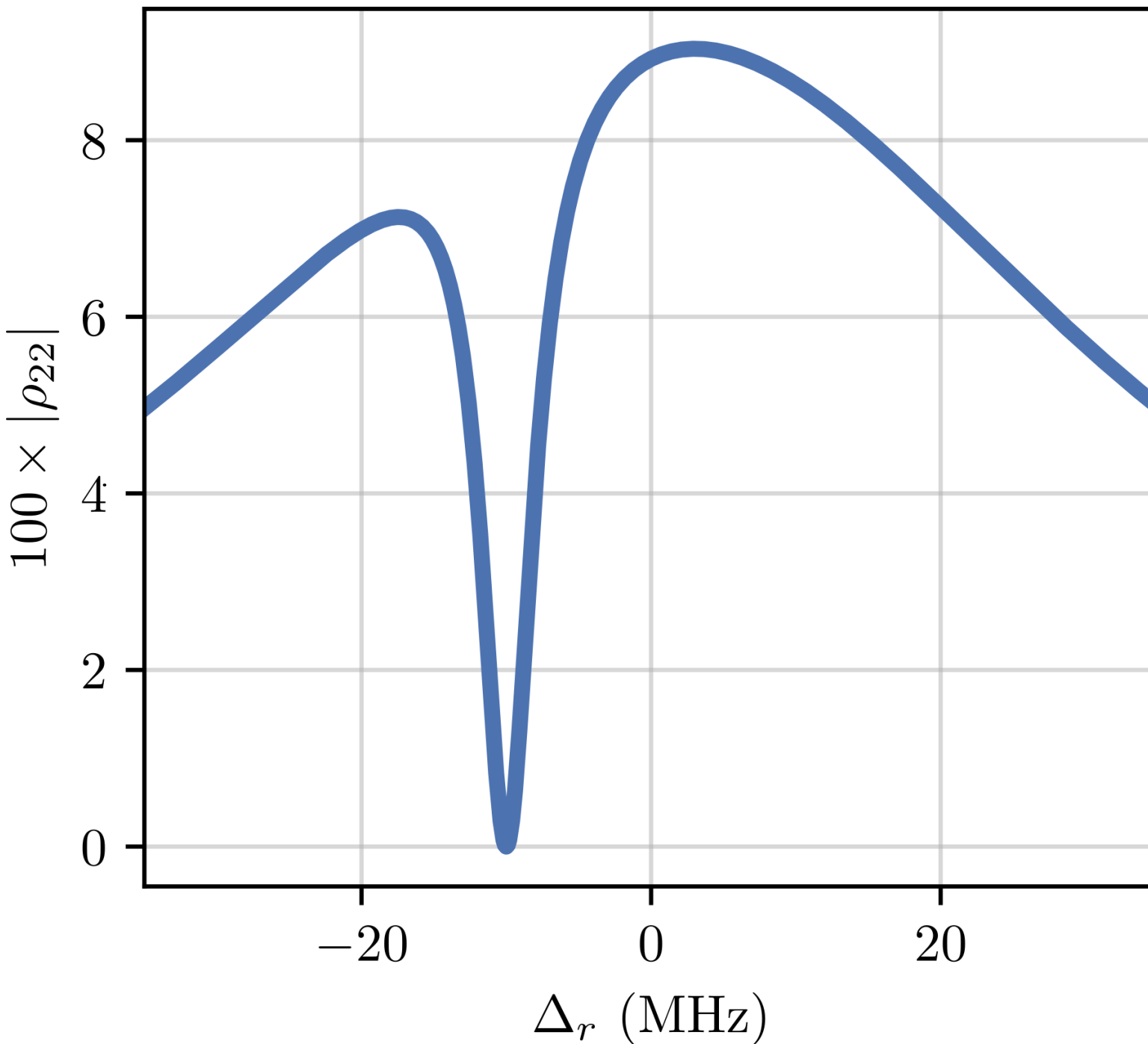
Doppler shifts - spectra with two beams at an angle

Expected shift



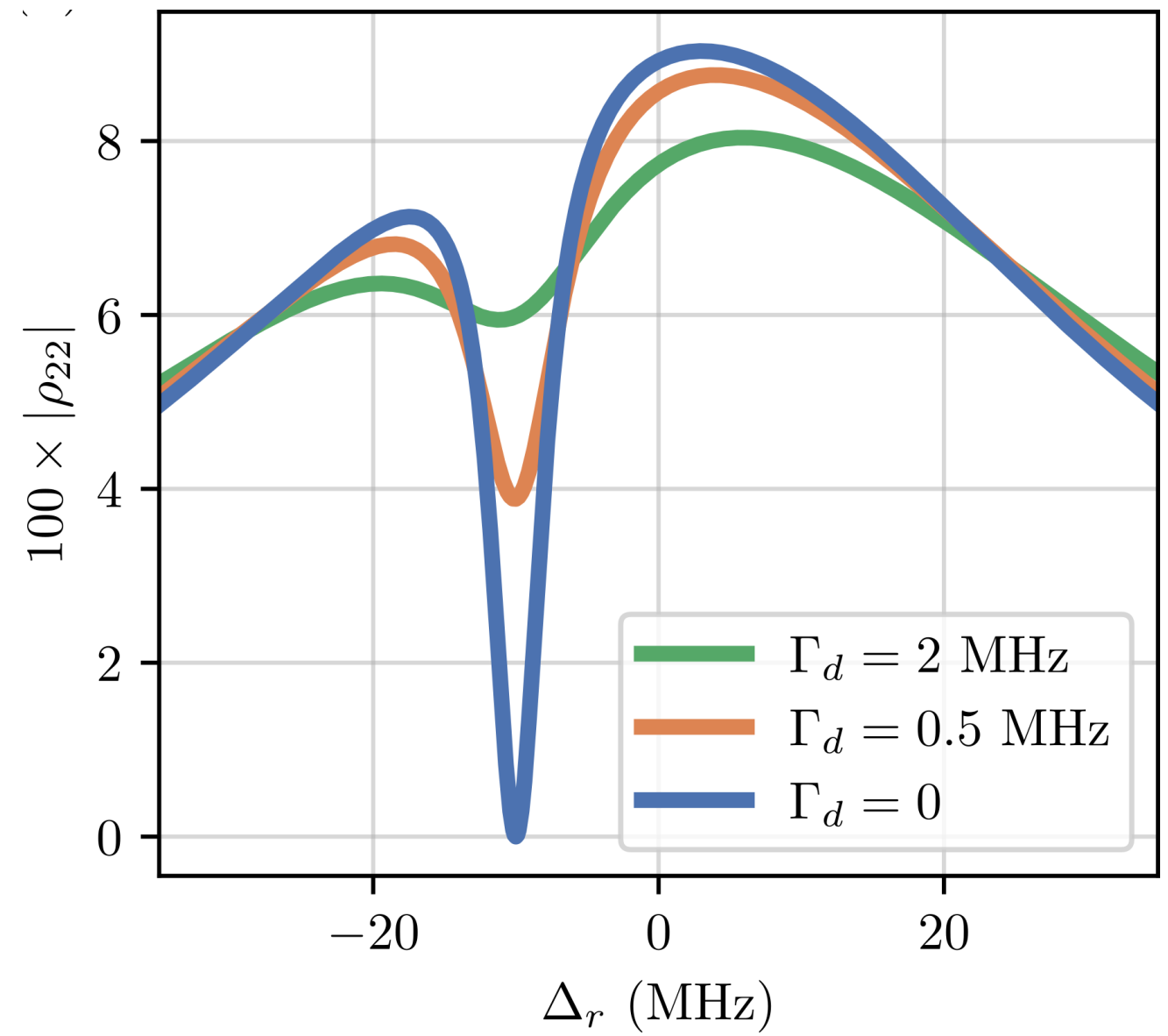
$$\Delta\delta = \Delta\vec{k} \cdot \vec{v}$$
$$\Delta\delta = \Delta k v_{\Delta k} \cos(\theta)$$

Simulation $v = 0$



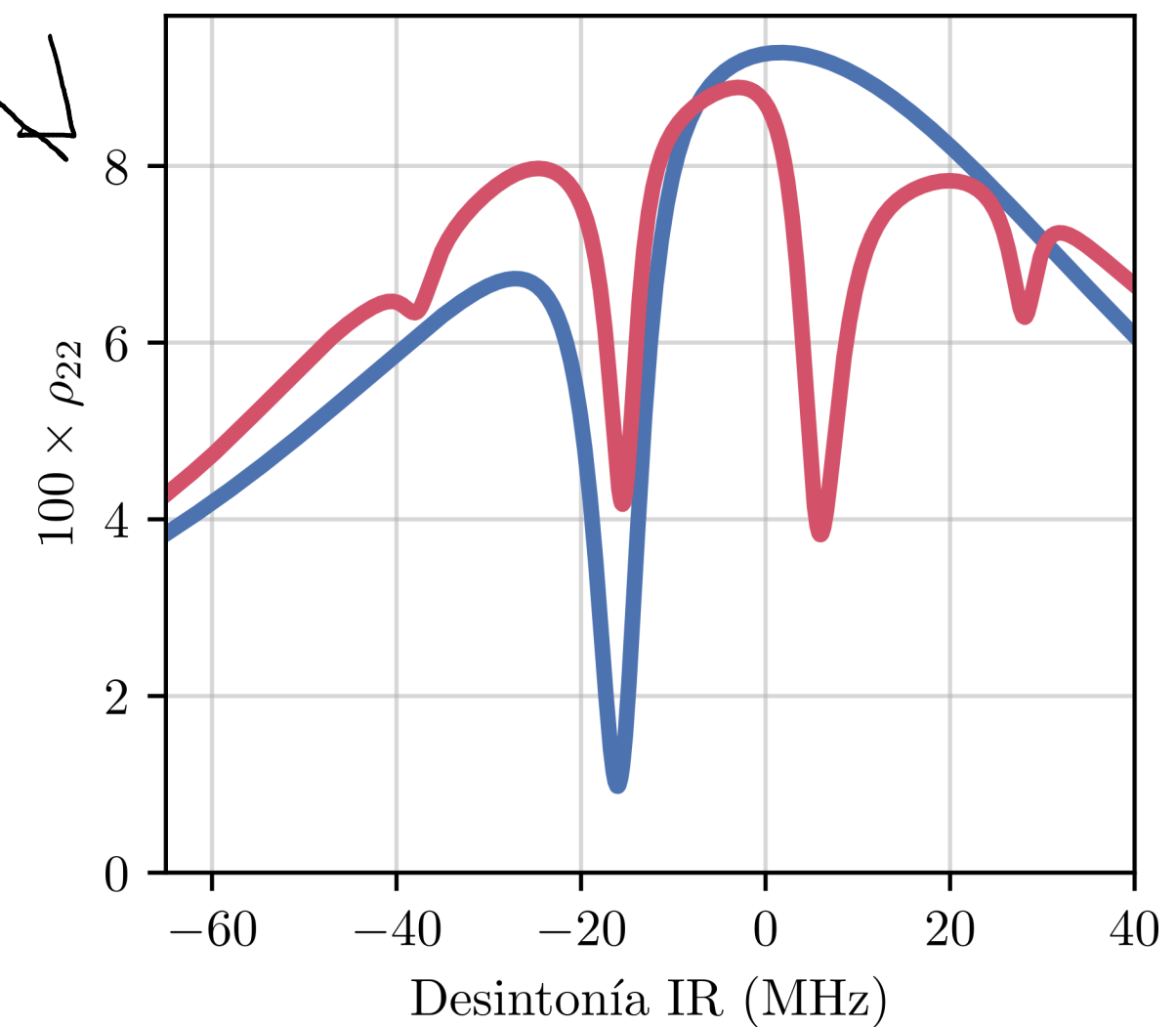
Temperature
 $p(v) \propto \exp(-mv^2/kT)$

Velocity distributions



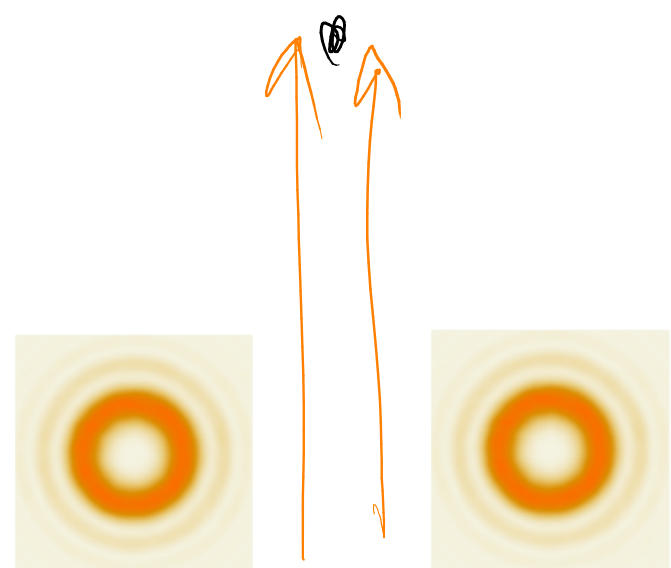
Micromotion

$$v = v_0 \sin \omega t$$

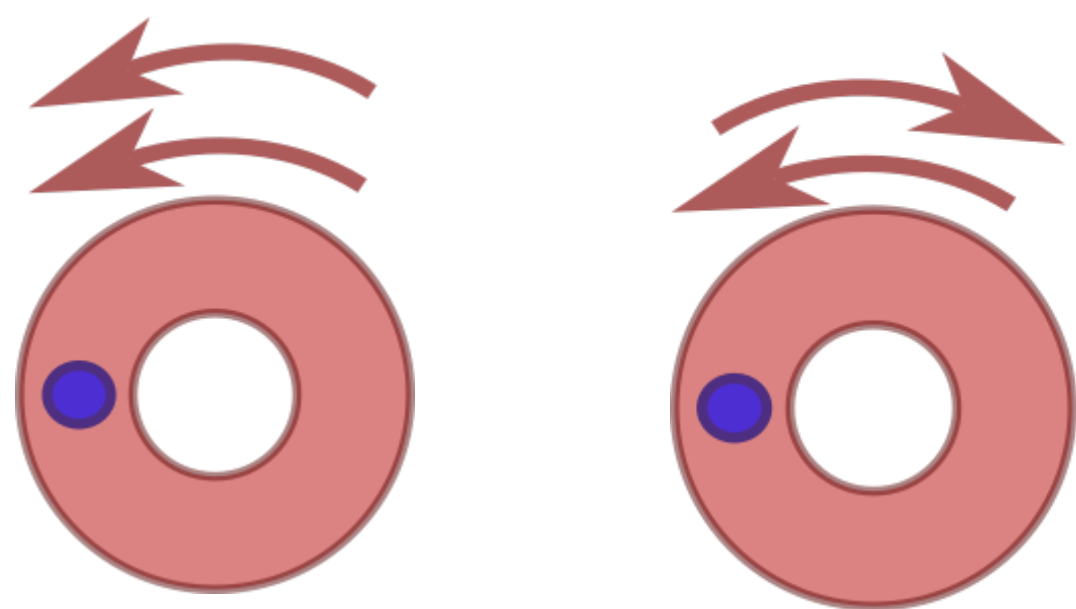


Rotational Doppler Effect - first evidence

Expected shift for $l = 2$

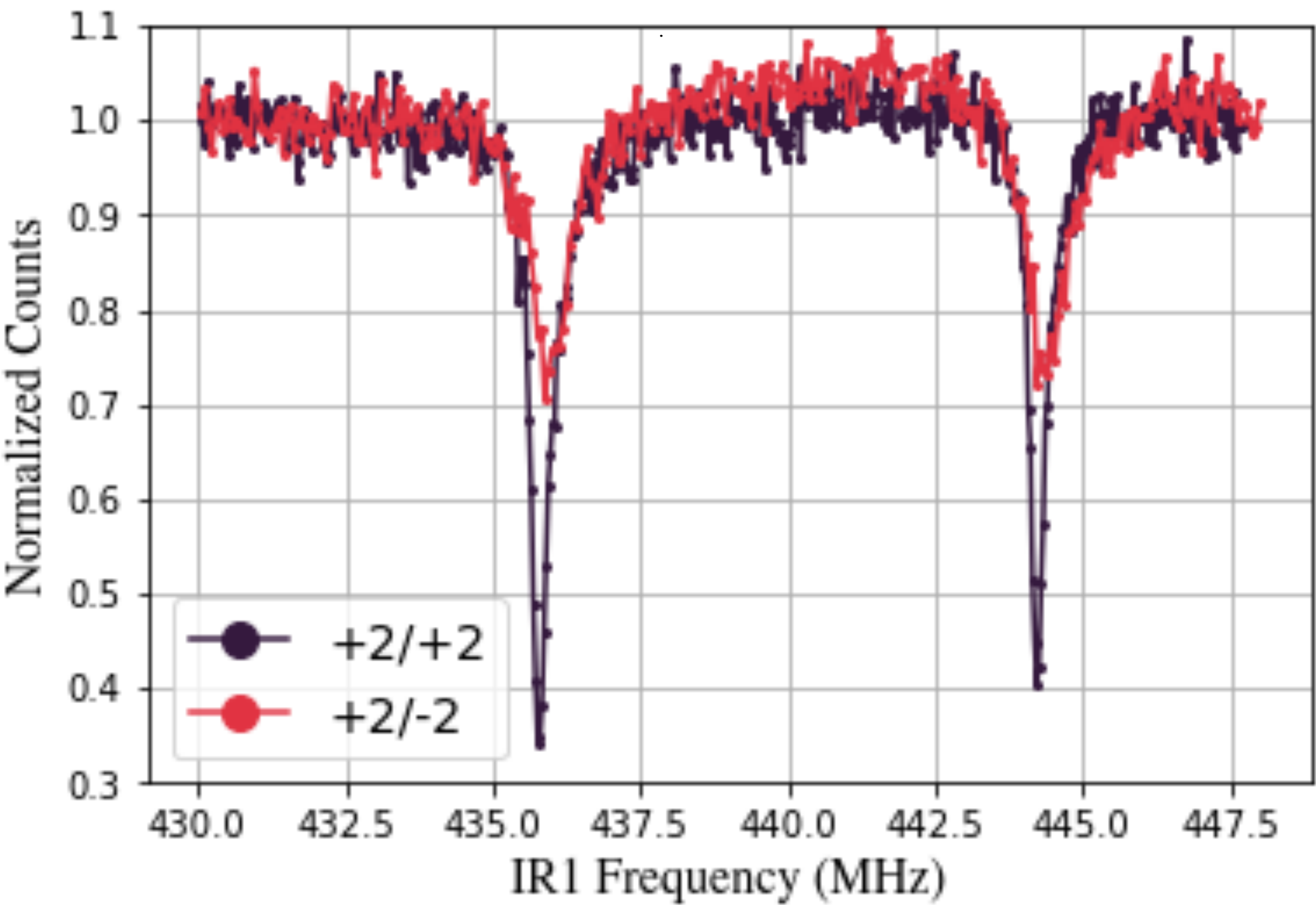


$$\Delta\delta \equiv \delta_{LG_1} - \delta_{LG_2} = \left(\frac{l_1 - l_2}{r}\right) V_\phi$$

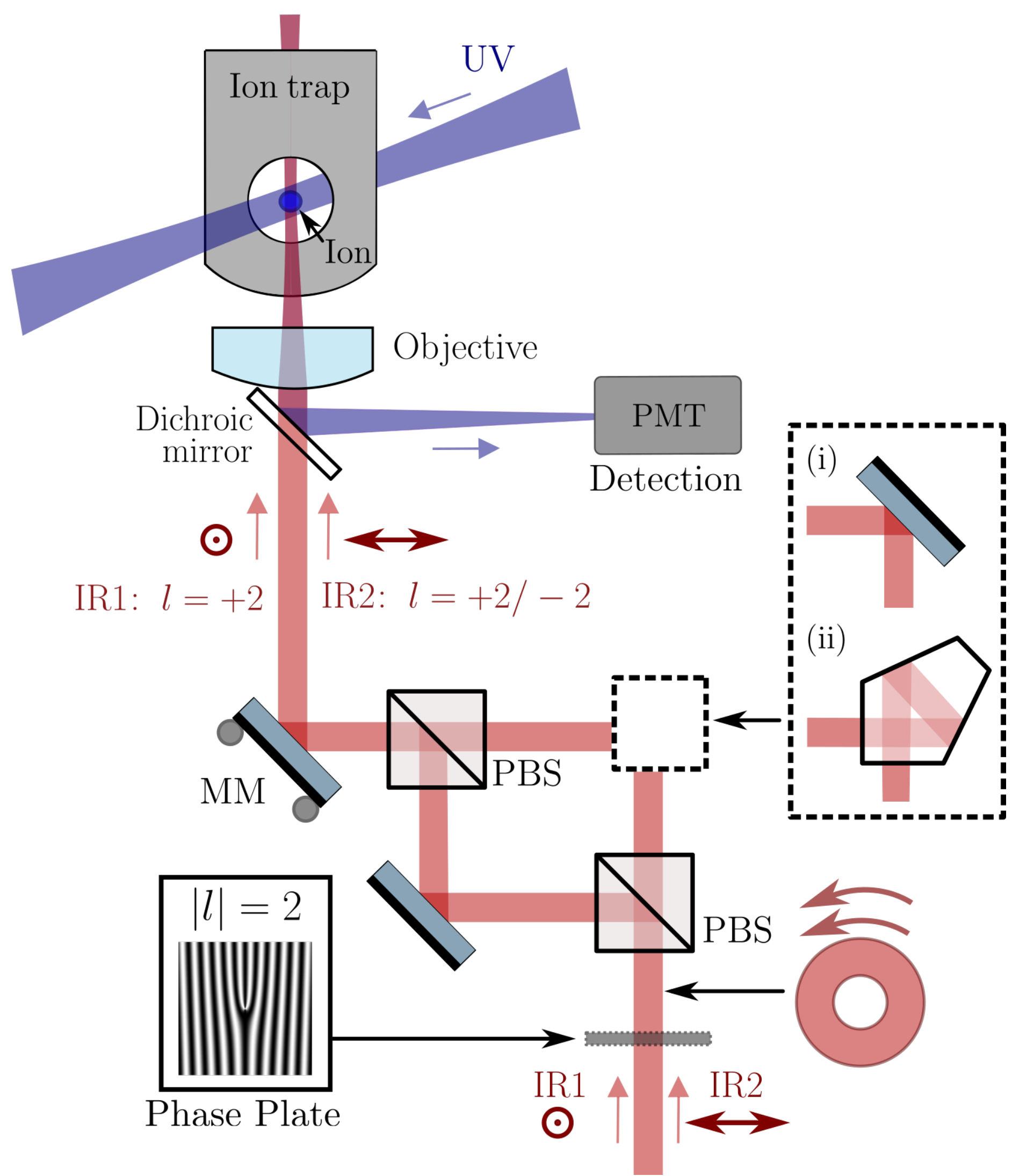


$$\Delta\delta = 0$$

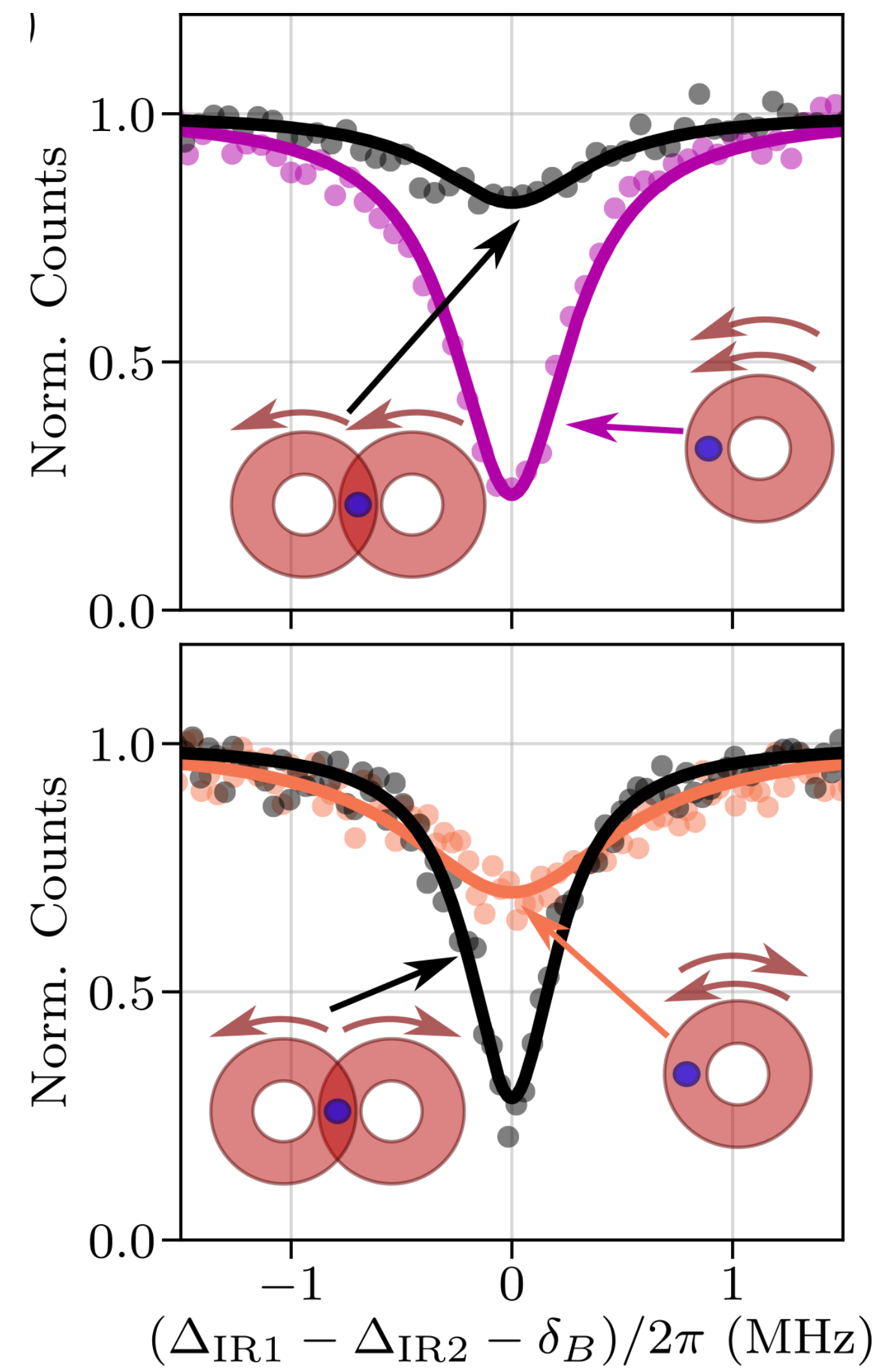
$$\Delta\delta = \frac{4}{r} V_\phi$$



Rotational Doppler Effect - ruling out ghosts



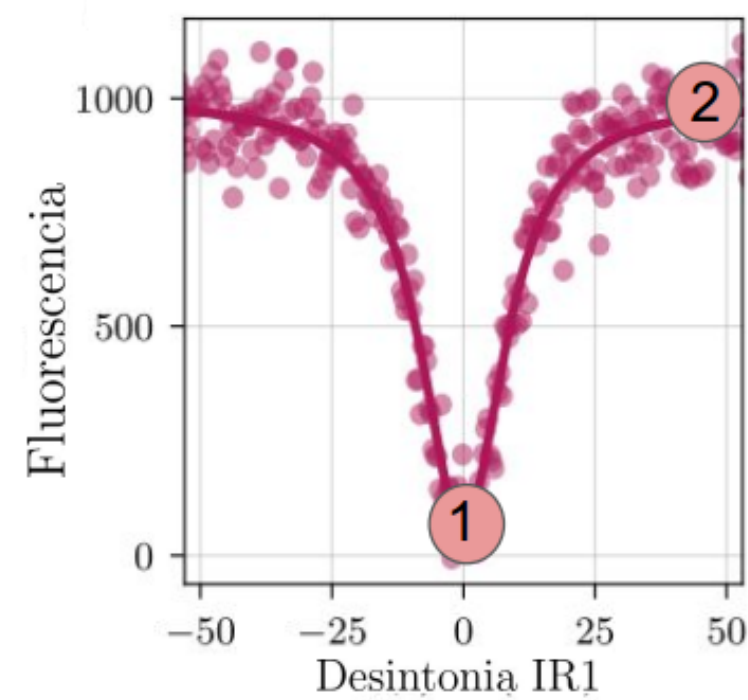
different configurations
-> it is NOT a missalignment effect!



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Rotational Doppler Effect - trasnversal scan

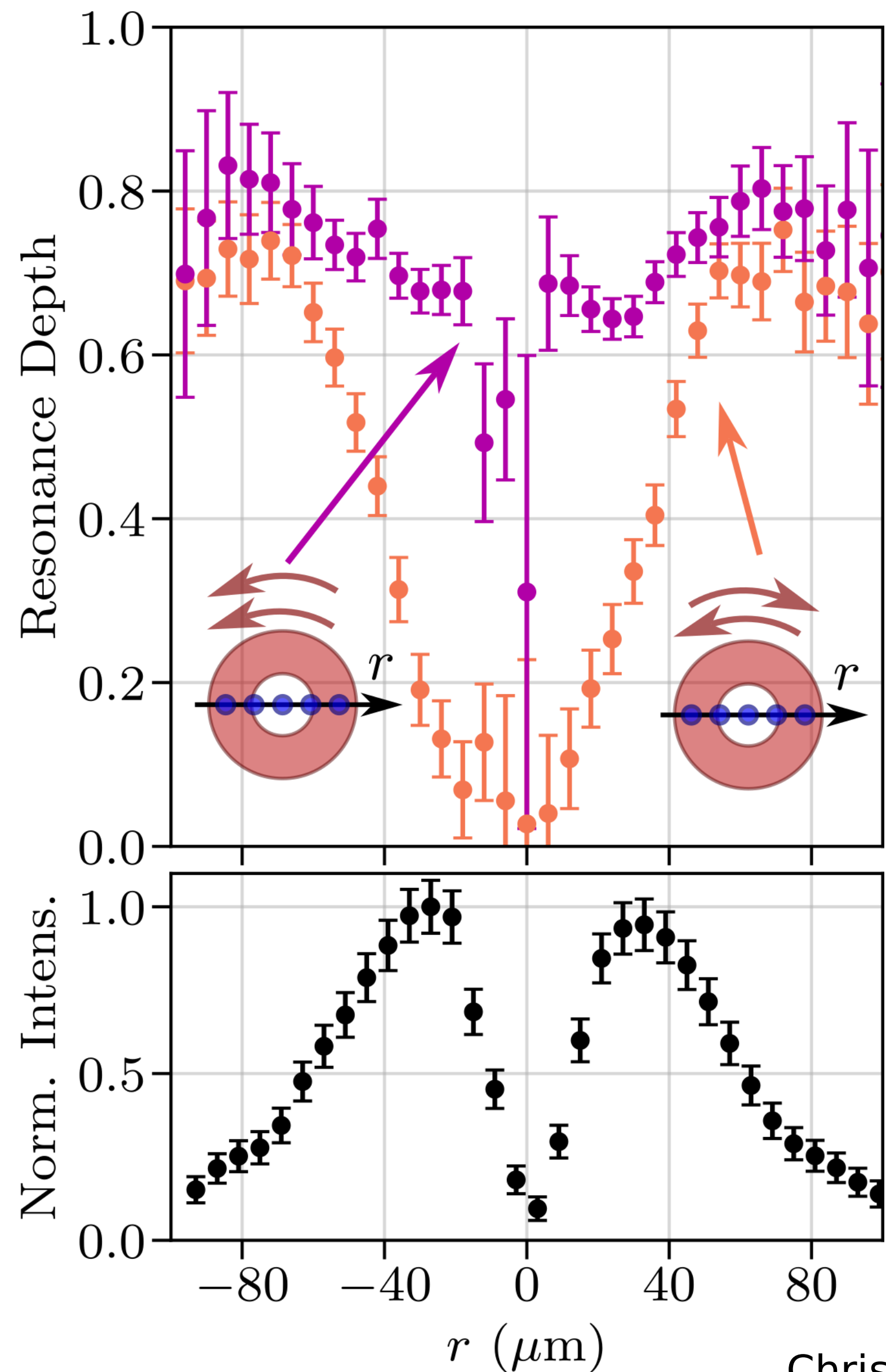
Measurement



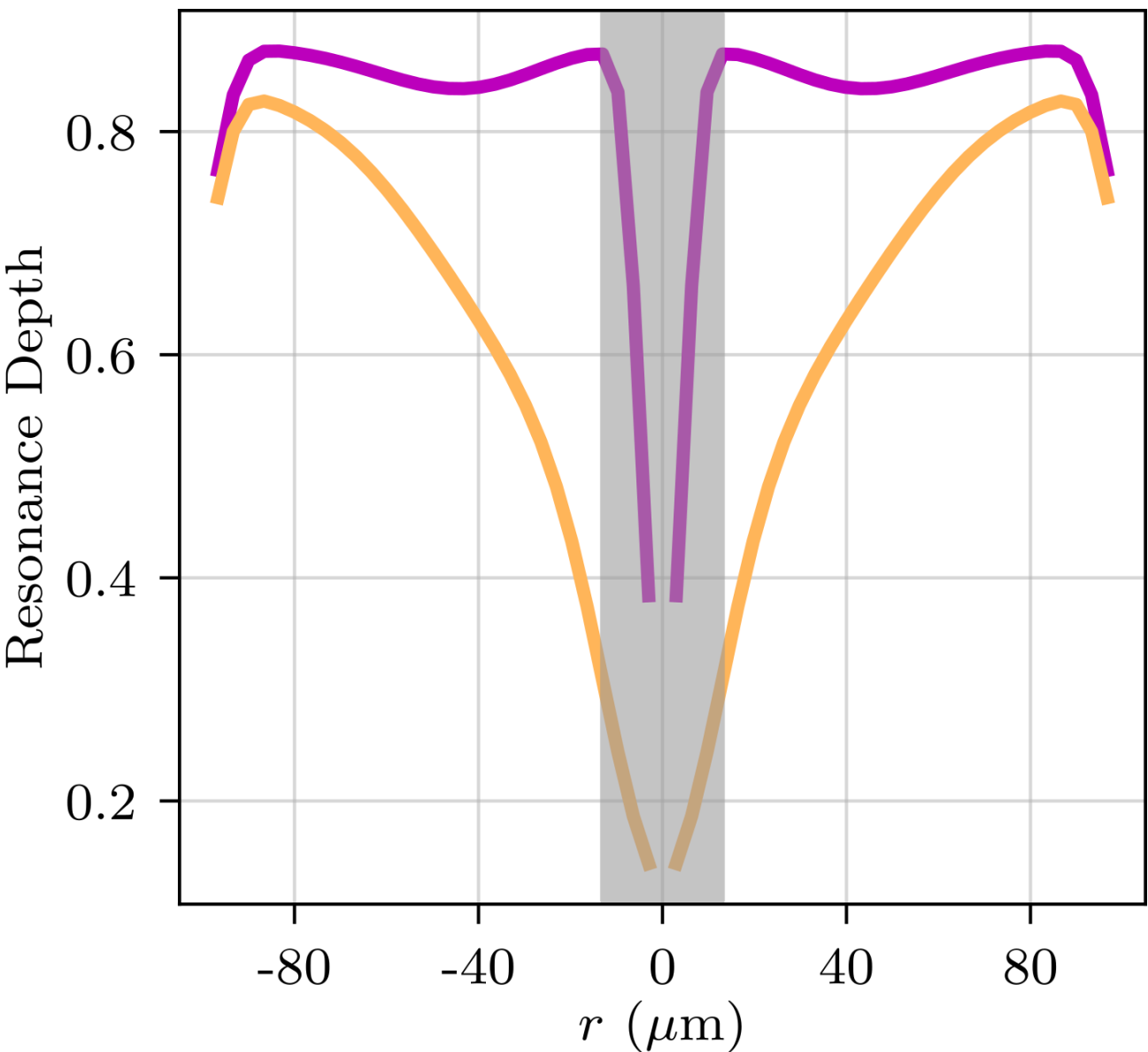
Resonance Depth

$$RD = 1 - \frac{F_1}{F_2}$$

Results



Simulation



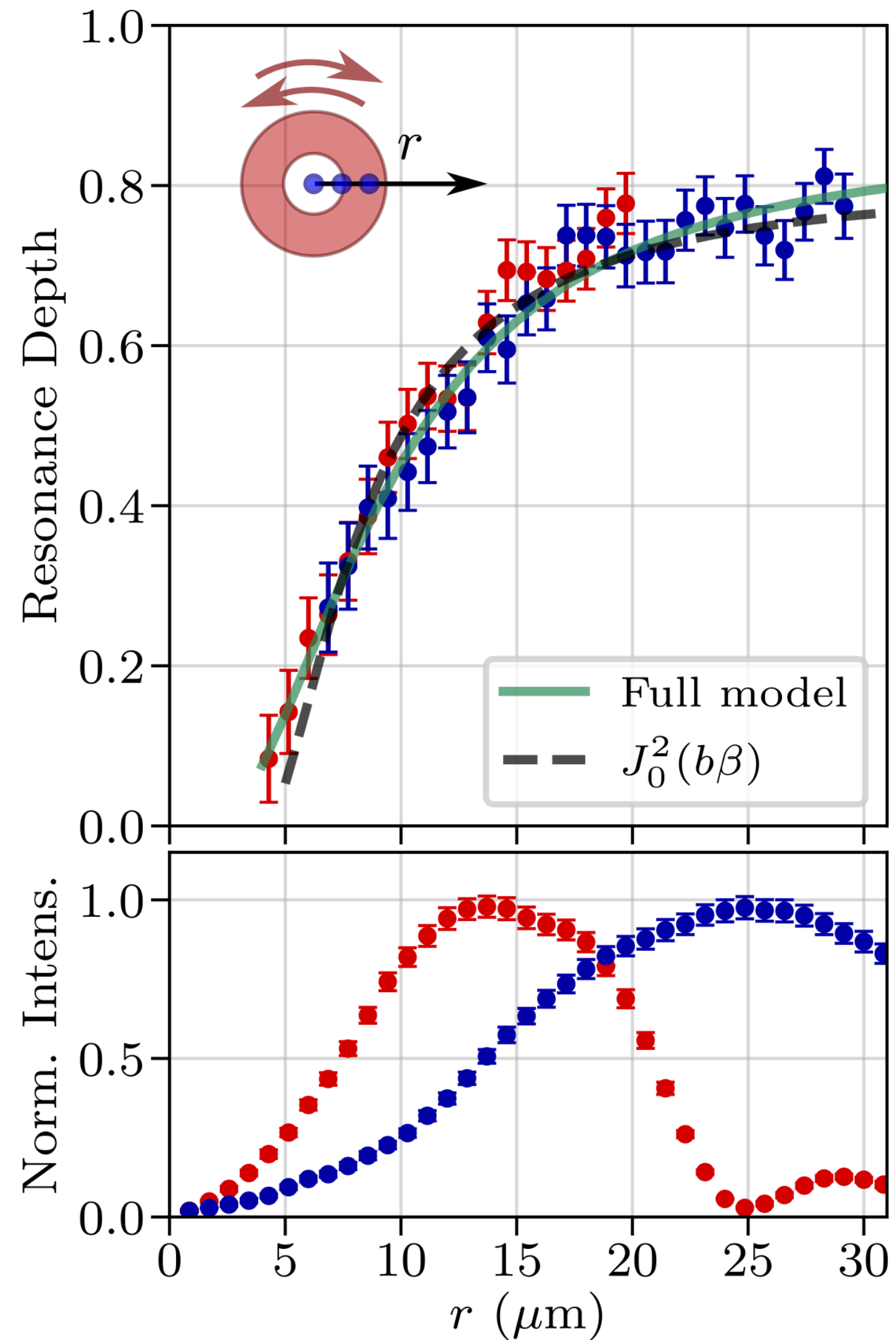
Observations

- co-rotating: no big change
- ccounter-rotating: the dip vanished

+Vanishing dip indicates:
- diverging Doppler effect.

$$\Delta\delta = \frac{4}{r}V_\phi$$

Scale invariance and modelling - trasnversal scan at constant intensity



Observations:

- it is invariant in the beam size
- full model and goss simplification fit the data!

Conclusion

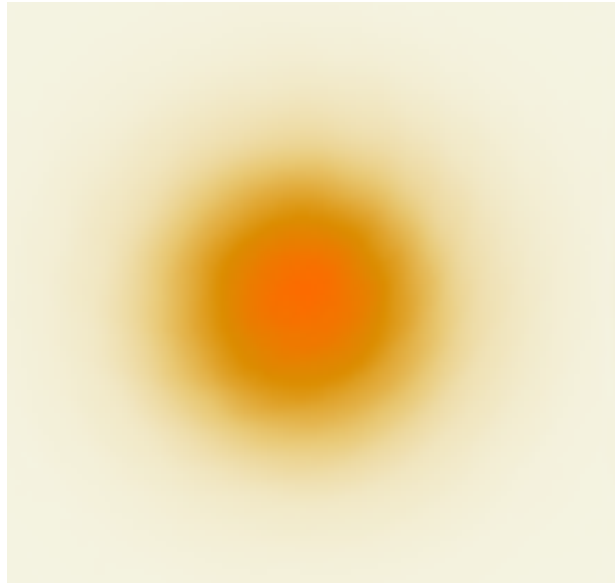
- there it is, we univocally see the doppler effect.
- it has all the structural features we expected

Perspective

- can we reach the super Doppler shift limit?
 - can we sense temperature with it?
-
- could we observe Berry super-kicks?

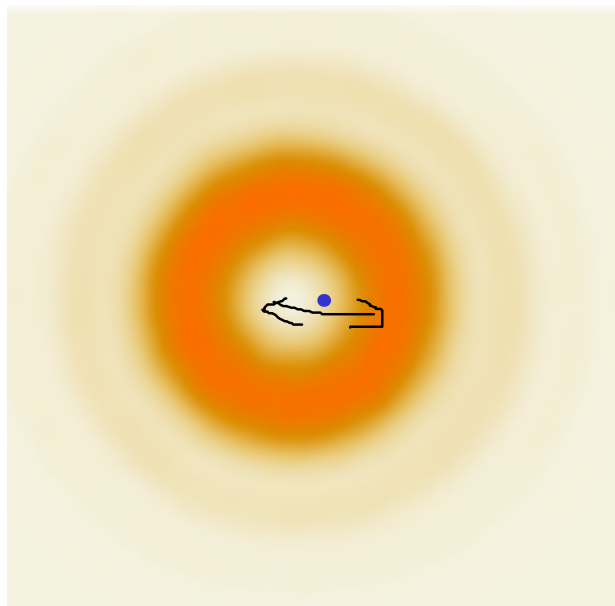
Super-kicks - azimuthal kicks, the idea of Berry y Barnett

- every sensor is an actuator, and every actuator is a sensor -



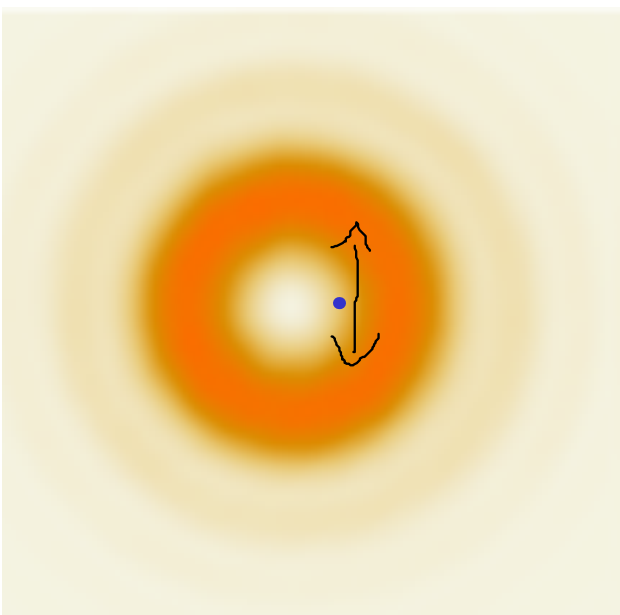
In a plan wave: longitudinal gradient

$$E = E_0 e^{ikz} \longrightarrow \Delta p = \hbar k \hat{z}$$



In previous experiment: radial gradient

$$E = E_0 e^{ikz} \rho \longrightarrow \Delta p = \hbar k \hat{z} + \hbar \frac{\hat{\rho}}{w_0}$$



and what about the azimuthal part?

$$E = E_0 e^{ikz} \rho e^{il\phi} \longrightarrow \Delta p = \hbar k \hat{z} + \hbar \frac{\hat{\rho}}{w_0} + \hbar \frac{l\hat{\phi}}{\rho}$$

transversal momentum transfer

- diverges at origin
- scale invariant!

Closing Remarks

Conclusions.

- 1) Atoms can be excited in the dark
- 2) Structured beams can transfer orbital angular momentum to bound electrons
- 3) Structured beams can transfer linear transverse momentum to whole atoms
- 4) We have seen the footprint of a super-kick

Outlook

- 1) Turning ion crystals with structured beams
- 2) Specially structured vector beams for full atomic control
- 3) Quantum gates with structured beams

Thank you for you attention.
Please leave you comments

